| L2/0 | )6-1 | 26 |
|------|------|----|
|------|------|----|

| ISO/IEC JTC 1/SC 2/WG<br>PROPOSAL SUMMARY FORM TO ACCOMPANY SUBMISSIONS<br>FOR ADDITIONS TO THE REPERTOIRE OF ISO/IEC 10646 <sup>1</sup>  | 2 N3087  |
|---|--|
| Please fill all the sections A, B and C below.<br>Please read Principles and Procedures Document (P & P) from <u>http://www.dkuug.dk/JTC1/SC2/WG2/dc</u>  | ocs/principles html for  |
| guidelines and details before filling this form.  |  |
| Please ensure you are using the latest Form from <a href="http://www.dkuug.dk/JTC1/SC2/WG2/docs/sum">http://www.dkuug.dk/JTC1/SC2/WG2/docs/sum</a><br>See also <a href="http://www.dkuug.dk/JTC1/SC2/WG2/docs/roadmaps.html">http://www.dkuug.dk/JTC1/SC2/WG2/docs/sum</a>  | maryform.html.   |
| A. Administrative   | <i>ps</i> .  |
| 1. Title: Rumi Numeral System Symbols   |  |
| 2. Requester's name: Azzeddine LAZREK   |  |
| 3. Requester type (Member body/Liaison/Individual contribution): Member b   |  |
| 4. Submission date: Cadi Ayyad University M<br>2006-03-   |  |
| 4. Submission date:       2006-03-         5. Requester's reference (if applicable):       lazrek@ucam.a  |  |
| 6. Choose one of the following:   |  |
| This is a complete proposal: <u>http://www.ucam.ac.ma/fssm/rydarab/doc/</u>   | unicode/amosl.pdf  |
| (or) More information will be provided later:   |  |
| B. Technical – General  |  |
| <ol> <li>Choose one of the following:</li> <li>a. This proposal is for a new script (set of characters):</li> </ol>   |  |
| Proposed name of script:  |  |
| b. The proposal is for addition of character(s) to an existing block: addition of characters<br>Name of the existing block:   | s to existing blocks   |
| 2. Number of characters in proposal:  | 31   |
| 3. Proposed category (select one from below - see section 2.2 of P&P document):         A-Contemporary         C-Major extinct         F-Archaic Hieroglyphic or Ideographic         4. Proposed Level of Implementation (1, 2 or 3) (see Annex K in P&P document):   |  |
| Is a rationale provided for the choice?<br>If Yes, reference:   | Yes  |
| <ul> <li>5. Is a repertoire including character names provided?</li> <li>a. If YES, are the names in accordance with the "character naming guidelines"<br/>in Annex L of P&amp;P document?</li> <li>b. Are the character shapes attached in a legible form suitable for review?</li> </ul>  | Yes<br>Yes<br>Yes  |
| 6. Who will provide the appropriate computerized font (ordered preference: True Type, or PostSc publishing the standard? <i>True Type and LaTeX package</i>   |  |
| If available now, identify source(s) for the font (include address, e-mail, ftp-site, etc.) and include:<br>used: <u>http://www.ucam.ac.ma/fssm/rydarab/doc/unicode/rumi.ttf</u><br><u>http://www.ucam.ac.ma/fssm/rydarab/system/zip/rumi.zip</u>   | dicate the tools   |
| <ul> <li>7. References:         <ul> <li>a. Are references (to other character sets, dictionaries, descriptive texts etc.) provided?</li> <li>b. Are published examples of use (such as samples from newspapers, magazines, or other of proposed characters attached?</li> </ul> </li> <li>8. Special encoding issues:</li> </ul>   | Yes<br>sources)  |
| Does the proposal address other aspects of character data processing (if applicable) such a presentation, sorting, searching, indexing, transliteration etc. (if yes please enclose information etc.)   |  |
| 9. Additional Information:<br>Submitters are invited to provide any additional information about Properties of the proposed Chara<br>that will assist in correct understanding of and correct linguistic processing of the proposed chara<br>Examples of such properties are: Casing information, Numeric information, Currency information,<br>information such as line breaks, widths etc., Combining behaviour, Spacing behaviour, Directiona<br>Collation behaviour, relevance in Mark Up contexts, Compatibility equivalence and other Unicode<br>related information. See the Unicode standard at <u>http://www.unicode.org</u> for such information on<br>see <u>http://www.unicode.org/Public/UNIDATA/UCD.html</u> and associated Unicode Technical Repor<br>needed for consideration by the Unicode Technical Committee for inclusion in the Unicode Stand | cter(s) or script.<br>Display behaviour<br>al behaviour, Default<br>normalization<br>other scripts. Also<br>ts for information |

<sup>&</sup>lt;sup>1</sup> Form number: N3002-F (Original 1994-10-14; Revised 1995-01, 1995-04, 1996-04, 1996-08, 1999-03, 2001-05, 2001-09, 2003-11, 2005-01, 2005-09, 2005-10)

L

#### C. Technical - Justification

| 1. Has this proposal for addition of character(s) been submitted before?       No         If YES explain       No         2. Has contact been made to members of the user community (for example: National Body, user groups of the script or characters, other experts, etc.)?       Yes         If YES, with whom?       If YES, available relevant documents:       http://www.ucam.ac.ma/fssm/rydarab/doc/unicode/rumibib.doc         3. Information on the user community for the proposed characters (for example: size, demographics, information technology use, or publishing use) is included?       About 100 million of people         Reference:       Arabic scripts       About 100 million of people         Reference:       Arabic scripts       About 100 million of people         Reference:       Arabic scripts       No         1 MYES, where? Reference:       No       If YES, where? Reference:         6. After giving due considerations to the principles in the P&P document must the proposed characters be entirely in the BMP?       No         If YES, reference:       No       If YES, is a rationale provided?       No         If YES, is a rationale provided?       No       If YES, is a rationale for its inclusion provided?       No         If YES, is a rationale for its inclusion provided?       If YES, is a rationale for its inclusion provided?       No         If YES, is a rationale for its inclusion provided?       If YES, is a rationale for its inclus |
|---|
| 2. Has contact been made to members of the user community (for example: National Body,<br>user groups of the script or characters, other experts, etc.)?  If YES, available relevant<br>documents:  3. Information on the user community for the proposed characters (for example:<br>size, demographics, information technology use, or publishing use) is included? About 100 million of people<br>Reference:  4. The context of use for the proposed characters (type of use; common or rare) Reference:  5. Are the proposed characters in current use by the user community?  If YES, where? Reference:  6. After giving due considerations to the principles in the P&P document must the proposed characters be entirely<br>in the BMP?  If YES, reference:  7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)?  Yes  8. Can any of the proposed characters be encoded using a composed character sequence of either<br>existing characters or other proposed characters?  No   |
| user groups of the script or characters, other experts, etc.)?       Yes         If YES, with whom?       http://www.ucam.ac.ma/fssm/rydarab/doc/unicode/rumibib.doc         documents:       http://www.ucam.ac.ma/fssm/rydarab/doc/unicode/rumibib.doc         3. Information on the user community for the proposed characters (for example:       About 100 million of people         size, demographics, information technology use, or publishing use) is included?       About 100 million of people         Reference:       Arabic scripts         4. The context of use for the proposed characters (type of use; common or rare)       rare         Reference:   |
| If YES, with whom?       http://www.ucam.ac.ma/fssm/rydarab/doc/unicode/rumibib.doc         documents:       http://www.ucam.ac.ma/fssm/rydarab/doc/unicode/rumibib.doc         3. Information on the user community for the proposed characters (for example:       about 100 million of people         size, demographics, information technology use, or publishing use) is included?       About 100 million of people         Reference:       Arabic scripts         4. The context of use for the proposed characters (type of use; common or rare)       rare         Reference:       Solution         5. Are the proposed characters in current use by the user community?       No         If YES, where? Reference:       No         6. After giving due considerations to the principles in the P&P document must the proposed characters be entirely in the BMP?       No         If YES, reference:       No         7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)?       Yes         8. Can any of the proposed characters be considered a presentation form of an existing character or character sequence?       No         If YES, is a rationale for its inclusion provided?       If YES, reference:         9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?       No  |
| If YES, available relevant<br>documents:       http://www.ucam.ac.ma/fssm/rydarab/doc/unicode/rumibib.doc         3. Information on the user community for the proposed characters (for example:<br>size, demographics, information technology use, or publishing use) is include?       About 100 million of people         Reference:       Arabic scripts         4. The context of use for the proposed characters (type of use; common or rare)       rare         Reference:  |
| documents:         3. Information on the user community for the proposed characters (for example:<br>size, demographics, information technology use, or publishing use) is included?       About 100 million of people         Reference:       Arabic scripts         4. The context of use for the proposed characters (type of use; common or rare)       rare         Reference:  |
| <ul> <li>3. Information on the user community for the proposed characters (for example:<br/>size, demographics, information technology use, or publishing use) is included? About 100 million of people<br/>Reference:</li> <li>4. The context of use for the proposed characters (type of use; common or rare) rare<br/>Reference:</li> <li>5. Are the proposed characters in current use by the user community? No<br/>If YES, where? Reference:</li> <li>6. After giving due considerations to the principles in the P&amp;P document must the proposed characters be entirely<br/>in the BMP? No</li> <li>If YES, reference:</li> <li>7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)? Yes</li> <li>8. Can any of the proposed characters be considered a presentation form of an existing<br/>character or character sequence? No</li> <li>If YES, is a rationale for its inclusion provided?<br/>If YES, is a rationale for its inclusion provided?</li> <li>If YES, is a rationale for its inclusion provided?</li> <li>If YES, is a rationale for its inclusion provided?</li> <li>If YES, is a rationale for its inclusion provided?</li> <li>If YES, reference:</li> <li>9. Can any of the proposed characters be encoded using a composed character sequence of either<br/>existing characters or other proposed characters?</li> </ul>   |
| size, demographics, information technology use, or publishing use) is included? About 100 million of people<br>Reference: Arabic scripts 4. The context of use for the proposed characters (type of use; common or rare) rare<br>Reference: 5. Are the proposed characters in current use by the user community? No<br>If YES, where? Reference: 6. After giving due considerations to the principles in the P&P document must the proposed characters be entirely<br>in the BMP? No<br>If YES, reference: 7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)? Yes<br>8. Can any of the proposed characters be considered a presentation form of an existing<br>character or character sequence? No<br>If YES, is a rationale for its inclusion provided?<br>If YES, is a rationale for its inclusion provided?<br>If YES, is a rationale for its inclusion provided?<br>If YES, reference: 9. Can any of the proposed characters be encoded using a composed character sequence of either<br>existing characters or other proposed characters? No  |
| Reference:       Arabic scripts         4. The context of use for the proposed characters (type of use; common or rare)       rare         Reference:   |
| <ul> <li>4. The context of use for the proposed characters (type of use; common or rare) rare</li> <li>Reference:</li> <li>5. Are the proposed characters in current use by the user community? No</li> <li>If YES, where? Reference:</li> <li>6. After giving due considerations to the principles in the P&amp;P document must the proposed characters be entirely in the BMP? No</li> <li>If YES, reference:</li> <li>7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)? Yes</li> <li>8. Can any of the proposed characters be considered a presentation form of an existing character sequence? No</li> <li>If YES, is a rationale for its inclusion provided?</li> <li>If YES, is a rationale for its inclusion provided?</li> <li>If YES, reference:</li> <li>9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?</li> </ul>  |
| Reference:       No         5. Are the proposed characters in current use by the user community?       No         If YES, where? Reference:       No         6. After giving due considerations to the principles in the P&P document must the proposed characters be entirely in the BMP?       No         If YES, is a rationale provided?       No         If YES, reference:       No         7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)?       Yes         8. Can any of the proposed characters be considered a presentation form of an existing character or character sequence?       No         If YES, is a rationale for its inclusion provided?       No         If YES, reference:       No         9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?       No  |
| <ul> <li>5. Are the proposed characters in current use by the user community?</li> <li>If YES, where? Reference:</li> <li>6. After giving due considerations to the principles in the P&amp;P document must the proposed characters be entirely in the BMP?</li> <li>If YES, is a rationale provided?</li> <li>If YES, reference:</li> <li>7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)?</li> <li>Yes</li> <li>8. Can any of the proposed characters be considered a presentation form of an existing character sequence?</li> <li>If YES, is a rationale for its inclusion provided?</li> <li>If YES, is a rationale for its inclusion provided?</li> <li>If YES, reference:</li> <li>9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?</li> </ul>  |
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| If YES, is a rationale provided?<br>If YES, reference:<br>7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)?<br>8. Can any of the proposed characters be considered a presentation form of an existing<br>character or character sequence?<br>If YES, is a rationale for its inclusion provided?<br>If YES, reference:<br>9. Can any of the proposed characters be encoded using a composed character sequence of either<br>existing characters or other proposed characters?<br>No  |
| If YES, is a rationale provided?<br>If YES, reference:<br>7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)?<br>8. Can any of the proposed characters be considered a presentation form of an existing<br>character or character sequence?<br>If YES, is a rationale for its inclusion provided?<br>If YES, reference:<br>9. Can any of the proposed characters be encoded using a composed character sequence of either<br>existing characters or other proposed characters?<br>No  |
| If YES, reference: 7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)? 8. Can any of the proposed characters be considered a presentation form of an existing character or character sequence? If YES, is a rationale for its inclusion provided? If YES, reference: 9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?   |
| <ul> <li>7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)? Yes</li> <li>8. Can any of the proposed characters be considered a presentation form of an existing character or character sequence? No</li> <li>If YES, is a rationale for its inclusion provided? If YES, reference:</li> <li>9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters? No</li> </ul>   |
| <ul> <li>8. Can any of the proposed characters be considered a presentation form of an existing character or character sequence?</li> <li>If YES, is a rationale for its inclusion provided?</li> <li>If YES, reference:</li> <li>9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?</li> </ul>   |
| character or character sequence?       No         If YES, is a rationale for its inclusion provided?       If YES, reference:         9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?       No   |
| If YES, is a rationale for its inclusion provided?<br>If YES, reference:<br>9. Can any of the proposed characters be encoded using a composed character sequence of either<br>existing characters or other proposed characters?<br>No   |
| If YES, reference:         9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?         No  |
| 9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?  |
| existing characters or other proposed characters? No  |
|   |
| If $\mathbf{v} \models \mathbf{v}'$ is a rationale for its inclusion provided?  |
| If YES, is a rationale for its inclusion provided?  |
| If YES, reference:  |
| 10. Can any of the proposed character(s) be considered to be similar (in appearance or function)  |
| to an existing character? No  |
| If YES, is a rationale for its inclusion provided?  |
| If YES, reference:  |
| 11. Does the proposal include use of combining characters and/or use of composite sequences? No   |
| If YES, is a rationale for such use provided?   |
| If YES, reference:  |
| Is a list of composite sequences and their corresponding glyph images (graphic symbols) provided?   |
| If YES, reference:  |
| 12. Does the proposal contain characters with any special properties such as  |
| control function or similar semantics? No   |
| If YES, describe in detail (include attachment if necessary)  |
|   |
| 13. Does the proposal contain any Ideographic compatibility character(s)? No  |
| If YES, is the equivalent corresponding unified ideographic character(s) identified?  |
|   |
| If YES, reference:  |

# Rumi Numeral System Symbols,

Additional characters proposed to Unicode

Azzeddine LAZREK lazrek@ucam.ac.ma Cadi Ayyad University, Faculty of Sciences P.O. Box 2390, Marrakech, Morocco Phone: +212 44 43 46 49 Fax: +212 44 43 74 09 URL: http://www.ucam.ac.ma/fssm/rydarab

March 30, 2006

## 1 Introduction

A special numeral system  $rumi^1$  has been in use in North Africa since the X<sup>e</sup> century. It remained in use until the XVII<sup>e</sup> century. This system has been especially used in the administration of the city of Fez in Morocco. It has also been used in Al-Andalusians, Spain, starting from the XII<sup>e</sup> century. The forms of the digits are quiet different from the Arabic<sup>2</sup> or the Arabic-Indic<sup>2</sup> digits in use today. The system of numeration was decimal, but not really positional. rumi use some special symbols (see Table 1, Table 2, Table 3 and Table 4). Some examples are available (see Table 5, Table 6 and Table 7). This system is also known as "zimam letters, Roman, Fez letters" (namely Hrwf al-zmAm, al-rumi, Hrwf fAs or also rasm al-zmam, Qalam al-rumi, Qalam al-fAsy).

### 2 Description

rumi numeral system has been described by many researchers and there is many studies about it. A deailed bibliography is presented in Figure 1 (see some figures from this bibliography in the end). We have adopted the one

<sup>&</sup>lt;sup>1</sup>using Transtec Transliteration

http://www.ucam.ac.ma/fssm/rydarab/doc/communic/transtec.pdf

<sup>&</sup>lt;sup>2</sup>the identifier name used by The Unicode Consortium http://www.unicode.org

described by the mathematician Ibn Al-Banna (1256-1321, Marrakech) in his famous book [1] "Abstract of using rumi in calculus" in Arabic (namely Al-YqtDAb mn al-Eml b-al-rwmI fI al-HsAb).

rumi use some special symbols for digits:

- rumi ones are(see Table 1):  $\mathbf{J}, \mathbf{J}, \mathbf{K}, \mathbf{K}, \mathbf{\Lambda}, \mathbf{T}, \mathbf{\Gamma}, \mathbf{T}, \mathbf{J}, \mathbf{J}, \mathbf{S}$ .
- rumi tens are (see Table 2):  $c, w, J, \mathcal{E}, \mathcal{N}, \mathcal{E}, o, \mathcal{L}, \mathcal{E}$ .

Multiples of thousand are represented by adding a slash under the based number:

- rumi thousands are noted by one bar under the number (see Table 5) (ex.,  $\checkmark$  for three thousands);
- rumi million are noted by two bars under the number (see Table 6) (ex.,  $\checkmark$  for three million);
- and so on.

Fraction is represented by adding a slash symbol separating the numerator from the denominator:

- rumi fractions are generally noted by (see Table 7):
- Some special fractions are also noted by (see Table 4): 3, //, /, /, //,

### 3 proposition

These symbols are proposed to be included in Unicode Standard. There names are descriped in rumi ones digits (see Table 8), rumi tens digits (see Table 9) rumi handreds digits (see Table 10) and rumi specila fractions (see Table 11).

As many manuscripts in studying use these symbols, we need to encode them. We are working on studying and translating to english the Ibn Al-Banna manuscript Al-YqtDAb mn al-Eml b-al-rwmI fI al-HsAb. A computer system for transforming numbers from and to rumi numeral system is also in development.

The **rumi** and **AntiSym** fonts available, includes all these characters. In **rumi** font, used here, the shapes of the reference glyphs are scanned from [1]. It's in OpenType format [3] and converted in METAFONT as a LATEX package [4]. In **AntiSym** font, glyphs are drawing by hand in METAFONT as a LATEX package [2].

The shapes of the reference glyphs used are not frozen. They are continually being improved in *Multilingual scientific e-document processing* Project at Al-khawarizmi Atelier.

Some boxes are add to some symbols in Figures in order to emphases them and understand the purpose of the samples.

More information about this presentation is available in [5].

# References

- [1] Ibn Al-Banna (1256-1321, Marrakech), Abstract of using rumi in calculus, in Arabic.
- [2] Arabic mathematical old symbols package antisym for LATEX, http://www.ucam.ac.ma/fssm/rydarab/system/zip/antisym.zip.
- [3] rumi numeral system font in OpenType, http://www.ucam.ac.ma/fssm/rydarab/doc/unicode/rumi.ttf.
- [4] rumi numeral system as a package for LATEX, http://www.ucam.ac.ma/fssm/rydarab/system/zip/rumi.zip.
- [5] Azzeddine Lazrek, Arabic mathematical symbols for Unicode, http://www.ucam.ac.ma/fssm/rydarab/english/unicode.htm.



Table 1: rumi ones symbols

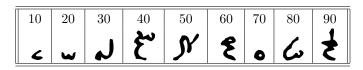


Table 2: rumi tens symbols

| 100 | 200 | 300 | 400 | 500 | 600 | 700 | 800 | 900 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| e   | ケ   | હ   | メ   | 9   | ð   | 4   | 7   | ٣   |

Table 3: rumi handreds symbols

| 1/2 | 1/4 | 1/3 | 2/3 |
|-----|-----|-----|-----|
| ŕ   | 7   | مر  | *   |

Table 4: rumi special fractions symbols

| 1000     | 2000     | 3000   | 4000   | 5000       | 6000   | 7000   | 8000   | 9000     |
|----------|----------|--------|--------|------------|--------|--------|--------|----------|
| 2        | 5        | ~~     | ^      | 7          | /      | 2      | 4      | গ্র      |
| 10000    | 20000    | 30000  | 40000  | 50000      | 60000  | 70000  | 80000  | 90000    |
| <u>د</u> | <b>w</b> | 2      | بح     | <u>s</u> r | 2      | 0      | لم     | <u></u>  |
| 100000   | 200000   | 300000 | 400000 | 500000     | 600000 | 700000 | 800000 | 900000   |
| e        | ヶ        | ٤      | と      | 2          | ð      | 4      | 7      | <u> </u> |

Table 5: rumi thousands examples

4

| 1000000  | 2000000   | 3000000   | 4000000   | 5000000   | 6000000   | 7000000   | 8000000  | 9000000  |
|----------|-----------|-----------|-----------|-----------|-----------|-----------|----------|----------|
| <b>)</b> | 5         | ~~        | <u>^</u>  | ケ         |           | 2         | 5        | ىك       |
| 10000000 | 2000000   | 30000000  | 40000000  | 50000000  | 60000000  | 70000000  | 8000000  | 9000000  |
| ٤        | w         | لم        | ٣         | SV.       | ٤         | 0         | ل        | Z        |
| 10000000 | 200000000 | 300000000 | 400000000 | 500000000 | 600000000 | 700000000 | 80000000 | 90000000 |
| <b>_</b> | ケ         | ٤         | <b>×</b>  | <b>P</b>  | *         | 4         | 2        | <u>¥</u> |

Table 6: rumi millions examples

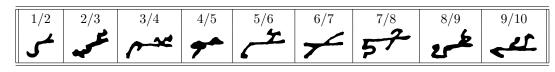


Table 7: rumi fractions examples

| 3        | RUMI DIGIT ONE  |
|----------|---|
|          | $\approx$ 0031 1 digit one                                      |
|          | $\approx$ 0661 \ Arabic-Indic digit one                         |
| 5        | RUMI DIGIT TWO  |
|          | $\approx$ 0032 2 digit two                                      |
|          | $\approx 0662$ $\Upsilon$ Arabic-Indic digit two                |
| ~        | RUMI DIGIT THREE  |
| • -      | $\approx$ 0033 3 digit three                                    |
|          | $\approx 0663$ ° Arabic-Indic digit three                       |
| 1        | RUMI DIGIT four   |
| -        | $\approx$ 0034 4 digit four                                     |
|          | $\approx 0664$ $\pounds$ Arabic-Indic digit four                |
| 4        | RUMI DIGIT FIVE   |
| <i>(</i> | $\approx 0035 5$ digit five                                     |
|          | $\approx$ 0605 5 digit five<br>≈ 0665 • Arabic-Indic digit five |
|          | RUMI DIGIT SIX  |
| 6        | $\approx$ 0036 6 digit six                                      |
|          | $\approx$ 0666 $\checkmark$ Arabic-Indic digit six              |
| 2        | RUMI DIGIT SEVEN  |
|          | $\approx 0037$ 7 digit seven                                    |
|          | $\approx$ 0667 $\vee$ Arabic-Indic digit seven                  |
| L        | Ŭ   |
| 7        | RUMI DIGIT EIGHT  |
|          | $\approx 0038 8 \text{ digit eight}$                            |
|          | $\approx 0668$ $\wedge$ Arabic-Indic digit eight                |
| ี่ย      | RUMI DIGIT NINE   |
|          | $\approx$ 0039 9 digit nine                                     |
|          | $\approx$ 0669<br>۹ Arabic-Indic digit nine                     |
|          | Table 8: RUMI ones digits                                       |
|          | Table 0. Ito mi onos ulguos                                     |

| ۲  | RUMI DIGIT TEN   |
|----|--|
| -  | $\bullet$ used as a symbol with a numeric value of 10  |
| W  | RUMI DIGIT TWENTY                                      |
|    | $\bullet$ used as a symbol with a numeric value of 20  |
| 2  | RUMI DIGIT THIRTY                                      |
|    | $\bullet$ used as a symbol with a numeric value of 30  |
| *  | RUMI DIGIT FORTY                                       |
|    | • used as a symbol with a numeric value of 40          |
| ~  | • used as a symbol with a numeric value of 40          |
| ינ | RUMI DIGIT FIFTY                                       |
| _  | $\bullet$ used as a symbol with a numeric value of 50  |
| ٤  | RUMI DIGIT SIXTY                                       |
|    | $\bullet$ used as a symbol with a numeric value of 60  |
| 0  | RUMI DIGIT SEVENTY                                     |
| -  | $\bullet$ used as a symbol with a numeric value of 70  |
| 6  | RUMI DIGIT EIGHTY                                      |
| -  | $\bullet$ used as a symbol with a numeric value of 80  |
| 1  |  |
| C  | RUMI DIGIT NINETY                                      |
| •  | • used as a symbol with a numeric value of 90          |
| e  | RUMI DIGIT HUNDRED                                     |
|    | $\bullet$ used as a symbol with a numeric value of 100 |
|    |  |

Table 9: RUMI tens digits

| ケ | RUMI DIGIT TWO HUNDRED                                 |
|---|--|
|   | $\bullet$ used as a symbol with a numeric value of 200 |
| ૯ | RUMI DIGIT TREE HUNDRED                                |
|   | • used as a symbol with a numeric value of 300         |
| × | RUMI DIGIT FOUR HUNDRED                                |
|   | • used as a symbol with a numeric value of 400         |
| 9 | RUMI DIGIT FIVE HUNDRED                                |
|   | • used as a symbol with a numeric value of 500         |
| 8 | RUMI DIGIT SIX HUNDRED                                 |
|   | • used as a symbol with a numeric value of 600         |
| 4 | RUMI DIGIT SEVEN HUNDRED                               |
|   | • used as a symbol with a numeric value of 700         |
| 7 | RUMI DIGIT EIGHT HUNDRED                               |
|   | • used as a symbol with a numeric value of 800         |
| 2 | RUMI DIGIT NINE HUNDRED                                |
|   | $\bullet$ used as a symbol with a numeric value of 900 |
|   |  |

Table 10: RUMI handreds digits



/r

بهم/

### RUMI FRACTION ONE HALF

- $\bullet$  used as an other symbol with a numeric value of 1/2
- $\approx$  00BD 1/2 vulgar fraction one half

### RUMI FRACTION ONE QUARTER

- $\bullet$  used as a symbol with a numeric value of 1/4
- $\approx$  00BC 1/4 vulgar fraction one quarter

### RUMI FRACTION ONE THIRD

- $\bullet$  used as a symbol with a numeric value of 1/3
- $\approx$  2153 1/3 vulgar fraction one third



#### RUMI FRACTION TWO THIRDS

- $\bullet$  used as an other symbol with a numeric value of 2/3
- $\approx$  2154 2/3 vulgar fraction two thirds

Table 11: RUMI special fractions

[2] ابن البا المراكضي، اقتضاب في العمل بالرومي، مخطوط بالخزانة الوطنية بالرباط تحت رقم ف 416 محموعة ص425 -432 [3] اهمد ابن العياشي سكوج، إرغاد المتعلم والناسي في صفة أشكال القلم الثاسي، طبعة فاس، 1316هـ (المكتبة الوطنية 17000989). [4] قاسم بن أهد السامرائي، الأرقام في المشرق عربية النجار وفي النرب الأورى سنسكريتية هندية الدئار، عالم الكتب، المحلد التاسع عشر، العدد الخامس والسادس مزدوجين عن الرقم العربي، 1998. [10] S. Bartina, Cifras coptas y cultura árabe, Studia Papyrologica 7 (1968), 199-210. [11] Georges S. Colin, De l'origine grecque des "chiffres de Fès" et de nos "chiffres arabes", Journal Asiatique 222 (1933), 193-215. http://laporti.club.fr/maghreb/Journalasiatique.doc http://phrontistery.info/nnsbib.html [12] Rosa Comes, Arabic, Rûmî, Coptic, or merely Greek Alphanumerical Notation? The case of a Mozarabic 10th Century Andalusî Manuscript. Subayl 3 (2002-2003), 157-185. http://chama.fltr.ucl.ac.be/chama2/newsletter 3.htm http://www.ub.es/arab/llibrevs/index3.htm [13] A. González Palencia, Los mozárabes de Toledo en los siglos XII y XIII. 4 vols., Madrid, 1926-1930. http://www.filosofia.org/ave/001/a042.htm http://www.architoledo.org/catedral/archivos/textoarchivo.htm [14] Youcef Guergour, Les différents systèmes de numérotation au Maghreb à l'époque ottomane: l'example des chiffres rûmî. E. Ihsanoglu, A. Diebbar et F. Günergun, eds. Burlington, Science, Technology and Industry in the Ottoman World. Proceedings of the XXth International Congress of History of Science, Liège, 20-26 July 1997, Vol. VI. Brepols. Turnhout, 2000, 67-74. http://www.math.buffalo.edu/mad/AMU/amu\_chma\_23a.html http://phrontistery.info/nnsbib.html www.math.buffalo.edu/mad/AMU/amuchmapdf/amuchma23.pdf [15] Ana Labarta y Carmen Barceló, Números y cifras en los documentos arábigo-hispanos. Córdoba, 1988. http://www.islamval-andalus.org/control/noticia.php?id=477 http://museodeamerica.mcu.es/pdf/anales13/capitulo14.pdf http://www.porticolibrerias.es/c/PS627ARA.pdf http://www.porticolibrerias.es/dept\_estudios\_arabes\_valencia.htm [16] G. Levi della Vida, Appunti e quesiti di storia letteraria araba: Numerali greci in documenti arabo-spagnoli, Rivista degli studi orientali 14 (1933), 249-283. http://web.uni-frankfurt.de/fb13/igaiw/publication/mathematic.html http://cura.free.fr/quing/04bezza.html http://web.uni-bamberg.de/unibib/melcom/Sagaria%20Rossi-1.html [17] J.A. Sánchez Pérez, Sobre las cifras rûmies, Al-Andalus 3 (1935), 97-125. http://www.islamval-andalus.org/control/noticia.php?id=477 [18] Abel REY, A propos de l'origine grecque des "chiffres de Fès" et de nos "chiffres arabes", Revue des Etudes Grecques. Tome 48, 1935, pp. 525-538. [19] Driss Lamrabet, Aperçu sur les systèmes de numération en usage au Maghreb du XVIIe siècle, Publications de la Faculté des Lettres et des Sciences Humaines, Rabat ; Si Colloques et Séminaires nº 104, 2003, pp. 23-37. [20] Adam Gacek, The Arabic Manuscript Tradition: A Glossary of Technical Terms and Bibliography, Brill Academic Pub Published, 2001 https://bookweb.kinokuniya.co.jp/guest/cgi-bin/booksea.cgi?ISBN=9004120610

Figure 1: rumi numeral system in [1] page 1

ille a X 7 425 هرا العراليب الع 24 i Ċ 15 8 ζw C (L Š Ø ۶ Ŵ 93 4 J)

Figure 2: rumi numeral system in [1] page 1

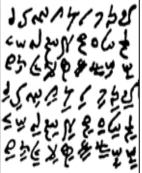
بسمالأه الرحمن الرحيم صلى الأمعلى سيدنا محمد وعلى أله وصحبه وسلم تسليما

[لاقضاب من العمل بالرومي في الحساب، تأليف الشيخ الفقيه الجليل الفاضل المشارك الأكمل المرحوم أي العاس أخمد بن عمد بن عثمان الأرذي، حرف بابن البناء العددي المراكشي، قدس الله روحه ورخمه بمه وفضله وطوله".

الحمد لله همدا لا انقطاع <sup>ع</sup> لعده <sup>\*</sup> ولا فحاية لحده والصلاة على محمد نبيه وعبده وعلى أله وسلم وضرفه كثيرا <sup>\*</sup>. وبعد، فهذا اقضاب من العمل بالرومي في الحساب على نحو ما وقع <sup>ت</sup>احتيار الرؤساء <sup>ف</sup> من العمال، وهن الله اسأل حسن التوفيق. باب في أ<sup>م</sup>ماء مراتب الأعداد وصفة الرضم بالرومي. اعلم أن المرتبة الأول هي الأحاد النسعة والثانية هي العشرات النسع والثالثة هي المؤن النسع والرابعة هي الألاف النسعة والخامسة هي عشرات

الألاف النسعة والسامنة هي ملثوا الألاف النسع وللسابعة هي آلاف الألاف النسعة وهكذا إلى غير فحاية. ولكل عدد من أعداد المراتب الثلاث الأول رشم يخصه أولها واحد وآخرها تسع مائة ورشوم الألاف وعشرائها ومائيها كرشوم الأحاد وعشرائها ومائيها والفرق بينهما بالتكرار وشكل التكرار خفظة تحت العدد وهذه صورة ذلك كله:

وكذلك آلاف الألاف وعشراقًا ومؤها ترجع إلى رغوم التي قبلها والفرق بينهما التكرار. لكل نوع ما يجب له منه " كذلك إلى غير أفاية. وأما رضوم الكسور فرغم العدد الذي يشتق منه الكسر<sup>11</sup> ويخط فوقه خط يسمى كرسيا ويكتب فوقه عدة الأجزاء التي تشتق منه وكذلك كسور الكسور وهي أمثلة منها رغم نصف **ك**و وثلثين **عُمَ** وثلاثة أرباع محمم وأربعة أخمل محم وخسة



أمدنس على وسنة أسباع مسر وسبعة أكمن سلم وتمانية أنساع <sup>21 علمي</sup> وتسعة أعشار على وقد اصطلح أصحاب العمل على أن يرتموا النصف هكذا في والربع هكذا عسر والثلث هكذا عسل والثلثين <sup>مد</sup> هكذا في ولا يستعملون الأجزاء التي فقاماتها أكثر من عشرة. وان وقع لهم شيء منها في العمل صرفوه على ما ستعرفه في باب الجمع بعد هذا. والكسور المستعملة عندهم نوعان مضافة ومختلفة فقًا المضافة فيقدم الكسر الذي مقامه أعظم ويكون الأقل عن بينه منتخفضا هه قليلا مثل خسة أكمان وثلاثة أكمان تمن وثلث تمن رئمها<sup>مد</sup> هكذا للكسر الذي مقامه أعظم ويكون الأقل عن بينه منتخفضا هه قليلا مثل خسة أكمان وثلاثة أكمان تمن وثلث تمن رئمها<sup>مد</sup> هكذا

المختلفة فبصنها تحت بعض مثل خمسة أكمان وسنة أسباع رنمها هكذا

اً مون ت الففرة بإ السلا الاباب: لما الشيع الأبط الأعناداغضو اللانا الشارك أبوالتباس أخذ بو حمد بو مقماة الأرتي رها الله وردني منا 1 يونه كمة الفاع" ويرح كمة القطاع" كما ورد بإ السلاة الابا

- ورد عما الناع : ورج عما الن
  - ا ۾ السخا الايا جا ۽ جد،
- " ﴿ السَّدَا قَابَةَ فَا : وَالْمُنَادَةَ وَالْمَنَادَ عَلَى مِيدَنَا عَمَدَ بِي وَمِيدَ، وَعَلَى أَنَا وَتُعرف كَقِرا
  - <sup>6</sup> () السخا قاباً رباط: مليا
- هُ وربد عَمَّةَ "ارُوسا" وبرح عَمَةَ "ارُوُسَلَ" عَمَا وردَقَ السَّحَةَ قَابَةَ وَقُو مَرْحُو"ا رُسَلًا"
  - " ﴿ السَّحَا فَايَاتِ : الْمُبْح
- » والسخة فابة ضاء: : وأنسابة في ألاف الآلاف المنعة ومرح سَلْها توبيه، ما حدور أشد والله بو
  - ° ورده عدة "حُمَّنَ" وبرح عدة "جُعْلَ" عنا وردع السَّاة الآبا

Figure 3: rumi numeral system in [1] page 1 printed

In the name of The God, the most Merciful, the most Compassionate The God prayed on Mohammed reigned and on his family and accompanied him and peace of delivery

The shortening from the work in the Rwmy in the calculation, formation of the participant virtuous of the magnificent jurist generous associated complete Abou AlEbas Ahmed Ben Mohammed Ben Othman al'azdy. He was introduced as mason's son numerical Almraakshy. The God sanctified went him and his uterus in his blessing and his casual dress and lengthens him.

The God praised neither his break-off for acne nor his end for border and the prayer on Mohammed is discerning and worshipped him and on his family and his peace and honor a lot. After, so this shortening from the work in the Rwmy in the account on towards what choice of the heads from the laborers fell, and from The God asks the good success.

Chapter in names ranks of the numbers and prescription glyphs in Rwmy.

Knows that the rank first is the ones nine and the second is the tens nine and the third is the hundreds nine and the fourth is the thousands nine and the fifth is the tens of thousands nine and the sixth is the hundreds of thousands nine and the seventh is the thousands thousands nine and so on until the infinite one.

For each number of the first three numbers ranks a sign witch distinguishes it, the first is one

and the last is nine hundred. The draws of thousands and its tens and its hundreds are the same as the draws of ones and tens and hundreds and the difference between them is the repetition. The form of the repetition is a bar under the number and these images for all them:

Likewise thousands of thousands and its tens and its hundreds return to glyphs before them and the difference between them the repetition. For each kind what be necessary for him likewise so on until the infinite one.

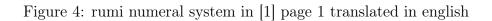
When the fractions are to be drawn, we write the base number which derives the fraction and draws above him a line called chair and writes above him the parts which

derives from him, and as the fraction's fraction. Here are examples of draw: one half  $\checkmark$ , two thirds  $\checkmark$ , tree quarters  $\checkmark$ , four fifths  $\checkmark$ , five sixths  $\checkmark$ , six sevenths  $\checkmark$ , seven eighths  $\checkmark$ , eight ninths  $\checkmark$ , nine tenths  $\checkmark$ . And leads the man working in make up provided that draw the one half in this way  $\checkmark$ , and one quarter in this way  $\checkmark$ and one third in this way  $\checkmark$ , and the two third in this way  $\checkmark$ . They don't use fractions

which there based are more than ten. If they arrive to have some of them they transform them to what you will know in the addition chapter after this one.

The fractions they used stubborn two kinds added and different. So for added fraction, the fraction whose based is great advances and the little about right and little low from him,

example five eighth and three eighth and third eighth in this way **FFF**. As for different fraction, parts are under others parts example five eighths and six sevenths in this way



ey.

Figure 5: Integer rumi symbols in [1]



Figure 6: Fraction rumi symbols in [1]

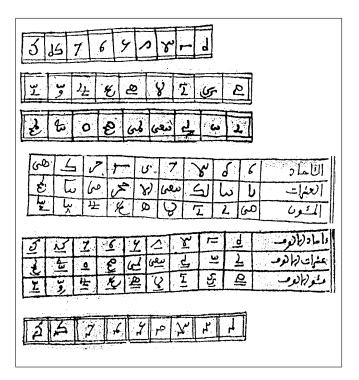


Figure 7: Examples in [3]

الجؤير هوانهايته مااتة < 1 R < e ωð لما ωý 47 ىھ w, L, ۲ų 4 21 N でへ Np キシ ÷, s 1 544 25 SV S 6 ፟፟ቚ م ہ لر. • ^ Ē م •2 t., ٩/ 6 205 Ê7 51-21 21 6~ RA **ଜ**୍ୟ ď 25

Figure 8: Examples from [4]

parum dirutus, necesse fuit abscidere folia quæ inutilia evaserant; hæc suspitio confirmatur ex facto, quod folia octogesimo posteriora morsus vermium majores habent præcipue circa folium centesimum tertium; et notandum est hos morsus jam in codice existentes esse cum collatio, saltem secunda fiebat, nam quidam restaurati fuere, ut videtur ab antiquo et verba a vermibus plene corrosa in margine explicantur: charta antiquioris codicis major erat, nam a folio trigesimo nono usque ad centesimum quintum vestigia antiquioris foliorum numerationis existunt, nam numeratio ex magna parte abscisa fuit: in foliis secundæ partis nihil hujuscemodi numerationis distinguitur, et breves notæ marginales, præcipue verbum <u>uit</u> pluries in margine primæ partis scriptum fere evanuit.

x

SPECIMEN NUMERATIONIS FOLIORUN IN FODICE ESCURIALENSI.

Folierum numeratio. Codex habet foliorum numerationem modernam, factam postquam codex a librario numerationis arabicæ imperito compactus est; a folio enim secundo transilire necesse fuit ad folium decimum septimum et a folio vigesimo secundo iterum ad tertium recedere.

Ex foliorum numeratione antiqua codex centum sexaginta

Figure 9: Examples from [4]

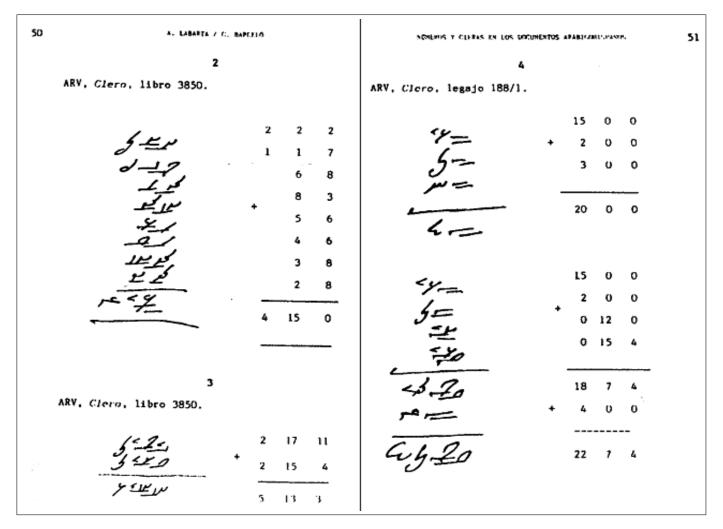


Figure 10: Examples in [15] pages 50-51 from [4]

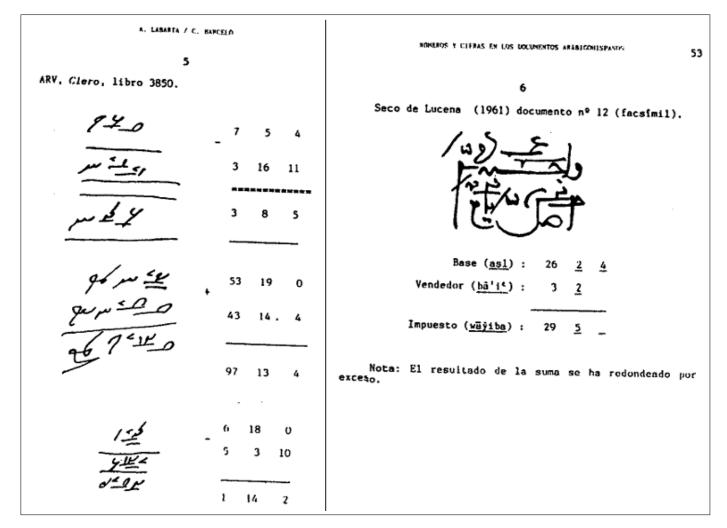


Figure 11: Examples in [15] pages 52-53 from [4]