# Proposal to Encode Diwani Siyaq Numbers in Unicode 

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## 1 Introduction

This is a proposal to encode Diwani Siyaq Numbers in the Unicode standard. It draws upon information originally presented in the following documents, which referred to the proposed block using the designation 'Diwani Siyaq Numbers', and it supersedes those documents:

- L2/07-414 "Proposal to Encode Siyaq Numerals"
- L2/09-140 "Diwani Numerals: Towards a Model for Encoding Numerals of the Siyaq Systems"
- L2/11-269 "Preliminary Proposal to Encode Diwani Siyaq Numbers in the UCS"

The major changes from earlier versions are:

- Inclusion of primary sources with transliterations of numbers
- New analysis of glyphic variants and alternate forms
- Addition of alternate forms for various units
- Enhancements to the glyphs of several numbers

Proposals to encode characters of the other three Siyaq systems have been submitted. These following documents contain information on the typology of the numbers and the notation system, and explain the necessity for encoding independent blocks for the four Siyaq systems:

- L2/15-072R2 "Proposal to Encode Ottoman Siyaq Numbers in Unicode"
- L2/15-121R2 "Proposal to Encode Indic Siyaq Numbers in Unicode"
- L2/15-122 "Proposal to Encode Persian Siyaq Numbers in Unicode"


## 2 Script Details

Block name The name 'Diwani Siyaq Numbers' is assigned to the block. This name reflects the types of documents in which these numbers were used.

Character repertoire The proposed repertoire contains 57 characters. it includes alternate forms of numbers that have distinctive shapes. All characters are attested in the available sources, from which several specimens are included here as figures.

Representative glyphs Diwani Siyaq Numbers are attested in sources from the early 10th through 14th centuries. Their forms are quite regular across the available sources. The representative glyphs used here were produced by the proposal author. They are based upon the printed forms used in Exposé des signes de numération usités chez les peuples orientaux anciens et modernes by Antoine Paulin Pihan (Paris: L'imprimerie impériale, 1860), specimens of which are shown in figures 12 and 13 . These glyphs have been modified as necessary in order to reflect actual usage in the available sources and new glyphs have been created for numbers not illustrated by Pihan.

Structure Diwani Siyaq Numbers represent units of a decimal positional system. The notation system is additive, that is, the value of a number is the sum of the values of the numerals that constitute it. There is no character for zero; it is inherently represented in the distinct numerals for the various decimal orders. There are numbers for the primary units, tens, hundreds, thousands, and ten thousands. Numbers of higher orders are represented using sequences of these characters.

Directionality Diwani Siyaq Numbers are written right-to-left in the regular Arabic manner.
Ordering The ordering of Diwani Siyaq Numbers reflects the method of expressing numbers in Arabic. The largest number occurs first and smaller units follow in sequential order. Compound numbers involving the tens and primary units are written transposed, such that the latter is placed before the former.

## 3 Characters Proposed

### 3.1 Primary numbers

The following 9 characters are used for representing primary numbers:

| $\boldsymbol{1}$ | DIWANI SIYAQ NUMBER ONE |
| :--- | :--- |
| $\boldsymbol{y}$ | DIWANI SIYAQ NUMBER TWO |
| $\boldsymbol{u}$ | DIWANI SIYAQ NUMBER THREE |
| DIWANI SIYAQ NUMBER FOUR |  |
| L DIWANI SIYAQ NUMBER FIVE |  |
| L DIWANI SIYAQ NUMBER SIX |  |
| L DIWANI SIYAQ NUMBER EIGHT |  |
| L DIWANI SIYAQ NUMBER NINE |  |

### 3.2 Alternate forms of the primary numbers

The following 8 characters are included in the repertoire:
DIWANI SIYAQ NUMBER ALTERNATE THREE

These alternate forms are not glyphic variants, but are used in place of the regular forms in compounds involving the tens and ten thousands (see section 3.10):

These forms are produced by removing the left ascending terminal of the regular form. The exception is alternate three, which is a secondary abbreviation of Arabic talāta "three". A comparison of the regular and alternate forms of the primary numbers are shown below:

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Regular | 1 | ل | $\bigcirc$ | لJ | حا | ᄂ | Lus | 4 | Uع |
| Alternate | - | - | لا | لس | 7 | $\checkmark$ | $\mu$ | $r$ | لع |

### 3.3 Tens

The following 9 characters are used for representing the tens:

| عا | DIWANI SIYAQ NUMBER TEN |
| :---: | :---: |
| es | DIWANI SIYAQ NUMBER TWENTY |
| ひ | DIWANI SIYAQ NUMBER THIRTY |
| 1 | diwani siyaq number forty |
| 1 | DIWANI SIYAQ NUMBER FIFTY |
|  | DIWANI SIYAQ NUMBER SIXTY |
| 14 | DIWANI SIYAQ NUMBER SEVENTY |
|  | DIWANI SIYAQ NUMBER EIGHTY |
| 1 |  |

### 3.4 Alternate form of ten

The following character is included in the repertoire:

The $\boldsymbol{q}$ alternate ten is shown in figure 13. It is included in the proposed repertoire because of its distinctive form.

### 3.5 Hundreds

The following 9 characters are used for representing the hundreds:


### 3.6 Alternate forms of the hundreds

The following characters are included in the repertoire:


The alernate three hundred is shown as a variant of three hundred by Pihan in figure 13. This form is not shown in the available primary sources.

The $\mathbf{l}$ alternate four hundred occurs as a variant of $ل$ four hundred in Abbasid and Ilkhanate sources. It is shown in figure 5 (ie. 492,434, in figure 9 (ie. 176,400). 10 (ie. 2,412,900).

The alternate seven hundred is occurs as a variant of $\boldsymbol{L}_{\boldsymbol{\sigma}}$ SEven hundred in the Ilkhanate source in figure 8 (ie. in 338,700 ).

These are proposed for encoding on account of their distinctive shapes.

### 3.7 Thousands

The following 9 characters are used for representing the thousands:

> DIWANI SIYAQ NUMBER ONE THOUSAND

| العى | diwan sivaq number tue |
| :---: | :---: |
| טת | diwani sivaq number three thousand |
| 1-1 | diwan sival number four thousand |
| حك | diwani sivaq number five thousand |
| cr | diwani sixaq number six thousand |
| cer | diwan siyaq number seven thousand |
| cror | diwani siyaq number eight thou |
| תعف | DIWANI SIYAQ NUMBER NINE |

Figures 11 and 13 show الس as a variant form of thousand. It is not proposed for encoding. It is considered a glyphic variant because of its close resemblance to the representative form.

### 3.8 Ten Thousands

The following 9 characters are used for representing the ten thousands:
DIWANI SIYAQ NUMBER TEN THOUSAND

### 3.9 Alternate form of twenty thousand

The following character is included in the repertoire:

## elq DIWANI SIYAQ NUMBER ALTERNATE TWENTY HUNDRED

Figure 7 shows the use of the forms luy and $\boldsymbol{C}$ \& for expressing 20,000. The first is the representative form for TWENTY thousand. The second is an alternate whose shape is based upon that for the thousands, similar to عתع TEN THOUSAND. Another contrastive usage occurs again in figure 10 (ie. compare 22,600 and 25,200 ). This form is proposed for encoding on account of its distinctive shape and concurrent usage with the the regular elq.

### 3.10 Orthography

The proposed method for representing Diwani Siyaq Numbers in encoded text is described below. The examples contain three columns: the left is the numeric value; the center is the Diwani Siyaq representation in the regular right to left orientation; the right is the sequence of proposed Unicode characters that would be used for producing the numerical notation in encoded text. The order of the characters in the Unicode sequence (right column) is left to right and indicates the order of input for the characters, ie. the left-most character is the first to be input.


Compound numbers of primary units Compound numbers involving the primary units and the tens, ten thousands, and hundred thousands units are written transposed with the primary unit placed before the larger number. Compounds involving 3-9 are written using the alternate forms of the primary numbers. Below are representations of 11-19. Compounds from 21-99 are written according to the same pattern.

| 11 | اعا | < ONE, ع TEN> |
| :---: | :---: | :---: |
| 12 | لاعا |  |
| 13 | للاعا | < لل alternate three, ع㇒ ten> |
| 14 | للرعا | < لسر alternate four, عا TEN> |
| 15 | حعا | < $\boldsymbol{\sim}$ alternate five, عا TEn> |
| 16 | ع | $<$ alternate six, عا TEn> |
| 17 | بر عا | < $\mu$ alternate SEven, عl LEN > |
| 18 | $L^{\text {r }}$ | $<\boldsymbol{\sim}$ alternate eight, عl TEn> |
| 19 | كععا | < عת alternate nine, Ten> |

Hundred thousands The hundred thousands are represented using the appropriate number for the hundreds followed by الع one thousand. This method is attested in Abbasid and Ilkhanate sources.

| 100,000 | 6الب | < ${ }_{\text {c one }}$ OUNDRED, الa One Thousand> |
| :---: | :---: | :---: |
| 200,000 | ¢ת اله |  |
| 300,000 | بلا | < لا Three hundred, الع one thousand> |
| 400,000 | لمعاله |  |
| 500,000 | حعاله | < حع Five hundred, الع one thousand> |
| 600,000 | كe | < الع six hundred, one thousand> |
| 700,000 | 1-4 | < $\mathbf{l}$ SEVEN HUNDRED, الف one thousand> |
| 800,000 | كالع |  |
| 900,000 | كعالع |  |

Another method shown by Pihan (1860: 211) is to use the primary unit followed by the compound $\boldsymbol{6}$ one hundred, الع one thousand> (see figure 12). According to Pihan the alternate forms of the primary units are used for THREE .. NINE when writing the order.

| 100,000 | 6الص |  |
| :---: | :---: | :---: |
| 200,000 | لا |  |
| 300,000 | للا | < ¢ alternate three, $\boldsymbol{6}$ one hundred, الص one thousand> |
| 400,000 | للر | < $\boldsymbol{\nu}_{\text {alternate four, } \boldsymbol{b} \text { one hundred, }{ }^{\text {a }} \text { One thousand> }}$ |
| 500,000 | ح ${ }^{1 / 2}$ | < $\boldsymbol{\sim}$ alternate five, $\boldsymbol{b}$ one hundred, الa one thousand> |
| 600,000 | ك | < alternate six, b one hundred, الa one thousand> |
| 700,000 | - | < $\mu$ alternate seven, $\boldsymbol{b}$ one hundred, الa one thousand> |
| 800,000 | هr | < $\boldsymbol{\downarrow}$ alternate eight, $\boldsymbol{b}$ one hundred, الع one thousand> |
| 900,000 | لع | - alternate nine, 6 One hundred, الص one thousand> |

This method is curious. It is not attested in the available sources and the provenance of the information given by Pihan is unknown.

Millions The millions are expressed in Arabic using repetition of 'one thousand': الف الف alf alf "thousand (and) thousand' means 'one million'. The Diwani representation follows this pattern:

| 1,000,000 | الع الع | الع> one thousand, الف one thousand> |
| :---: | :---: | :---: |
| 2,000,000 | العى | > الع one thousand> |
| 3,000,000 | سתع | < Three thousand, الف one thousand> |
| 4,000,000 | لمعكالع | / لـعكع four thousand, الع one thousand> |
| 5,000,000 | حكع | حكع FIVE thousand, الع one thousand> |
| 6,000,000 | 込 | < |
| 7,000,000 | بعת اله | < الع Seven thousand, one thousand> |
| 8,000,000 | ¢ | < ${ }_{\text {c }}^{\text {elght thousand, one thousand> }}$ |
| 9,000,000 | لعתع | < لعكع NINE THousand, الس One thousand> |

Larger orders The available sources for Diwani numbers do not contain values that exceed the millions.

### 3.11 Character Properties

In the format of UnicodeData.txt:
1ECC1;DIWANI SIYAQ NUMBER ONE;NO;0;AL;;;;1;N;;;;
1ECC2;DIWANI SIYAQ NUMBER TWO;No;0;AL; ; ; $2 ; \mathrm{N} ; ; ; ;$
1ECC3;DIWANI SIYAQ NUMBER THREE;No;0;AL; ; ; 3; $\mathrm{N} ; ; ; ;$
1ECC4;DIWANI SIYAQ NUMBER FOUR;No;0;AL; ; ; $4 ; N ; ; ; ;$
1ECC5;DIWANI SIYAQ NUMBER FIVE;No;0;AL; ; ; 5; $;$; ; ; ;
1ECC6;DIWANI SIYAQ NUMBER SIX;No;0;AL;;;;6;N;;;;
1ECC7;DIWANI SIYAQ NUMBER SEVEN;No;0;AL; ; ; 7; $\mathrm{N} ; ; ; ;$
1ECC8;DIWANI SIYAQ NUMBER EIGHT;No;0;AL; ; ; ; ; N; ; ; ;
1ECC9;DIWANI SIYAQ NUMBER NINE;No;0;AL;;;9;N;;;;
1ECCA;DIWANI SIYAQ NUMBER TEN;No;0;AL;;;i10;N;;;;
1ECCB; DIWANI SIYAQ NUMBER TWENTY;No;0;AL; ; ; 20;N; ; ; ;
1ECCC;DIWANI SIYAQ NUMBER THIRTY;No;0;AL; ; ; 30 ;N; ; ; ;
1ECCD;DIWANI SIYAQ NUMBER FORTY;NO;0;AL; ; ; 40 ; $\mathrm{N} ; ; ; ;$
1ECCE;DIWANI SIYAQ NUMBER FIFTY;No;0;AL; ;; 50;N; ; ; ;
1ECCF; DIWANI SIYAQ NUMBER SIXTY;No;0;AL;;;;60;N;;;;
1ECDO;DIWANI SIYAQ NUMBER SEVENTY;NO;0;AL; ; ; 70; $;$; ; ; ;
1ECD1;DIWANI SIYAQ NUMBER EIGHTY;No;0;AL; ; ; 80;N; ; ; ;
1ECD2;DIWANI SIYAQ NUMBER NINETY;No;0;AL; ; ; $90 ; \mathrm{N} ; ; ; ;$
1ECD3;DIWANI SIYAQ NUMBER ONE HUNDRED;No;0;AL; ; ; 100;N; ; ; ;
1ECD4;DIWANI SIYAQ NUMBER TWO HUNDRED;NO;0;AL; ; ; 200;N; ; ; ;
1ECD5;DIWANI SIYAQ NUMBER THREE HUNDRED;No;0;AL; ; ; 300; $\mathrm{N} ;$; ; ; ;
1ECD6; DIWANI SIYAQ NUMBER FOUR HUNDRED;NO;0;AL; ; ; 400 ; $;$; ; ; ; ;
1ECD7;DIWANI SIYAQ NUMBER FIVE HUNDRED;NO;0;AL;;;;500;N;;;;
1ECD8;DIWANI SIYAQ NUMBER SIX HUNDRED;NO;0;AL; ; ; $600 ; \mathrm{N} ; ; ; ;$
1ECD9;DIWANI SIYAQ NUMBER SEVEN HUNDRED;NO;0;AL; ; ; 700; $\mathrm{N} ; \boldsymbol{;} ; ;$
1ECDA;DIWANI SIYAQ NUMBER EIGHT HUNDRED;NO;0;AL; ; ; 800;N; ; ; ;
1ECDB;DIWANI SIYAQ NUMBER NINE HUNDRED;No;0;AL; ; ; 900 ;N; ; ; ;
1ECDC;DIWANI SIYAQ NUMBER ONE THOUSAND;No;0;AL; ; ; $1000 ; \mathrm{N} ; ; ; ;$
1ECDD; DIWANI SIYAQ NUMBER TWO THOUSAND;No;0;AL; ; ; 2000;N; ; ; ;
1ECDE;DIWANI SIYAQ NUMBER THREE THOUSAND;NO;0;AL; ; ; 3000;N; ; ; ;
1ECDF; DIWANI SIYAQ NUMBER FOUR THOUSAND;NO;0;AL;;;;4000;N;;;;
1ECEO;DIWANI SIYAQ NUMBER FIVE THOUSAND;NO;0;AL; ; ; ; 5000; $\mathrm{N} ; ; ; ;$
1ECE1;DIWANI SIYAQ NUMBER SIX THOUSAND;NO;0;AL; ; ; 6000 ; $;$; ; ; ;
1ECE2;DIWANI SIYAQ NUMBER SEVEN THOUSAND;No;0;AL; ; ; 7000;N; ; ; ; ;
1ECE3;DIWANI SIYAQ NUMBER EIGHT THOUSAND;No;0;AL; ; ; 8000 ; $;$; ; ; ;
1ECE4;DIWANI SIYAQ NUMBER NINE THOUSAND;NO;0;AL; ; ; ; 9000; $\mathrm{N} ; ; ; ;$
1ECE5; DIWANI SIYAQ NUMBER TEN THOUSAND;NO;0;AL; ; ; $10000 ; \mathrm{N} ; ; ; ;$
1ECE6;DIWANI SIYAQ NUMBER TWENTY THOUSAND;NO;0;AL;;;;20000;N;;;;;
1ECE7;DIWANI SIYAQ NUMBER THIRTY THOUSAND;NO;0;AL; ; ; 30000;N; ; ; ;
1ECE8;DIWANI SIYAQ NUMBER FORTY THOUSAND;NO;0;AL; ; ; 40000;N; ; ; ;
1ECE9;DIWANI SIYAQ NUMBER FIFTY THOUSAND;NO;0;AL; ; ; $50000 ; N ; ; ; ;$
1ECEA;DIWANI SIYAQ NUMBER SIXTY THOUSAND;NO;0;AL; ; ; 60000;N; ; ; ;
1ECEB;DIWANI SIYAQ NUMBER SEVENTY THOUSAND;No;0;AL; ; ; 70000;N;;;;
1ECEC;DIWANI SIYAQ NUMBER EIGHTY THOUSAND;No;0;AL; ; ; 80000;N; ; ; ;
1ECED;DIWANI SIYAQ NUMBER NINETY THOUSAND;NO;0;AL; ; ; 90000 ; $;$; ; ; ;
1EDEE;DIWANI SIYAQ NUMBER ALTERNATE THREE;No;0;AL; ; ; 3;N; ; ; ;
1ECEF;DIWANI SIYAQ NUMBER ALTERNATE FOUR;NO;0;AL;;;;4;N;;;;
1ECFO;DIWANI SIYAQ NUMBER ALTERNATE FIVE;NO;0;AL; ; ; 5 ; N; ; ; ; ;
1ECF1;DIWANI SIYAQ NUMBER ALTERNATE SIX;No;0;AL;;;;6;N;;;;
1ECF2;DIWANI SIYAQ NUMBER ALTERNATE SEVEN;No;0;AL; ; ; 7; $;$; ; ; ;
1ECF3;DIWANI SIYAQ NUMBER ALTERNATE EIGHT;No;0;AL; ; ; $8 ; \mathrm{N} ; ; ; ;$
1ECF4;DIWANI SIYAQ NUMBER ALTERNATE NINE;NO;0;AL; ; ; 9; $\mathrm{N} ; ; ; ;$
1ECF5; DIWANI SIYAQ NUMBER ALTERNATE TEN;No;0;AL; ; ; $10 ; \mathrm{N} ; ; ; ;$
1ECF6; DIWANI SIYAQ NUMBER ALTERNATE THREE HUNDRED;NO;0;AL;;;;300;N;;;;

```
1ECF7;DIWANI SIYAQ NUMBER ALTERNATE FOUR HUNDRED;NO;0;AL;;;;400;N;;;;;
1ECF8;DIWANI SIYAQ NUMBER ALTERNATE SEVEN HUNDRED;NO;0;AL;;;;700;N;;;;;
1ECF9;DIWANI SIYAQ NUMBER ALTERNATE TWENTY THOUSAND;NO;0;AL;;;;20000;N;;;;;
```

Linebreaking In the format of LineBreak.txt:

```
1ECC1..1ECF9;AL # No [57] DIWANI SIYAQ NUMBER ONE ..
    DIWANI SIYAQ NUMBER ALTERNATE TWENTY THOUSAND
```


### 3.12 Confusion Data

Given below are Arabic sequences that may mimic the forms of Diwani Siyaq Numbers:

| Diwani Siyaq Numbers | Arabic |
| :---: | :---: |
| ONE | ; ALEF |
| TWO | ; LAM, ALEF |
| THREE | ; SEEN, YEH BARREE |
| FOUR | ; LAM, DOTLESS BEH, AIN, ALEF |
| FIVE | ; HAH, ALEF |
| SIX | ; SEEN, ALEF |
| SEVEN | ; HEH GOAL, AIN, ALEF |
| EIGHT | ; HEH GOAL, ALEF |
| NINE | ; DOTLESS BEH, AIN, ALEF |
| TEN | ; AIN, ALEF |
| TWENTY | ; HAMZA, DOTLESS BEH |
| THIRTY | ; DOTLESS BEH, LAM, MEEM, ALEF |
| FORTY | ; LAM, DOTLESS BEH, AIN, ALEF |
| FIFTY | ; HAH, ALEF |
| SIXTY | ; TATWEEL, ALEF |
| SEVENTY | ; HEH GOAL, AIN, ALEF |
| EIGHTY | ; DOTLESS BEH, ALEF |
| NINETY | ; DOTLESS BEH, AIN, ALEF |
| ONE HUNDRED | ; MEEM, ALEF |
| TWO HUNDRED | ; MEEM, ALEF, LAM, HEH GOAL |
| THREE HUNDRED | ; SEEN, MEEM, ALEF |
| FOUR HUNDRED | ; ALEF, AIN, MEEM, ALEF |
| FIVE HUNDRED | ; HAH, MEEM, ALEF |
| SIX HUNDRED | ; SEEN, TATWEEL, MEEM, ALEF |
| SEVEN HUNDRED | ; LAM, MEEM, ALEF |
| EIGHT HUNDRED | ; LAM, MEEM, ALEF |
| NINE HUNDRED | ; LAAM, AIN, MEEM, ALEF |
| ONE THOUSAND | ; ALEF, LAM, FEH |
| TWO THOUSAND | ; ALEF, AIN, FEH, YEH |
| THREE THOUSAND | ; SEEN, ALEF, LAM, FEH |
| FOUR THOUSAND | ; LAM, DOTLESS BEH, AIN, ALEF, LAM, FEH |
| FIVE THOUSAND | ; HAH, ALEF, LAM, FEH |
| SIX THOUSAND | ; SEEN, ALEF, LAM, FEH |
| SEVEN THOUSAND | ; DOTLESS BEH, AIN, ALEF, LAM, FEH |
| EIGHT THOUSAND | ; HEH GOAL, ALEF, LAM, FEH |
| NINE THOUSAND | ; LAM, AIN, ALEF, LAH, FEH |
| TEN THOUSAND | ; AIN, ALEF, LAM, FEH |
| TWENTY THOUSAND | ; AIN, DOTLESS BEH, LAM, ALEF |
| THIRTY THOUSAND | ; DOTLESS BEH, DOTLESS BEH, LAM, ALEF |
| FORTY THOUSAND | ; LAM, LAM, AIN, LAM, ALEF |
| FIFTY THOUSAND | ; HAH, LAM, ALEF |
| SIXTY THOUSAND | ; SEEN, LAM, ALEF |
| SEVENTY THOUSAND | ; HEH GOAL, AIN, LAM, ALEF |
| EIGHTY THOUSAND | ; HEH GOAL, LAM, ALEF |

```
NINETY THOUSAND ; LAM, AIN, LAM, ALEF
ALTERNATE THREE ; LAM, LAM, ALEF
ALTERNATE FOUR ; LAM, DOTLESS BEH, medial AIN
ALTERNATE FIVE ; initial HAH
ALTERNATE SIX ; initial SEEN
ALTERNATE SEVEN ; DOTLESS BEH, medial AIN
ALTERNATE EIGHT ; medial HEH GOAL
ALTERNATE NINE ; LAM, medial AIN
ALTERNATE TEN ; HAMZA
ALTERNATE THREE HUNDRED ; SEEN, HEH DOACHASHMEE, MEEM, ALEF
ALTERNATE FOUR HUNDRED ; ALIF, SEEN, MEEM, ALEF
ALTERNATE SEVEN HUNDRED ; SEEN, MEEM, ALEF
ALTERNATE TWENTY THOUSAND ; AIN, SEEN, ALEF, LAM, FEH
```


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|  | 1ECC | 1ECD | 1ECE | 1ECF |
| :---: | :---: | :---: | :---: | :---: |
| 0 |  |  | حك <br> 1ECE0 | $\underset{\text { 1ECF0 }}{7}$ |
| 1 | $\underset{1 \mathrm{ECC} 1}{ }$ | $\underbrace{1}_{1 E C D 1}$ | cl <br> 1ECE1 | $\underbrace{}_{1 E C F 1}$ |
| 2 | ע <br> 1ECC2 | كع1 <br> 1ECD2 | תعתع <br> 1ECE2 | $\boldsymbol{\mu}_{1 E C F 2}$ |
| 3 | $\underset{1 \mathrm{ECC} 3}{\boldsymbol{u}}$ | $\underset{1 E C D 3}{6}$ | cr 1ECE3 | $\underset{1 E C F 3}{\boldsymbol{r}}$ |
| 4 | لـ <br> 1ECC4 | ת <br> 1ECD4 | سعתع <br> 1ECE4 | $\underset{\text { 1ECF4 }}{ }$ |
| 5 | L <br> 1ECC5 | لمل <br> 1ECD5 | عתع <br> 1ECE5 | $\underset{\text { 1ECF5 }}{9}$ |
| 6 | 1ECC6 | لم8ا <br> 1ECD6 | Wy <br> 1ECE6 | Leg <br> 1ECF6 |
| 7 | L <br> 1ECC7 | la <br> 1ECD7 | سلا <br> 1ECE7 | اتا <br> 1ECF7 |
| 8 | ${\underset{1 E C C B}{L}}^{2}$ 1ECC8 | 16 <br> 1ECD8 | لسعلا <br> 1ECE8 | $L_{6}^{6}$ |
| 9 | ع <br> 1ECC9 | 18 <br> 1ECD9 | حلا <br> 1ECE9 | cers |
| A | ع <br> 1ECCA | b <br> 1ECDA | $\underbrace{}_{1 \in C E A}$ |  |
| B | bg <br> 1ЕССВ | كع <br> 1ECDB | Hen <br> 1ECEB |  |
| C | て <br> 1ECCC | الع <br> 1ECDC |  <br> 1ECEC |  |
| D | 1 <br> 1ECCD | العى |  |  |
| E | ح <br> 1ECCE | سתc 1ECDE | 3 <br> 1ECEE |  |
| F | $\sim$ | لـعـع 1ECDF | لـع |  |


|  | $x 1$ | $x 10$ | $x 100$ | $x 1,000$ | $x 10,000$ | $x 100,000$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | ع | 6 | الع | عתع | 6الع |
| 2 | لا | 4 | $\Omega$ | العى | WY | 6ه الع |
| 3 | $\sim$ | $\tau$ | 6 | سתع | سلا | كا |
| 4 | لما | 1 | لس8ا | لععف | لععلا | لسعالع |
| 5 | L | 2 | lea | حكع | リ | حعالع |
| 6 | $\checkmark$ | 2 | 6 | سl | 4 | كعالع |
| 7 | 14 | 14 | 18 | תعת | 1814 | ب8ا |
| 8 | 4 | 2 | b | cror | لـ | بالe |
| 9 | عL | ع1 | be | لعك | ععلا | كعِ |

Table 1: Diwani forms of the Siyaq numbers for six decimal orders.


Figure 1: Folio of an Abbasid financial document from 918-919 CE (from Kremer 1887: fig. 1).


Figure 2: Folio of an Abbasid financial document from 918-919 CE (from Kremer 1887: fig. 2a).


Figure 3: Folio of an Abbasid financial document from 918-919 CE (from Kremer 1887: fig. 2b).


4,746,492

| 40,460 | 80,750 | 290,773 |
| ---: | ---: | ---: |
| 102,062 | 230,647 | $1,080,000$ |
| 133,097 | $1,460,000$ | 113,057 |
| 352,570 | 115,114 | 315,300 |
|  |  |  |
| 5,397 | 52,985 | 15,765 |
| 65,332 |  |  |
|  |  | 14,501 |
| 56,750 | 5,478 |  |
|  |  |  |
| 82,422 | 82,422 | 34,120 |

Figure 4: Folio of an Abbasid financial document from 918-919 CE (from Kremer 1887: fig. 3a).


Figure 5: Folio of an Abbasid financial document from 918-919 ce (from Kremer 1887: fig. 3b).


Figure 6: Part of a financial document from the Ilkhanate period dated to 1340 ce (from Elitaş et al 2008: 125).


Figure 7: Part of a financial document from the Ilkhanate period dated to 1340 CE (from Elitaş et al 2008: 126).


Figure 8: Part of a financial document from the Ilkhanate period dated to 1340 CE (from Elitaş et al 2008: 127).


Figure 9: Part of a financial document from the Ilkhanate period dated to 1340 CE (from Elitaş et al 2008: 128).


Figure 10: Part of a financial document from the Ilkhanate period dated to 1340 CE (from Elitaş et al 2008: 129, 130).

LES CHIFFRES «DÎVÂNî» CHEZ LES ARABES (i)

| chiffres | valeur | cmiffres | valeur | chiffres | valeur |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | I | 985 | 19 | rallou | 1,000 |
| 1 | 2 | 25 | 20 | cell | 2,000 |
| $\mathcal{C}$ ou lll | 3 | 1 | 30 | cat | 3,000 |
| dad | 4 | Led | 40 | colld | 4,000 |
| La | 5 | 1 | 50 | ¢ | 5,000 |
|  | 6 | 2 | 60 | ル | 6,000 |
|  | 7 | 12 | 70 | coll | 7,000 |
|  | 8 | 1 | 80 | 0 | 8,000 |
| L | 9 | Led | $9^{\circ}$ | كـ6 | 9,000 |
| L | 10 | 6 | 100 | cla | 10,000 |
| 91 | I I | $\int$ | 200 | $1_{y} 8$ | 20,000 |
| sy | 12 | ou 16 | 300 | 1-s | 30,000 |
| Sc | I 3 | 18 | 400 | glan | 40,000 |
| sed | 14 | Las | 500 | Ha | 50,000 |
| 58 | I 5 | 10 | 600 | 11 | 60,000 |
| $y$ | 16 | 124 | 700 | IL | 70,000 |
| 924 | 17 | J | 800 | And | 80,000 |
| G-r | 18 | Lel | 900 | Yay | 90,000 |

(t) D’après un manuscrit du Vocabulaire arabe-persan de Zamakhcharì (Bibliothéque Nationale, ancien fonds arabe no 1256 ), reproduits dans la Grammaire arabe de Silyestre de Sacy et dans l'ouvrage de A.-P. Pihan.

Figure 11: Hand-written chart of "the diwani numbers of the Arabs" (from Kazem-Zadeh 1915: Plate VII). The variant form of 300 is missing in the original.

| unitis. |  | DİANESS. |  | cemtanss. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | ع | 10 | 6 | 100 |
| لا | 2 | as | ${ }^{20}$ | $\bigcirc$ | 200 |
| O-1 | 3 | て | 30 | كل大 | 300 |
| لr | 4 | 1 | 40 | ل-1 | 400 |
| ح | 5 | 1 | 50 | ¢ | 500 |
| $\checkmark$ | 6 | U | 60 | le | 600 |
| 4 | 7 | 1 | 70 | bir | 700 |
| 4 | 8 | $\sim$ | 80 | b | 800 |
| L | 9 | 12 | 90 | Her | 900 |
| milue. |  | diLanes de milue. |  | CEETAINES dB mille. |  |
|  | 1,000 | عת | 10,000 | 6الع | 100,000 |
| العى | 2,000 | Lus | 20,000 | لا | ,000 |
| سת | 3,000 | سلا | 30,000 | Cllac | 300,000 |
| لred | 4,000 | لـعلا | 40,000 | للس | 400,000 |
| حك | 5,000 | حلا | 50,000 |  |  |
| U | 6,000 | d | 60,000 |  |  |
| rerer | 7,000 | بعلا | 70,000 |  |  |
| cr | 8,00 | كـلا | 80,000 |  |  |
| لعف | 9,000 | كعلا | 90,000 |  |  |

Figure 12: Printed forms of Diwani numbers (from Pihan 1860: 211).

EXEMPLES DE QUELQUES NOMBRES COMPOSES.

| cl | 11 | ser | ${ }^{17}$ | لالع1 | 42 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| لاع | 19 | ys | 18 | \% | 48 |
| \% | 13 | תr | 19 | 6الع16 | 141 |
| لل0 | 14 | el | ${ }^{21}$ | 1646 | 159 |
| 97 | 15 | لur | 34 | - 6 | 206 |
| 4 | 16 | حس1 | 35 | بلفاحs | 315 |

Figure 13: Printed forms of Diwani compound numbers (from Pihan 1860: 212).

## DE L'ÉGRITURE APABE.

ou figurait ces chiffres sur le sable; l’autre est appecée dyoudny, et s'employait jadis dans les bureaux de ladministration supérieure.
chiffres ghobit.


Comme il n'existe pas de zéro dans ce genre de numération, les dizaines s’indiquent par un point sur les unités, les centaines par deux points, et les mille par trois points; exemples: $\dot{\sim} 20, \vec{\gamma} 700, \dot{\boldsymbol{*}} 3000$, etc.

Les chiffres ghobir sont usités dans certains ourrages de mathématiques et de géographie.
chiffres dyouâny.


Ces signes paraissent être plutôt des abréviations de mots arabes exprimant les quantités, que de véritables chiffres. Pour les nombres plus élevés, on peut voir le

Figure 14: Printed forms of the "chiffres dyouâny" or "diwani numbers" (from Pihan 1861: 33). The metal font differs from that used in the excerpts shown in figures 12 and 13.

