

Universal Multiple-Octet Coded Character Set
International Organization for Standardization
Internationale Standardisierungs-Organisation
Organisation Internationale de Normalisation
Διεθνής Οργανισμός Τυποποίησης
Международная организация по стандартизации

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Title: Proposal to encode 21 miscellaneous scientific symbols

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1. Background

This proposal is part of the research program upon historical mathematical sources, conducted by the CNRS Philiumm project (headed by Prof. David Rabouin, University of Paris) and supported by researchers from the Landesbibliothek Hanover (Germany). The aim of this project work is to achieve a standardized encoding for special mathematical characters in historic texts, which is required for accurate facsimile editions of those sources.

For more background information about the Philiumm project and the related research work, please visit the [Philiumm website](#) or see doc. no. [N5277](#).

2. Miscellaneous symbols in historic sources

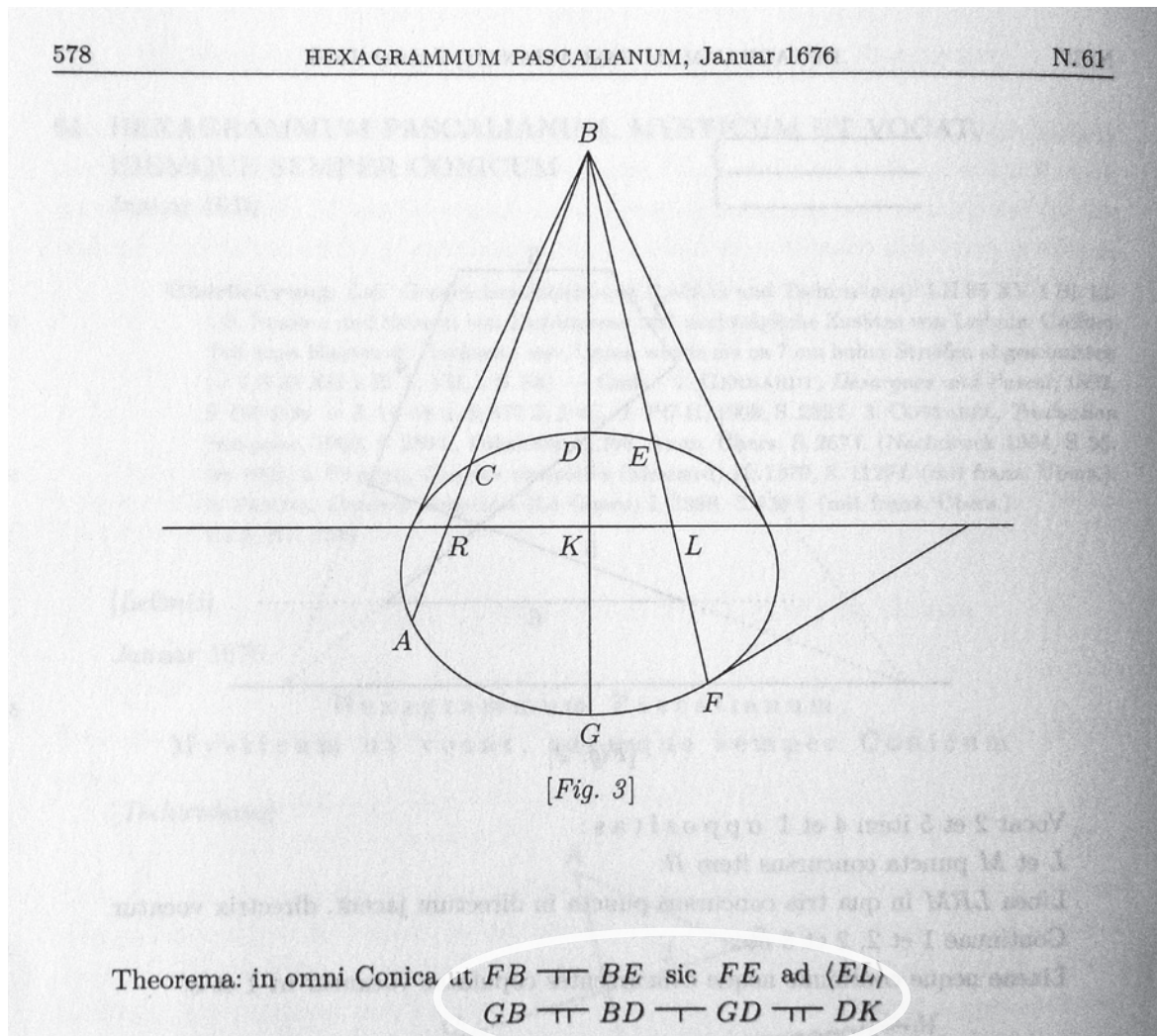
In this proposal we introduce a number of various symbols, mainly from the field of historical mathematics. Some of them are combining symbols (or marks) which in the sources occur in combination with digits or other symbols.

3. Characters

If this proposal gets accepted, the following characters will exist:

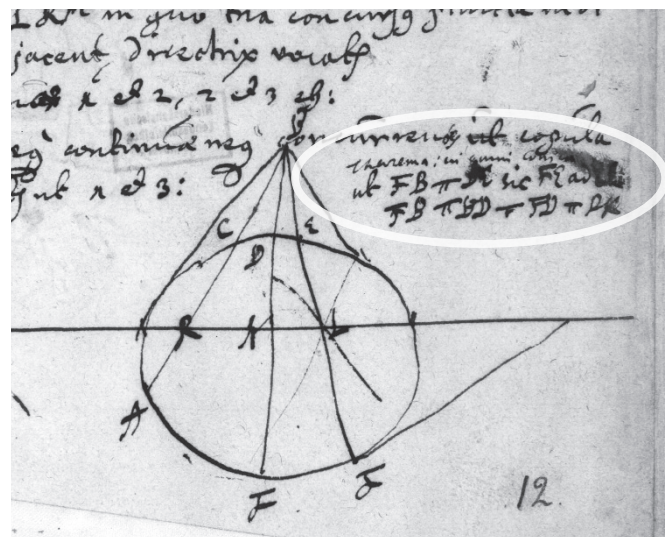
✕	CASTING-OUT-NINES
①	LUNATE ENCIRCLED DIGIT ONE
⌞	PROPORTION WITH ONE STROKE
⌘	PROPORTION WITH TWO STROKES
∞	INFINITY WITH TWO DOTS
⊖	INVOLVED
Ⓥ	LEIBNIZIAN ENCIRCLED V
Ⓥ	LEIBNIZIAN ENCIRCLED V IN BOX
- -	BROKEN EMDASH
⊕	CROSSED EMDASH
⁂	SUPERSCRIPT WAVE SYMBOL
⁂	SUPERSCRIPT WAVE WITH OVERLINE SYMBOL
⊙	COMBINING BOMBELLI POWER MARK
⧸	COMBINING DOUBLE-WIDE SLASH
⊙	COMBINING HALF CIRCLE BELOW
⊙	COMBINING ENCLOSING SPIRAL MARK
⊙	COMBINING DOUBLE-WIDE ENCLOSING SPIRAL MARK
⊙	COMBINING FACTOR MARK
⊙	COMBINING OVERLINE WITH TERMINALS
⊙	COMBINING DOUBLE-WIDE OVERLINE WITH TERMINALS
⊙	COMBINING HORIZONTAL PARANTHESIS

4. Figures and explanations



⊢ PROPORTION WITH ONE STROKE, ∟ PROPORTION WITH TWO STROKES
 LAA VII-7 p. 578

⊢ PROPORTION WITH ONE
 STROKE, ∟ PROPORTION WITH
 TWO STROKES
 LH 35 XV 1, fol. 12r



$$\begin{array}{c} \text{A} \text{---} \text{B} \text{---} \text{L} \quad \text{C} \text{---} \text{D} \text{---} \text{L} \quad \text{AB} \quad \text{EL} \quad \text{DC} \\ x \text{---} \text{---} \text{---} t \text{---} \text{---} c \text{---} \text{---} y \text{---} u \\ \text{DF} \propto a \quad [\text{BG} \propto d. \quad d^2 - a^2 \propto b^2 - c^2] \end{array}$$

[Leibniz]

ABDC semicirculus. AG $\cap$ AF. BCG est recta. DCF est recta.
DF $\cap$ a. BG $\cap$ d. BC $\cap$ b. BL $\cap$ t. AD $\cap$ y. AL $\cap$ v.

⊢ PROPORTION WITH ONE STROKE, ⊢ PROPORTION WITH TWO STROKES
LAA VII-2 p. 850

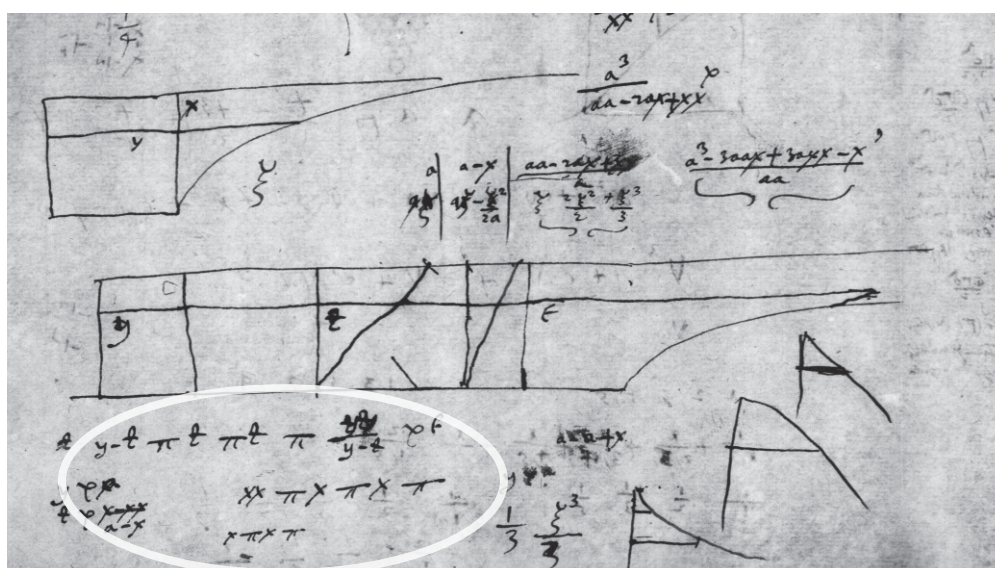


[Fig. 6]

$$\begin{array}{c} z \quad y \text{---} z \text{---} \text{---} z \text{---} \text{---} z \text{---} \text{---} \frac{zz}{y-z} \propto t \\ y \propto \\ z \propto a - x \quad \quad \quad xx \text{---} \text{---} x \text{---} \text{---} x \text{---} \text{---} \\ \quad \quad \quad x \text{---} \text{---} x \text{---} \text{---} \end{array}$$

10

⊢ PROPORTION WITH TWO STROKES
LAA VII-6 p. 271



⊢ PROPORTION WITH TWO STROKES
LH 35 V 6, fol. 10v

Als men de $\angle ACB$ wil 2 mahl in 2 gelijcke deel, deelen; om AF te vinden, soo kan men het dus oock doen[:]

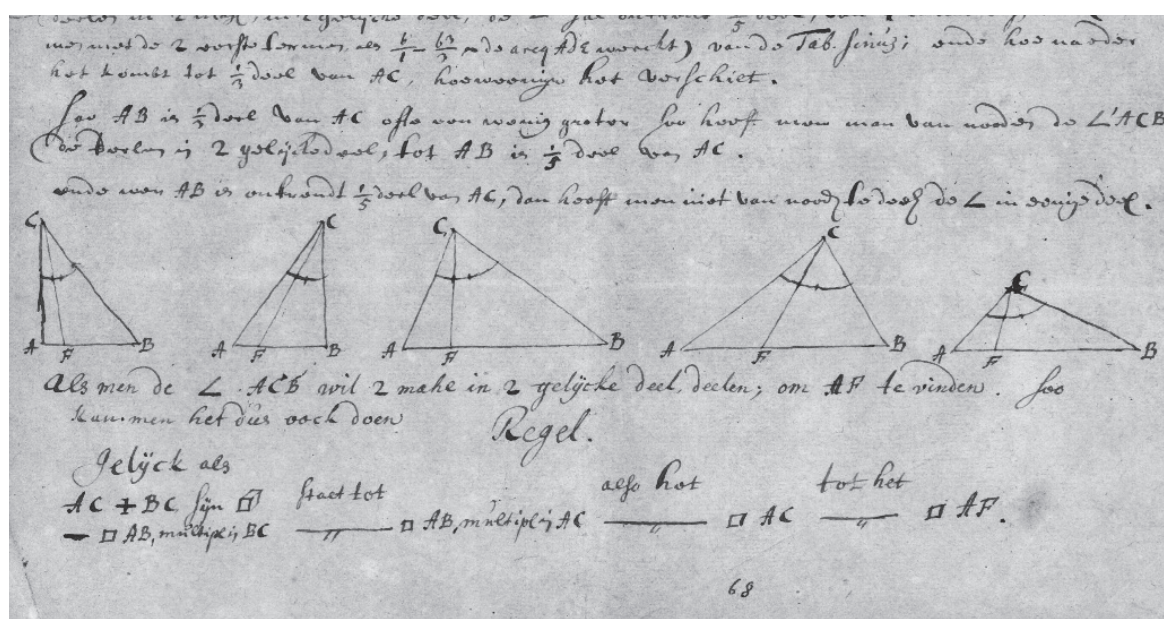
Regel.

Gelijck als

5 $AC + BC$, sijn $\square$ staet tot also het tot het
 $-\square AB$, multipl. in BC --- $\square AB$, multipl. in AC --- $\square AC$ --- $\square AF$.

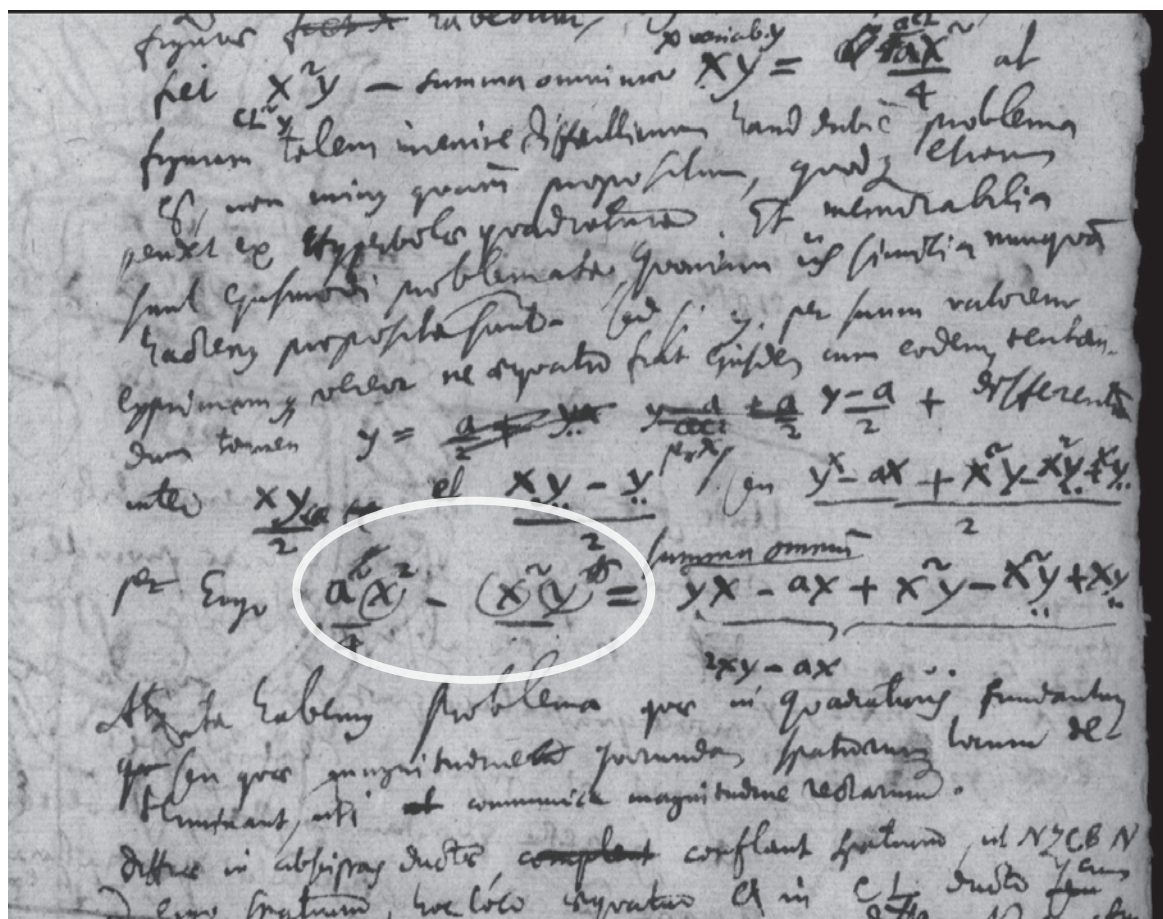
⌘ PROPORTION WITH TWO STROKES

This figure also shows the use of $\square$ WHITE CUBE (proposed in doc. L-2514 for u1F7F7).
 LAA VII-6 P. 302



⌘ PROPORTION WITH TWO STROKES

LH 35 VIII 30, fol. 68r



☉ COMBINING HALF CIRCLE BELOW

The shape of the character is typically at least a half circle, often it approximates 3/5 of a circle. Hence it is considerably different from COMBINING DOUBLE BREVE BELOW (035C).
LH 35 XIII 3, fol. 250v

Sed si y per suum valorem exprimamus, vereor ne aequatio fiat eiusdem cum eodem, tentandum tamen[:]

$$y = \frac{y-a}{2} + \text{differentia inter } \frac{xy}{2} \text{ et } \frac{xy-y}{2} \text{ per } x \text{ seu } \frac{yx-ax+x^2y-x^2y+xy}{2}. \text{ Ergo}$$

$$\frac{ax^2}{4} - (xy) = \text{summa omnium } \frac{yx-ax+x^2y-x^2y+xy}{2xy-ax}.$$

Atque ita habemus problemata quae in quadraturis fundantur, seu quae magnitudine quorundam spatiorum locum determinant, uti communia magnitudine rectorum.

Differentiae in abscissas ductae, conflant spatium ut $NZCBN$. Id ergo spatium hoc loco aequatur a in CL ducto, cum rectangulum QMB (quia QN et QM non differunt)

3 ZN^2 NM erg. L 6 posita φ maxima = CL . erg. L 8 CL^2 y ; φ variab. y ; a CL^2 erg. L

☉ COMBINING HALF CIRCLE BELOW

LAA VII-4 p. 824

ottavo del quadrato delli Tanti, fa 84 e se li aggiunge la metà delle 2 et 1 $\frac{1}{2}$ per regola, fa $84 + 2 \frac{1}{2} + 1 \frac{1}{2}$, che si salva. Poi si moltiplica la metà de' Cubi via la metà delli Tanti, fa 48, che aggiuntoli il numero cioè 2, fa 50, che sono Tanti e sono eguali a $84 + 2 \frac{1}{2} + 1 \frac{1}{2}$ serbato di sopra, che agguagliato, il Tanto valerà 2 e detto 2 si cava d'1 $\frac{1}{2} + 4 \frac{1}{2}$ (e li 4 $\frac{1}{2}$ nascono dalla metà de' Cubi) resta $1 \frac{1}{2} + 4 \frac{1}{2} - 2$, che il suo quadrato è $1 \frac{1}{2} + 8 \frac{1}{2} + 12 \frac{1}{2} - 16 \frac{1}{2} + 4$, che cavatone $1 \frac{1}{2} + 8 \frac{1}{2} + 4 \frac{1}{2} + 2$ resta $8 \frac{1}{2} - 16 \frac{1}{2} + 2$, che aggiunto a $24 \frac{1}{2}$ fa $8 \frac{1}{2} + 8 \frac{1}{2} + 2$, ch'il suo lato è R.q. $8 \frac{1}{2} + R.q. 2$ et è eguale a $1 \frac{1}{2} + 4 \frac{1}{2} - 2$, che agguagliato, il Tanto valerà R.q. L3 — R.q. 18J + R.q. 2 — 2.

Capitolo di potenza potenza Cubi Tanti e numero eguale a potenza.⁸³

Il presente Capitolo patisce le eccezioni degli altri sopradetti e può venire in assai modi, del quale (com'altre volte ho detto) per non andare, in l'infinito, ne porrò solo uno essemio.

Agguagliasi $1 \frac{1}{2} + 6 \frac{1}{2} + 6 \frac{1}{2} + 22$ a $29 \frac{1}{2}$. Aggionghisi alle 1 $\frac{1}{2}$ quarto del quadrato de' 3, ch'è 9, fa 38, e moltiplichisi per 11, metà del numero, fa 418, al quale si aggiunge l'ottavo del quadrato delli 3, ch'è $4 \frac{1}{2}$, fa $422 \frac{1}{2}$ e salvisi; poi si moltiplica la metà de' Cubi via la metà delli Tanti, fa 9 e si cava del numero, resta 13, e sono 1, che aggiunti a $422 \frac{1}{2}$ serbato di sopra fa $422 \frac{1}{2} + 13 \frac{1}{2}$ e per regola è eguale a $1 \frac{1}{2} +$ la metà delle 2, cioè $14 \frac{1}{2} \frac{1}{2}$, che agguagliato, il Tanto valerà 5 e si aggiunge a $1 \frac{1}{2} + 3 \frac{1}{2}$, fa $1 \frac{1}{2} + 3 \frac{1}{2} + 5$ e li Tanti nascono dalla metà de' Cubi, che il suo quadrato è $1 \frac{1}{2} + 6 \frac{1}{2} + 19 \frac{1}{2} + 30 \frac{1}{2} + 3$, che cavatone $1 \frac{1}{2} + 6 \frac{1}{2} + 6 \frac{1}{2} + 22$ resta $19 \frac{1}{2} + 24 \frac{1}{2} + 3$, che aggiunto a $29 \frac{1}{2}$ fa $48 \frac{1}{2} + 24 \frac{1}{2} + 3$, che il suo lato è R.q. $48 \frac{1}{2} + R.q. 3$ et è eguale a $1 \frac{1}{2} + 3 \frac{1}{2} + 5$ detto di sopra, che agguagliato, il Tanto valerà R.q. $12 - 1 \frac{1}{2} + R.q. L9 \frac{1}{4} - R.q. 75J$, ovvero R.q. $12 - 1 \frac{1}{2} - R.q. L9 \frac{1}{4} - R.q. 75J$, che l'una e l'altra valuta è vera.

⁸³ È l'equazione

$$x^4 + ax^3 + cx + d = bx^2.$$

Ci limiteremo d'ora in avanti agli esempi del B. avvertendo che gli altri casi sono sempre facilmente ricavabili dagli esempi finora posti. Qui si ha:

$$y^3 + \frac{b}{2} y^2 = \left(d - \frac{ac}{4}\right) y + \left(b + \frac{a^2}{4}\right) \frac{d}{2} + \frac{c^2}{8}.$$

Capitolo di potenza potenza potenze Tanti e numero eguale a Cubi.⁸⁴

Questo Capitolo patisce le difficoltà de' Capitoli di 2 eguale a 1 e numero e di 3 e numero eguale a 1 e rare volte si può agguagliare senza + di — e di esso solo ne porrò un essemio.

Agguagliasi $1 \frac{1}{2} + 3 \frac{1}{2} + 40 \frac{1}{2} + 20$ a $8 \frac{1}{2}$. Piglisi il quarto del quadrato de' 3, ch'è 16, del quale se ne cava 3, numero delle 2, resta 13, che moltiplicato via 10, metà del numero fa 130 e se li aggiunge l'ottavo del quadrato delli 1, ch'è 200, fa 330 e se li aggiunge la metà delle 2, ch'è $1 \frac{1}{2} \frac{1}{2}$, et $1 \frac{1}{2}$ per regola, fa $330 + 1 \frac{1}{2} \frac{1}{2} + 1 \frac{1}{2}$ e si salva. Poi si moltiplica la metà delli 1 via la metà de' 3, fa 80 et aggiuntoli il numero fa 100, e sono 1, che sono eguali a $330 + 1 \frac{1}{2} \frac{1}{2} + 1 \frac{1}{2}$ serbato di sopra, che agguagliato, il Tanto valerà 6, che si cava d'1 $\frac{1}{2} - 4 \frac{1}{2}$, resta $1 \frac{1}{2} - 4 \frac{1}{2} - 6$ (e li $-4 \frac{1}{2}$ nascono dalla metà delli Cubi e sono meno per essere li Cubi dalla parte contraria della 1), che il suo quadrato è $1 \frac{1}{2} - 8 \frac{1}{2} + 4 \frac{1}{2} + 48 \frac{1}{2} + 36$, che cavatone $1 \frac{1}{2} + 3 \frac{1}{2} + 40 \frac{1}{2} + 20$, resta $1 \frac{1}{2} + 8 \frac{1}{2} + 16 - 8 \frac{1}{2}$, che aggiunto a $8 \frac{1}{2}$ fa $1 \frac{1}{2} + 8 \frac{1}{2} + 16$, che il suo lato è $1 \frac{1}{2} + 4 \frac{1}{2}$ et è eguale a $1 \frac{1}{2} - 4 \frac{1}{2} - 6$, che agguagliato, il tanto valerà R.q. $16 \frac{1}{4} + 2 \frac{1}{2}$; avvertendosi che il lato d'1 $\frac{1}{2} - 8 \frac{1}{2} + 4 \frac{1}{2} + 48 \frac{1}{2} + 36$ può essere $6 + 4 \frac{1}{2} - 1 \frac{1}{2}$, che agguagliato, il Tanto valerà R.q. $4 \frac{1}{4} + 1 \frac{1}{2}$.

Capitolo di potenza potenza Cubi e Tanti eguale a potenza e numero.⁸⁵

Di questo Capitolo si può fare la positione in due modi e patisce le difficoltà del passato, e l'essemio che io ne porrò sarà di $-1 \frac{1}{2}$ di numero.

Agguagliasi $1 \frac{1}{2} + 12 \frac{1}{2} + 72 \frac{1}{2} + 8 \frac{1}{2} + 84$. Piglisi il quarto del quadrato delli Cubi, ch'è 36, e aggionghisi alle 2, fa 44, e moltiplichisi via la metà del numero, fa 1848, che cavatone l'ottavo del quadrato delli 1, resta 1200, e se li aggiunge la metà delle 2, fa $1200 + 4 \frac{1}{2}$ e si salva; poi si moltiplica il mezzo dei Cubi via il mezzo delli 1, fa 216,

⁸⁴ È l'equazione

$$x^4 + bx^3 + cx + d = ax^2.$$

Posto $-y$, si ottiene la seconda equazione della n. 82.

⁸⁵ È l'equazione

$$x^4 + ax^3 + cx = bx^2 + d.$$

Posto $-y$, si ottiene la:

$$y^4 + \left(d + \frac{ac}{4}\right) y = \frac{b}{2} y^3 + \left(\frac{a^2}{4} + b\right) \frac{d}{2} - \frac{c^2}{8}.$$

COMBINING BOMBELLI POWER MARK

A digit combined with a small bow below as introduced by R. Bombelli, denotes the n-th power of a quantity. Example from Bombelli (1966).

Agguagliasi $1 \frac{1}{2} + 6 \frac{1}{2} + 6 \frac{1}{2} + 22$ a $29 \frac{1}{2}$. Aggionghisi alle quarto del quadrato de' 3, ch'è 9, fa 38, e moltiplichisi per 11, metà del numero, fa 418, al quale si aggiunge l'ottavo del quadrato de' 3, ch'è $4 \frac{1}{2}$, fa $422 \frac{1}{2}$ e salvisi; poi si moltiplica la metà de' Cubi via la metà delli Tanti, fa 9 e si cava del numero, resta 13, e sono 1, che aggiunti a $422 \frac{1}{2}$ serbato di sopra fa $422 \frac{1}{2} + 13 \frac{1}{2}$ e per regola è eguale a $1 \frac{1}{2} +$ la metà delle 2, cioè $14 \frac{1}{2} \frac{1}{2}$, che agguagliato, il Tanto valerà 5 e si aggiunge a $1 \frac{1}{2} + 3 \frac{1}{2}$, fa $1 \frac{1}{2} + 3 \frac{1}{2} + 5$ e li Tanti nascono dalla metà de' Cubi, che il suo quadrato è $1 \frac{1}{2} + 6 \frac{1}{2} + 19 \frac{1}{2} + 30 \frac{1}{2} + 3$, che cavatone $1 \frac{1}{2} + 6 \frac{1}{2} + 6 \frac{1}{2} + 22$ resta $19 \frac{1}{2} + 24 \frac{1}{2} + 3$, che aggiunto a $29 \frac{1}{2}$ fa $48 \frac{1}{2} + 24 \frac{1}{2} + 3$, che il suo lato è R.q. $48 \frac{1}{2} + R.q. 3$ et è eguale a $1 \frac{1}{2} + 3 \frac{1}{2} + 5$ detto di sopra, che agguagliato, il Tanto valerà R.q. $12 - 1 \frac{1}{2} + R.q. L9 \frac{1}{4} - R.q. 75J$, ovvero R.q. $12 - 1 \frac{1}{2} - R.q. L9 \frac{1}{4} - R.q. 75J$, che l'una e l'altra valuta è vera.

Dimostrazione delle Rc. legate con il piu di meno, e meno di meno, in linea (+ puto: in linee +).

Habbisi Rc.₄ p. di m. Rq.₁₁, p. Rc.₄ m. di m. Rq. 11, e per trovare la sua linea aggiungasi 16. quadrato del 4. con 11. quadrato di Rq.₁₁. fa 27. e di questo si pigli il lato cubo ch'è 3. e per regola si moltiplichi per 3. fa 9, e salvisi, poi per regola si moltiplica il 4. per 2. fa 8, e queste due [Rc.] legate sono nate dall'aggiugliatione d' $1 \frac{3}{2}$ a $9 \frac{1}{2}$ p. 8. però faccisi la dimostrazione in linea d' $1 \frac{3}{2}$ eguale a $9 \frac{1}{2}$ p. 8. cioè in superficie piana e si troverà che la longhezza del tanto sarà ancora la longhezza delle due Rc. legate proposte.

Subicit postea demonstrationem quae originem exhibet inventionis regularum Cardani per sectionem cubi. Sed notat ipse

Sia $1 \frac{3}{2}$ eguale a $6 \frac{1}{2}$ p. 4. e sia la q. la unità. Tirisi la m.e. e faccisi m.l. che sia pari alla q. cioè sia 1. e l.f. o. cioè quanto è il numero delli tanti, e sopra detta l.f. si faccia un parallelogrammo che sia 4. di superficie, cioè quanto il numero, e sarà il parallelogrammo a.b.f. poi allonghisi la a.b. sino in d. ed' a.l. sino in r. poi habbiansi due squadri, delli quali l'uno si ponga con l'angolo sopra la linea r. e che l'uno delle braccia tocchi la estremità m. il qual squadra si alzi o abbassi tanto, che tirato dal angolo del squadra una linea, che tocchi la estremità f. che vada a toccare la b.d. in tal luogo, che mettendo un altro squadra con l'angolo al detto toccamento, e con l'uno delle braccia sopra la d.a. vadi a intersegare il braccio dell'altro squadra nella linea f.e. fatto questo dico che la linea, ch'è dal punto l. sino al angolo del squadra. è la valuta del tanto, e lo provo in questo modo. Presupposto che si habbia alzato e abbassato lo squadra talmente, che in l. tirando la l.f. ciao in c., e che il braccio dello squadra p. tagliassi con l'altro squadra in g. suso la linea g.e. fatto questo; dico la linea l.i. essere la valuta del tanto. Perché essendo la l.i. $1 \frac{3}{2}$ et m.l.i. (+ male credo impressum, lege: et m.l. 1. +) la l.g. sarà $1 \frac{3}{2}$, perché tanto può la m.l. in l.m. (+ lege: in l.g. +) quanto l.i. in se stessa, essendo il angolo i. retto, il parallelogrammo i.l.g. sarà un cubo (+ vel y^3 +) et il parallelogrammo i.l.f. sarà $6 \frac{1}{2}$, perché i.l. è $1 \frac{3}{2}$, et l.f. 6. et il parallelogrammo h.f.g. sarà 4, perché pari al parallelogrammo a.l.f. ch'era 4, e essendo i.l.g. tutto insieme $6 \frac{1}{2}$, e 4.; e per l'altra ragione è provato essere $1 \frac{3}{2}$, dunque $1 \frac{3}{2}$ sarà eguale a $6 \frac{1}{2}$ p. 4., et la i.l. sarà $1 \frac{3}{2}$, che per la aggiugliatione insegnata la l.i. sarà Rq.3. p. 1. la l.g. sarà 4. p. Rq.12. la f.g. sarà

☉ COMBINING BOMBELLI POWER MARK

A digit combined with a small bow below as introduced by R. Bombelli denotes the n-th power of a quantity. By this, Bombelli provides a different formalization of what is addressed otherwise by the use of cossic signs. Today, we write x , x^2 , x^3 , ... instead. This combining mark is intended for the use with superscript digits (00B2, 00B3, 00B9; 2074...2079).

LAA VII-2 p. 662, 663

ce tanto sconuenueuole, che più dir non si potrebbe, per
che pare, che punto non si confaccia in materia de nu-
meri sapendosi generalmente, che cosa significhi que-
sta uoce di censo senza che io lo dichi: Da altri è stato
chiamato poi quadrato, il qual nome è atto à genera-
re confusione perche bisogna poi nominare li numeri
quadrati, e le superficie quadrate: però mi son risoluto
di seguitare Diofante (come hò fatto nel restante,) e
chiamarlo potenza, la quale potenza quando è uno si
fa quadrato del Tanto, e si segnerà con questo cara-
tero $\textcircled{2}$.

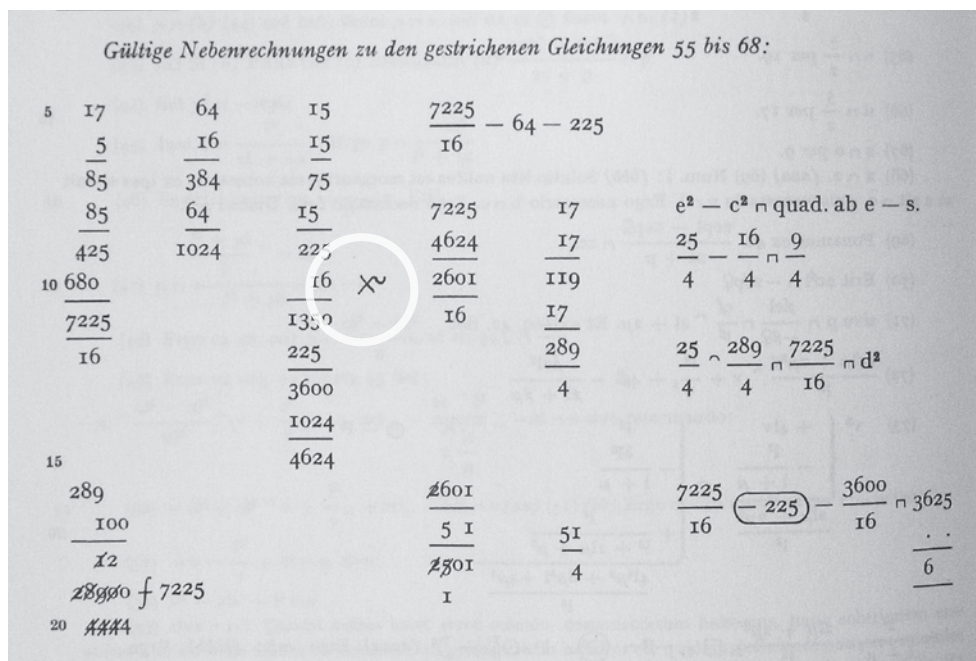
Diffinitione del cubo.

Il cubo è il prodotto di una potenza moltiplicata uia
vn Tanto, che uiene à seruare l'ordine de' cubi, che il
prodotto d'un numero quadrato moltiplicato uia il
suo lato, fa numero cubo, parimènte la potenza, ch'è qua-
drata moltiplicata uia il tanto suo lato, produce il cubo,
il quale si segnerà con questo caratere $\textcircled{3}$.

Diffinitione della potenza di potenza.

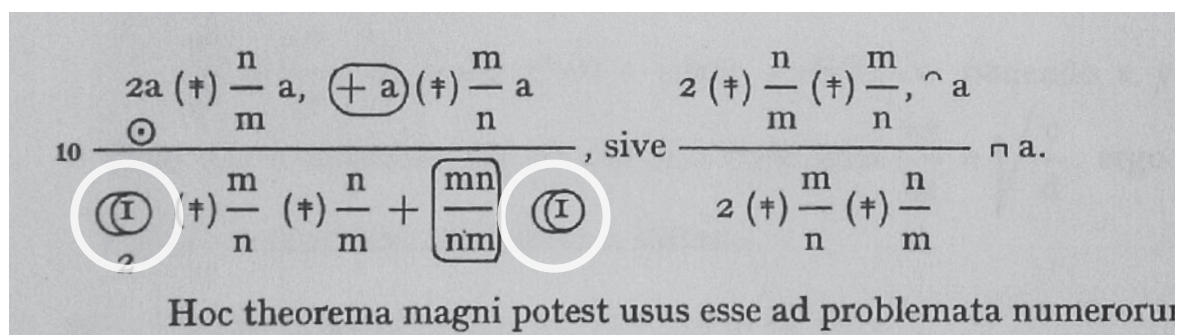
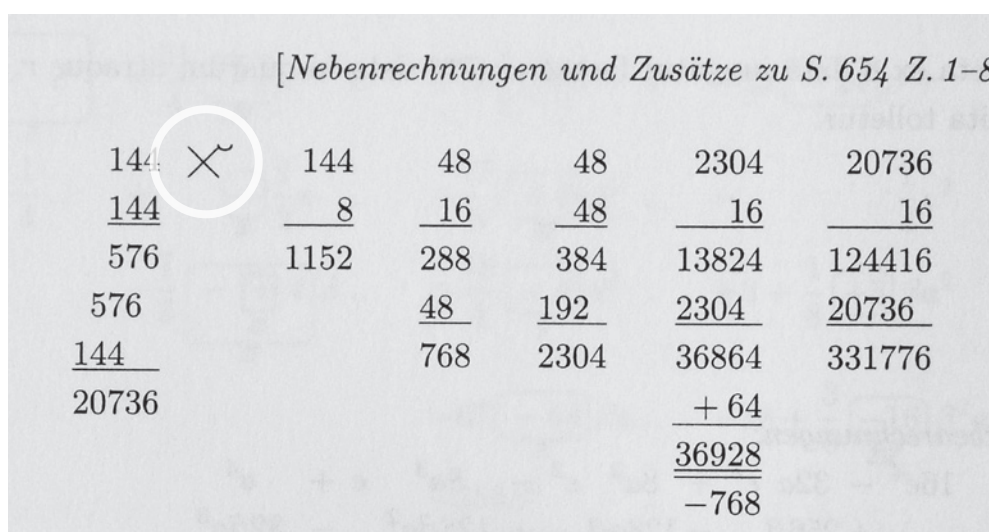
La potenza di potenza è il quadroquadrato del Tan-
to, ouero il quadrato della potenza, ouero il produt-
to del cubo uia il tanto, la quale sarà segnata con que-
sto caratere $\textcircled{4}$, e tutti questi nomi saranno chiamati di-
gnità, le quali (per non dilattarmi troppo) ma seguen-
do la solita breuità, non diffinirò particolarmente, pa-
rendomi, che queste bastino, poiche l'altre tutte nasco-
no da questo, e solo porrò li nomi loro qui sotto, e il suo
caratere.

© COMBINING BOMBELLI POWER MARK
R. Bombelli, L'Algebra. Bologna 1579, p. 203



×~ CASTING-OUT-NINES

LAA VII-1 p. 408; VII-3 p.660 (below)



① LUNATE ENCIRCLED DIGIT ONE

LAA VII-1 p. 472

Dn. Osannam, Mengolus, et Itali plerique, alique, an qui superscribunt literae, ut Cartesius, Wallisius; posteriores patet praeferendos, quia prioribus methodus mea sine confusione applicari non potest, nam pone esse quantitatem $(2) [4] a^2 3b$ more meo scriptam, more ipsorum fieret: $(2) 4a^2 3b$, ubi vides opus esse virgula interiecta, et proinde vel alio signo turbante ne confundantur numeri dimensionum, cum numeris calculi. Et cum postea novenarii proba adhibenda est cavendum est ne hos quoque numeros dimensionum aliquando caeteris confundamus, et, cum caeteris interponantur, perpetuo mentem turbant, gerent, cum contra si semper superscribantur; nihil turbant, accedit una magna ratio, quod aliquando ipsi numeri dimensionum sint in caeteros reflexi ut $41^2 h^2$, quod significat ipsum numerum 41 in se multiplicandum.

Dicet aliquis ad rationem praecedentem numeros calculo seu probae novenarii subi-ciendos, semper more communi, et ipsius Cartesii ac Wallisii initio termini ponendos; neque quenkum ante me, eos ipsi termino inseruisse nam in exemplo praedicto pro $(2) 4a^2 3b$ scribendum esse more communi, (et si velis adhibito meo separare numeros essen-tiales a fictitiis,) $(2) 12a^2 b$. Ita omnes numeri erunt ab initio, et ad secundam rationem. Dicetur: non esse ita scribendae 41^2 , sed absolvendam operationem seu scribendum 1681 . Verum hinc apparet perdi maximum methodi meae commodum quod est, numeros adhiberi,

☉ COMBINING ENCLOSING SPIRAL MARK

This non-spacing mark is to be combined with digits.

LAA VII-1 p. 530

cuius aequationis ut tollatur terminus secundus, (a) fiet (b) ponemus $\frac{3}{2}z + \frac{2e}{4} \cap 2y$, sive unde:

$$16y^4 \cap \frac{81}{16}z + (4) \frac{e}{2} \frac{27}{8}z + (6) \frac{e^2}{4} \frac{9}{4}z^2 + (4) \frac{e^3}{8} \frac{3}{2}z + \frac{1}{16}e^4 \cap 0. (2) 2y - 12e L \quad 4 \quad 2e L \text{ ändert Hrs dreimal}$$

☉ COMBINING ENCLOSING SPIRAL MARK, ☉ COMBINING DOUBLE-WIDE ENCLOSING SPIRAL MARK – LAA VII-2 p. 180; VII-3 p. 630 (below)

630 DIFFERENZEN, FOLGEN, REIHEN 1672–1676 N. 432

$$625y^4 + \frac{8b5s}{a} 125y^3 + 64b^2 - \beta^2 \sim \frac{5s}{a} 25y^2 + \frac{64b^2\beta - \beta^3[-1]5a^2}{(8)} 5y \quad *$$

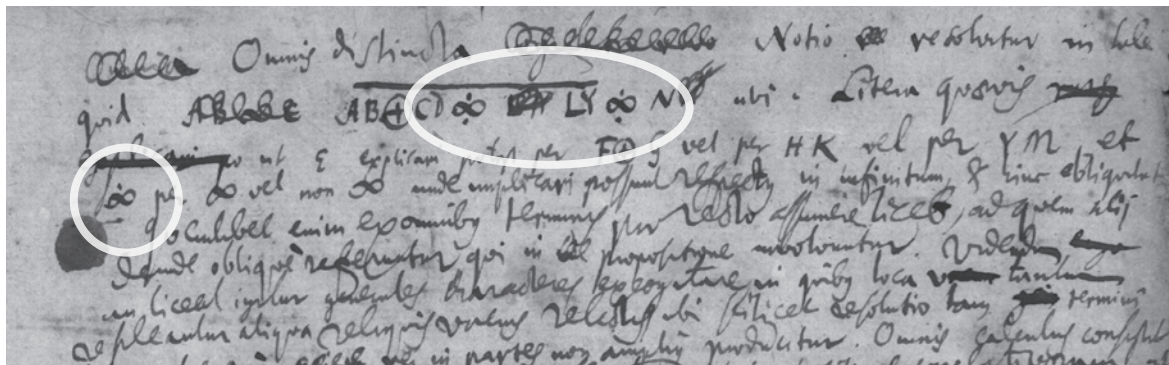
$$+ \frac{10\gamma\beta}{(2)5s} \dots + \beta 8b \sim (2) \dots$$

$$\begin{array}{ccccccc} (41) & (319) & (8) & & & & \\ -31\lambda & -278\mu a & +72a^2\xi & & +66ma^3 & & \end{array}$$

Unde $10g \cap (2) 8^4 25^4 a^2 + 10\gamma\beta a - (2) 31\lambda a 5s, \sim (2) a 5s$, et $41h \cap (2) 5s 64b^2 - (2) 5s\beta^2 +$

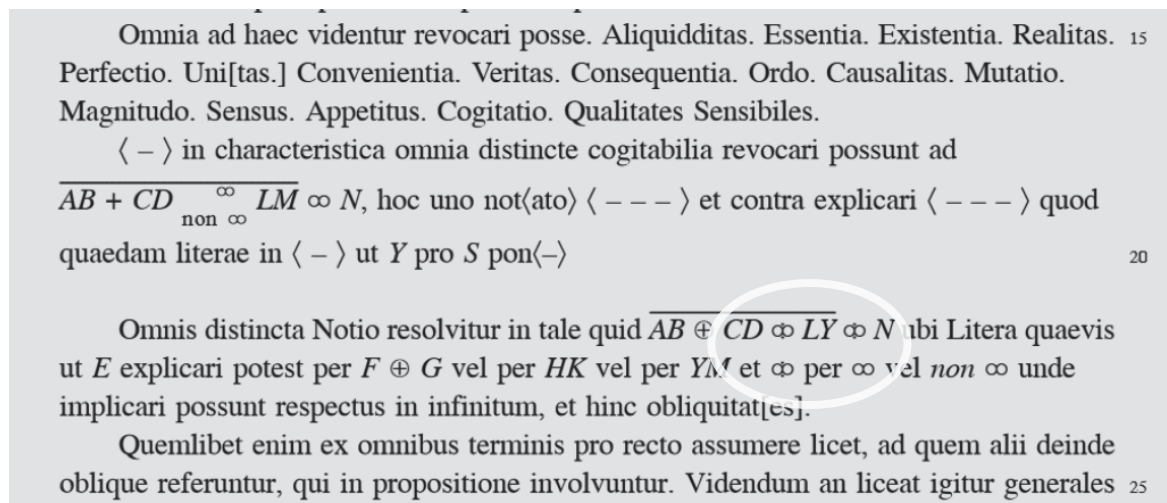
$$\beta a 8b - (2) 278\mu a^2 \sim (2) a^2.$$

$$\begin{array}{ccccccc} (8) a^3 125s^3 \sim 1000g^3 & \cap & (8) 8b^3 25^3 s^3 & + & (12) 64b^2 25^2 s^4 10\gamma\beta a & - & (24) 64^2 25^2 s^4 31\lambda a 5s, \\ & & & & & & \\ & & & & + & (6) 8b 25s^2 100\gamma^2 \beta^2 a^2 & + & (24) 8b 25s^2 31^2 \lambda^2 a^2 25^2 s^2 \end{array}$$



∞ INFINITY WITH DOTS

LH 4 VII B 2, fol. 73v (top), LAA VI-4 p. 873 (below)



In a comment from SEW (2024) another solution has been proposed:

#8 INFINITY SIGN WITH DOTS This character could potentially already be accurately represented using the sequence <∞>.

¶8 This solution would require a sequence of **three** different existing characters of which two are combining characters. In which succession they are to be arranged properly? This is not at all obvious and hence this model would result in at least two different sequences in practice, which makes the identification of the character difficult to impossible, because one can never be sure (in a search) to reach all instances, when they happen to be encoded differently (although looking the same visually). Moreover, there is precedence of structurally similar cases encoded. For instance, the Mathematical Operators block contains a range of characters whose glyphs are built of other well-known base glyphs and dots, in the range 2238 to 2255; e.g. HOMOTHETIC (223B) and GEOMETRICALLY EQUAL TO (2251) can be seen as analogue characters, which have their own meaning, despite being graphically composed of prevalent glyphs. There are also many characters which are represented by combinations of e.g. = or < with a SLASH or ‘solidus overlay’. It is a feature inherent in mathematical notation that new expressions are created by combining established elements, in the one way or the other. Nevertheless, it is justifiable to assign a separate codepoint for such a character, because its use and meaning are testified and this encoding is conformant with established encoding practice and principles.

		Rechenkunst.		73
		$D - E = 2B$		
		$D = E + 2B$		
		$\therefore D > E$		
		Aus D und F das übrig finden.		
$a = ?$	1	$a + b = D$		
$b = ?$	2	$ab = F$		
$i \odot 2$	3	$aa + 2ab + bb = DD$		
$i * 4$	4	$4ab = 4F$		
$3 - 4$	5	$aa - 2ab + bb = DD - 4F$		
$5 \sqrt{2}$	6	$a - b = \sqrt{DD - 4F}$		
		Weil $a + b$ Item $a - b$ bekant sind / so werr es ein überfluß weiter zuprocedieren / als da in den nächst hiervorstehenden auflösungen / die manier weiter zuschreiten / vor augen ligt.		
		Aus D und G.		
$a = ?$	1	$a + b = D$		
$b = ?$	2	$\frac{a}{b} = G$		

© INVOLVED – J. H. Rahn, Teutsche Algebra, 1659 (after Cajori).

In expressions of the form $a \odot b$, the sign $\odot$ is used to denote the exponentiation of a by the power of b . In his “Teutsche Algebra” from 1659, the swiss mathematician Johann Heinrich Rahn refers to the operation as “involieren” (= to involve).

		Involieren in einfachen ungebrochenen quantiteten.				
		Das Hauptzeichen des Involviereus ist $\odot$ heisset eingewickelt oder involviert.				
		Regel.				
		So vil mal eine quantitet erslich in sich selbs/darnach in ihr product / und drittens wider in das letztere product /c. eingewickelt oder involviert wird ; so groß ist das vermögen besagter quantitet / so groß muß auch die zahl seyn die solchem zeichen in dem breiten reyen des nebenrands nachzusetzen ist.				
$i \odot 2$	1	$-a$	$++ab$	bcd	yx	zyy
$i \odot 3$	2	$++aa$	$++aabb$	$bbccdd$	$yyxx$	$4y^4$
$i \odot 4$	3	$-a^3$	$++a^3b^3$	$b^3c^3d^3$	y^3x^3	$8y^6$
	4	$++a^4$	$++a^4b^4$	$b^4c^4d^4$	y^4x^4	$16y^8$

© INVOLVED – J. H. Rahn, Teutsche Algebra, 1659.

In the time of Leibniz, the usual way of referring to curves or magnitudes is by giving equations that describe their specific relations. The concept of mapping as it is used in modern mathematics is not yet developed. Leibniz writes the signs $\odot$ and $\boxed{\odot}$ to the right of an expression (such as $x \odot$ and $y+1, \boxed{\odot}$) in order to denote two different arbitrary rules by which the expressions given in the left position are treated. The result is an expression. By this, the meaning is similar to writing $f(x)$ or $g(y+1)$ in modern mathematical notation with f and g denoting arbitrary functions.

In a similar way, Johann Bernoulli uses the sign ϕ (see L-2520) to denote a quantity depending on variables x and a (in modern terminology a function in x and a).

stantem numerum multiplicatam esse vel 1, vel multipulum facti ex denominatoribus duobus proximis, per numerum respondentem, ut 3. 35 etc. nempe:

Sunto duo termini: $\frac{b}{z \odot} \frac{b}{z+1, \odot}$ erit $b \frac{z+1, \odot, -z \odot}{z \odot, \wedge z+1, \odot} \sqcap \frac{1}{16z^2 - 16z + 3}$. Quod si nominator etiam sit inconstans, erunt termini $\frac{z \boxed{\odot}}{z \odot} \cdot \frac{z+\beta, \boxed{\odot}}{z+\beta, \odot}$ et fiet:

$$\frac{z+1, \odot, \wedge z \boxed{\odot}, -z \odot, \wedge z+\beta, \boxed{\odot}}{z \odot, \wedge z+\beta, \odot} \sqcap \frac{1}{16z^2 - 16z + 3}.$$

Certum est semper destrui omnia quae non ducuntur in β . Sed hanc aequationem

$\odot$ LEIBNIZIAN ENCIRCLED V, $\boxed{\odot}$ LEIBNIZIAN ENCIRCLED V IN BOX

LAA VII-1 p. 527 (above), LH 35 V 4, fol. 6 (below), LH 35 VIII 30, fol. 115r (bottom)

Investigamus paulo accuratius, post modum fieri possit, ut quicquid in differentibus dicitur aliter fiat.

Sic: $\frac{y \odot}{\boxed{\odot} y} - \frac{y+1, \odot}{y+1, \boxed{\odot}}$ unde $\frac{y \odot, y+1, \boxed{\odot} - y \boxed{\odot}, y+1, \odot}{\boxed{\odot} y, y+1, \boxed{\odot}}$

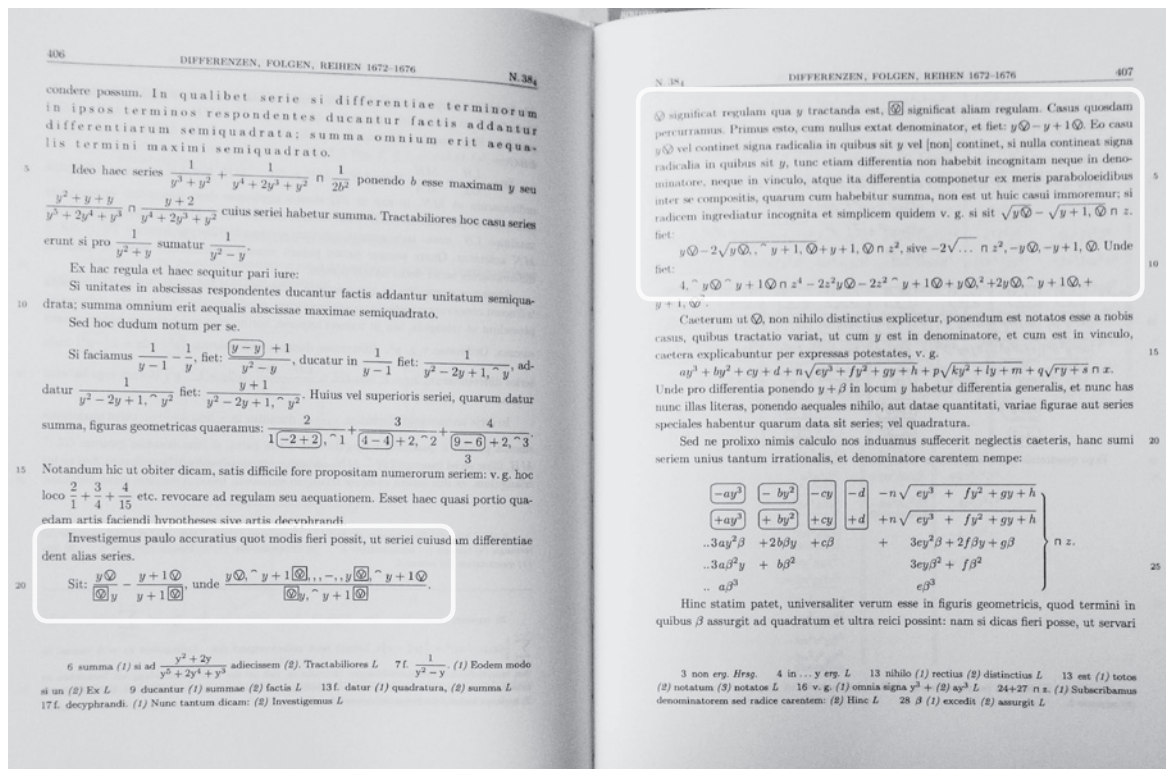
Observeat regulas quae y tractantur & $\boxed{\odot}$ significat aliam regulam. Cuius quidem periculum. primum quod nullus est denominator et fieri: $y \odot - y+1, \odot$. Et casu $y \odot$ vel continet signa radicalia in quibus y vel continet si nulla sit in casu signa radicalia tunc etiam differentia nulla est. unde habebit in denominatoribus, nec differentia componetur ex mensurabilibus.

vel multipulum facti ex denominatoribus duobus proximis, ut 3. 35 etc. nempe:

Sunto duo termini: $\frac{b}{2 \odot} \frac{b}{2+1, \odot}$ erit $b \frac{2+1, \odot, -2 \odot}{2 \odot, \wedge 2+1, \odot} \sqcap \frac{1}{16z^2 - 16z + 3}$

Composui, & erunt termini $\frac{2 \boxed{\odot}}{2 \odot} \cdot \frac{2+\beta, \boxed{\odot}}{2+\beta, \odot}$ et fiet: $\frac{2 \odot, \wedge 2+\beta, \boxed{\odot} - 2 \boxed{\odot}, \wedge 2+\beta, \odot}{2 \odot, \wedge 2+\beta, \odot} \sqcap \frac{1}{16z^2 - 16z + 3}$

Aequationem resolvere per hanc methodum est in potestate humana; sed quidem cum una methodo regeretur per diversa successat. Cumque fieri sit per methodum universalem ipse determinari non potest, quare ea est methodus in qua aequationes solvuntur per hanc methodum.



© LEIBNIZIAN ENCIRCLED V, ⊙ LEIBNIZIAN ENCIRCLED V IN BOX

The typographical solution of these characters in the edition is bad. In fact the round shape has to be connected with the v, similar as in @ (0040). – LAA VII-3 p. 406-407

Investigemus paulo accuratius quot modis fieri possit, ut seriei cuiusdam differentiae dent alias series.

$$\text{Sit: } \frac{y \odot}{\odot y} - \frac{y+1 \odot}{y+1 \odot}, \text{ unde } \frac{y \odot, \wedge y+1 \odot, , , -, , y \odot, \wedge y+1 \odot}{\odot y, \wedge y+1 \odot}.$$

$\odot$ significat regulam qua y tractanda est, $\odot$ significat aliam regulam. Casus quosdam percurramus. Primus esto, cum nullus extat denominator, et fiet: $y \odot - y + 1 \odot$. Eo casu $y \odot$ vel continet signa radicalia in quibus sit y vel [non] continet, si nulla contineat signa radicalia in quibus sit y , tunc etiam differentia non habebit incognitam neque in denominatore, neque in vinculo, atque ita differentia componetur ex meris paraboloeidibus inter se compositis, quarum cum habebitur summa, non est ut huic casui immoremur; si radicem ingrediatur incognita et simplicem quidem v. g. si sit $\sqrt{y \odot} - \sqrt{y+1, \odot} \cap z$. fiet:

$$y \odot - 2\sqrt{y \odot, \wedge y+1, \odot} + y+1, \odot \cap z^2, \text{ sive } -2\sqrt{\dots} \cap z^2, -y \odot, -y+1, \odot. \text{ Unde fiet:}$$

$$4, \wedge y \odot \wedge y+1 \odot \cap z^4 - 2z^2 y \odot - 2z^2 \wedge y+1 \odot + y \odot, ^2 + 2y \odot, \wedge y+1 \odot, + y+1, \odot^2.$$

Caeterum ut $\odot$, non nihilo distinctius explicetur, ponendum est notatos esse a nobis casus, quibus tractatio variat, ut cum y est in denominatore, et cum est in vinculo,

La Colonne C. du mesme feuillet, contient l'aplication que j'ay faite de la premiere
 15 analogie de M. Leibnits, en ne se servant que de la ligne interrompue -- pour designer
 le Zero; et de la ligne entiere — pour marquer Un. La continuation de cette colonne est
 de l'autre coté du mesme feuillet.

Les colonnes D. E. F. G. H. font connoitre les diverses combinaisons qui se forment,
 lors que la ligne interrompue -- et la ligne entiere — se trouvent une à une; ou jointes
 20 deux à deux; ou trois à trois; ou 4. à 4. ou 5. à 5.

Et enfin la colonne I. donne les 64. caracteres ou figures de Fo-hi, arrangez dans
 l'ordre qu'ils doivent estre suivant la seconde analogie de M. Leibnits, pour marquer la
 suite naturelle des nombres, depuis 0. jusques et compris 63. Mais par ce que depuis 31.
 les figures de cette Colonne I se raportent parfaitement au reste de ceux de la colonne C.
 25 je n'ay pas cru necessaire de les repeter.

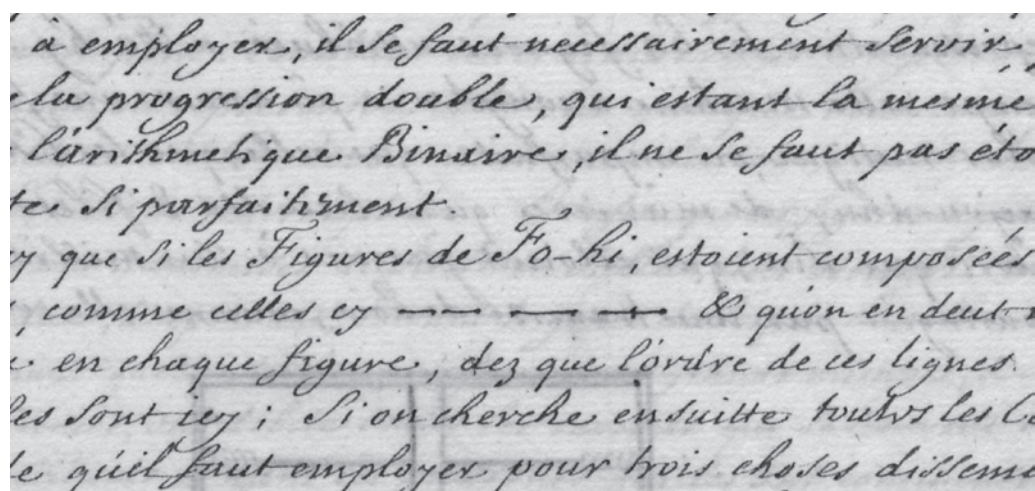
-- BROKEN EMDASH, +- CROSSED EMDASH

LAA III-9 p. 606 (top), p. 610 (below). In this example these two characters will be used alongside
 the existent EMDASH (2014) .

15 qui estant la mesme qu'il faut employer dans l'arithmetique Binaire, il ne se faut pas
 étonner que le tout se raporte si parfaitement.

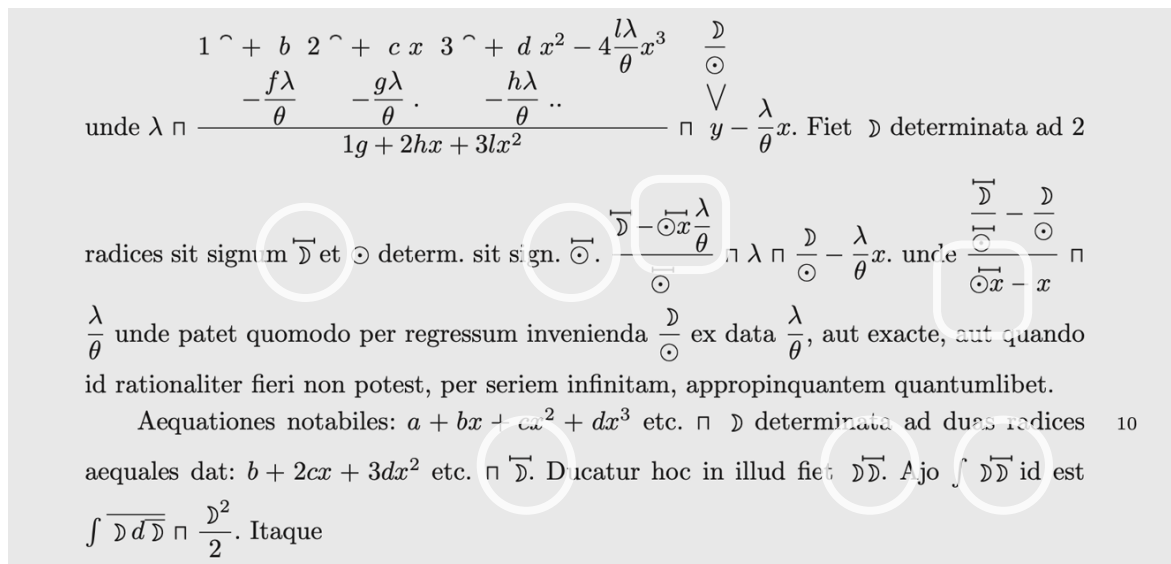
Cela est si vray que si les Figures de Fo-hi, estoient composées de trois sortes de
 Lignes, comme celles cy -- — +- et qu'on en deut mettre pareillement six en chaque
 figure, dez que l'ordre de ces lignes aura esté fixé comme elles sont icy; si on cherche
 20 ensuite toutes les Combinaisons selon la methode qu'il faut employer pour trois choses
 dissemblables, on trouvera 729 figures differentes de six lignes chacune; sans qu'il paroisse
 d'aucune necessité que cela se puisse raporter à aucune sorte d'arithmetique. Et cepen-
 dant si on se propose d'appliquer l'arithm. ternaire à ces trois sortes de lignes, et que la
 premiere interrompue -- designe le Zero. La suivante entiere — Un. Et la trois[i]esme
 25 croisée par le milieu +- deux, on trouvera en descendant de haut en bas, ou en remon-
 tant de bas en haut, que toute la suite des figures, donnera exactem^t toute la suite des
 nombres depuis 0. Jusques et compris 728.

Il n'est donc pas facile à mon sens de determiner certainement, si les 64 caracteres
 de Fo-hi, doivent estre regardez comme une simple Combinaison, ou comme une arith.
 30 binaire complete, puis qu'il y a un si parfait raport entre ces deux choses; sur tout si



-- BROKEN EMDASH, +- CROSSED EMDASH

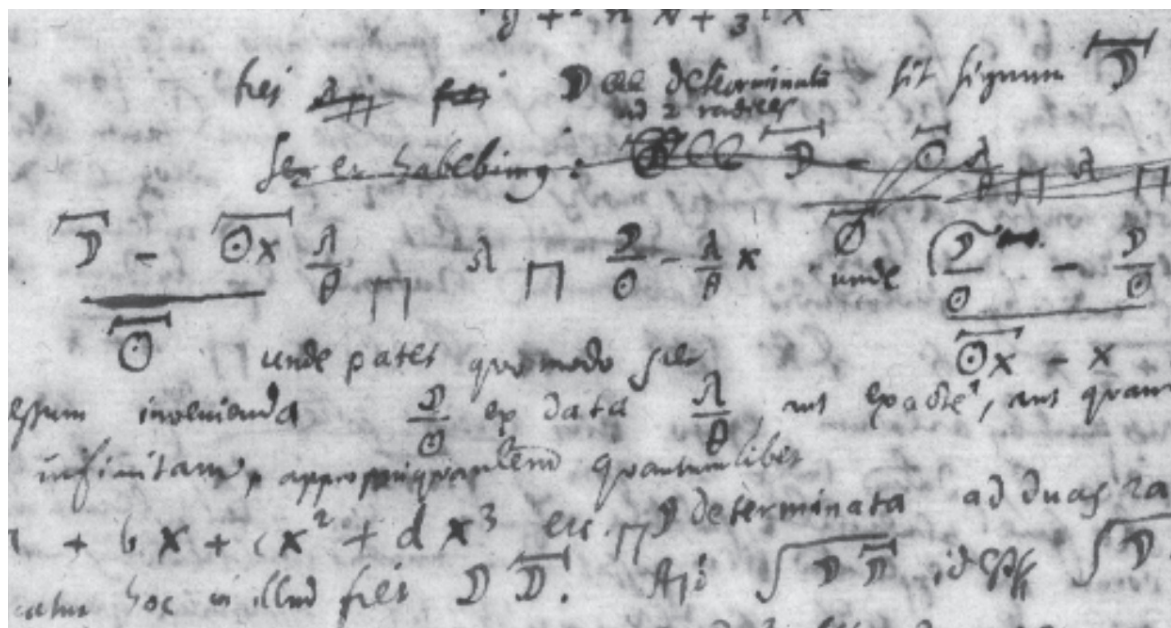
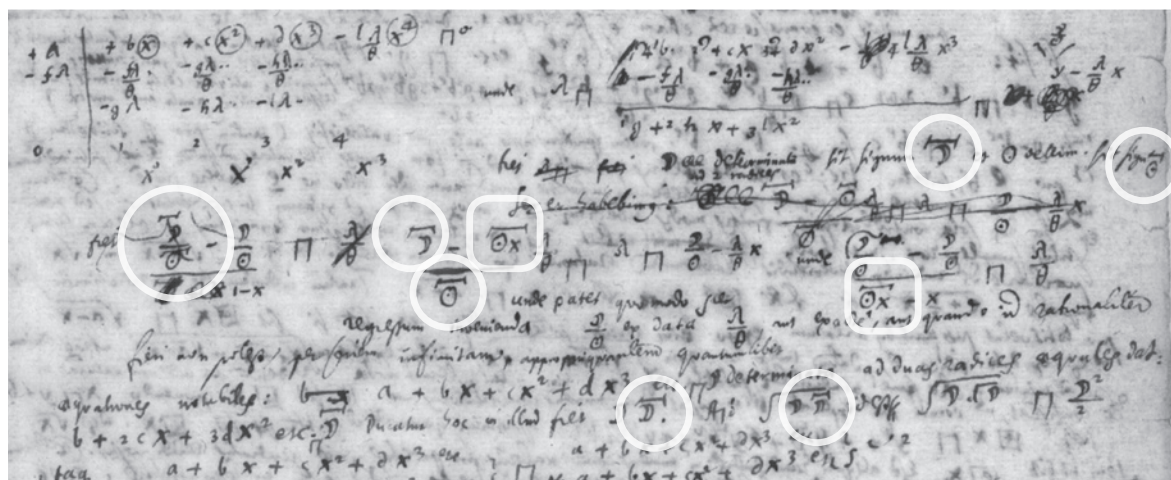
From a letter of César Caze to Leibniz (1699), LH 35 III B 7, fol. 4r

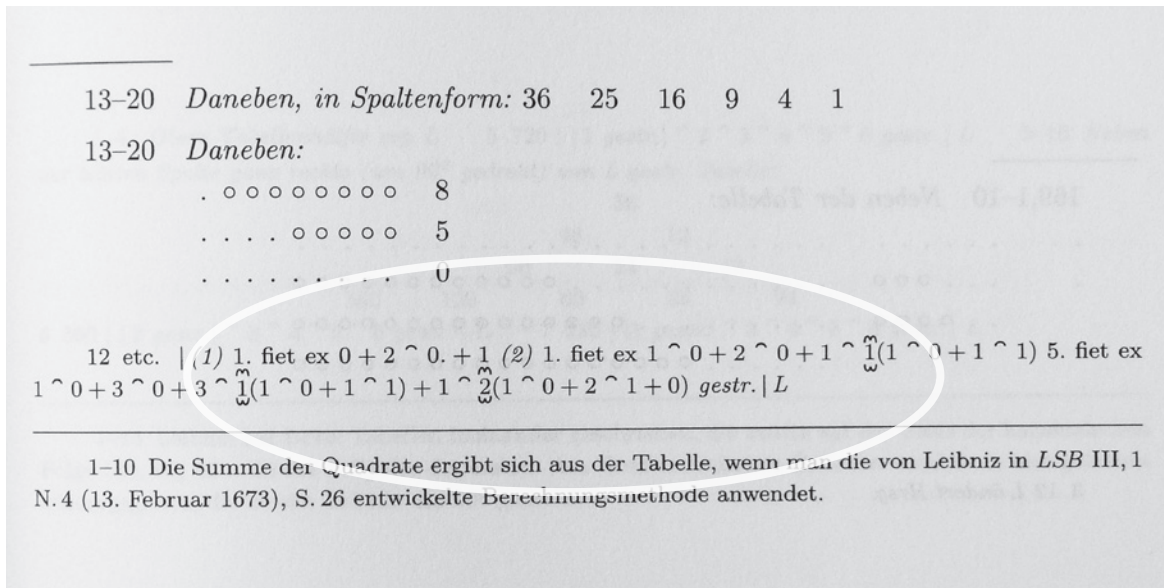


⏞ COMBINING OVERLINE WITH TERMINALS

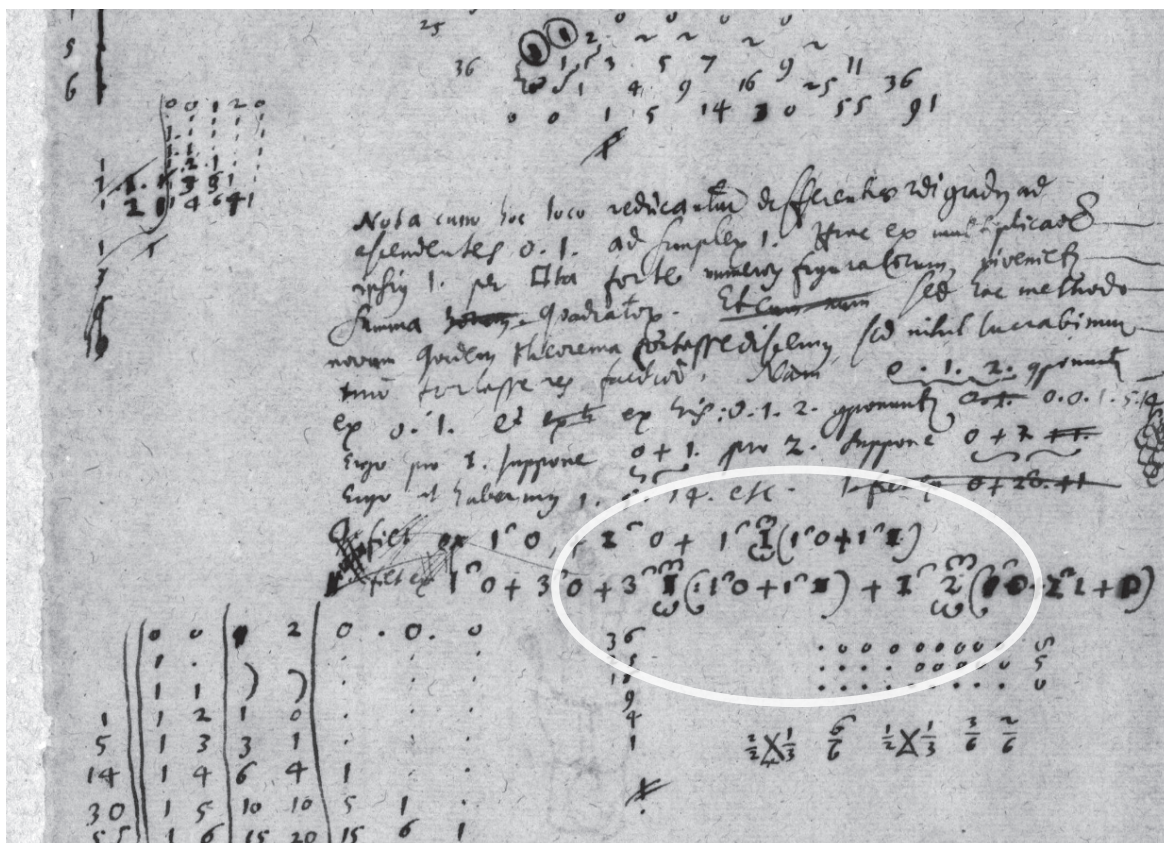
⏞ COMBINING DOUBLE-WIDE OVERLINE WITH TERMINALS

LAA VII-5 p. 587 (top); LH 35 XIII 1, fo. 446r (below)





COMBINING FACTOR MARK
LAA VII-3 p. 167



COMBINING FACTOR MARK
LH 35 XII 1, fol. 138r

Esto jam aequatio ad sectionem Conicam $y \sqcap \sqrt{2ax \mp \frac{r}{t}x^2} B$. Primum ponendo $x \sqcap v$ videamus quod eventurum sit, nam si res non succedit, valorem mutabimus: At y esto $\sqcap w + \varphi + k - \psi$. fietque $B + \psi \sqcap A$. et quadrando $B^2 + 2\psi B + \psi^2 \sqcap A^2$, unde ordinando:

$+1$	v^2	$-e$	v	$-\lambda^2$	$\sqcap$	$-2\psi B$.
$\mp \frac{r}{t}$		$-2h$		$-eh$		
$\odot$		$+2a$		$+h^2$		
		$\mathfrak{D}$		$+2\varphi k$		
				$+k^2$		
				$+\psi^2$		
				$\mathfrak{F}$		

et rursus quadrando atque ordinando

$$\odot^2 v^4 + 2\odot \mathfrak{D} v^3 + 2\odot \mathfrak{F} v^2 [+] 2 \mathfrak{D} \mathfrak{F} v + \mathfrak{F}^2 \sqcap 0.$$

$$+ \mathfrak{D}^2 \dots - 8\psi^2 a \dots$$

$$\pm 4\psi^2 \frac{r}{t} \dots$$

$\odot$ COMBINING HORIZONTAL PARANTHESIS
LAA VII-7 p. 329

Esto jam aequatio ad sectionem Conicam $y \sqcap \sqrt{2ax \mp \frac{r}{t}x^2} B$. Primum ponendo $x \sqcap v$ videamus quod eventurum sit, nam si res non succedit, valorem mutabimus: At y esto $\sqcap w + \varphi + k - \psi$. fietque $B + \psi \sqcap A$. et quadrando $B^2 + 2\psi B + \psi^2 \sqcap A^2$, unde ordinando:

$+1$	v^2	$-e$	v	$-\lambda^2$	$\sqcap$	$-2\psi B$.
$\mp \frac{r}{t}$		$-2h$		$-eh$		
$\odot$		$+2a$		$+h^2$		
		$\mathfrak{D}$		$+2\varphi k$		
				$+k^2$		
				$+\psi^2$		
				$\mathfrak{F}$		

et rursus quadrando atque ordinando

$$\odot^2 v^4 + 2\odot \mathfrak{D} v^3 + 2\odot \mathfrak{F} v^2 [+] 2 \mathfrak{D} \mathfrak{F} v + \mathfrak{F}^2 \sqcap 0.$$

$$+ \mathfrak{D}^2 \dots - 8\psi^2 a \dots$$

$$\pm 4\psi^2 \frac{r}{t} \dots$$

conferatur cum data

$$\odot^2 v^4 + \odot \mathfrak{D} v^3 + \odot \mathfrak{D} \mathfrak{D} v^2 + \odot \mathfrak{D} \mathfrak{F} v + \odot \mathfrak{F}^2 \sqcap 0.$$

unde patet, habetur $\mathfrak{F} \sqcap \odot \mathfrak{D} \mathfrak{F}$. et $\mathfrak{D} \mathfrak{D} \sqcap \odot \mathfrak{D}$ et $\mathfrak{F} \sqcap \sqrt{\mathfrak{F}^2 - \odot \mathfrak{D} \mathfrak{D}}$

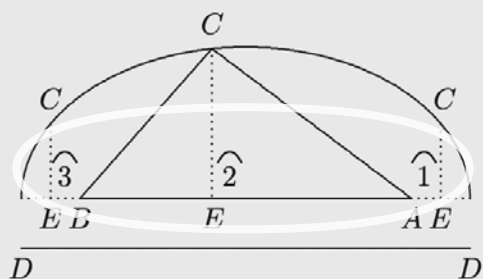
unde ipse ψ valor adhuc finel habetur ex aequatione ista quod sa abundu.

unde rei facile remedium habebimus si cum parabola tantum unum, de offes

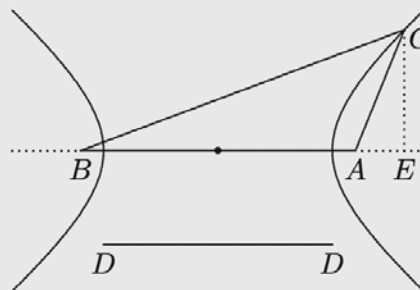
$\odot$ COMBINING HORIZONTAL PARANTHESIS
LH 35 I 17, fol. 5v

Schediasma de Focis Conicarum, Octob. 1674

Invenire locum, unde ductae ad data duo puncta rectae datam faciant summam, aut dato differant intervallo. Quod ita reperiemus:



[Fig. 1]

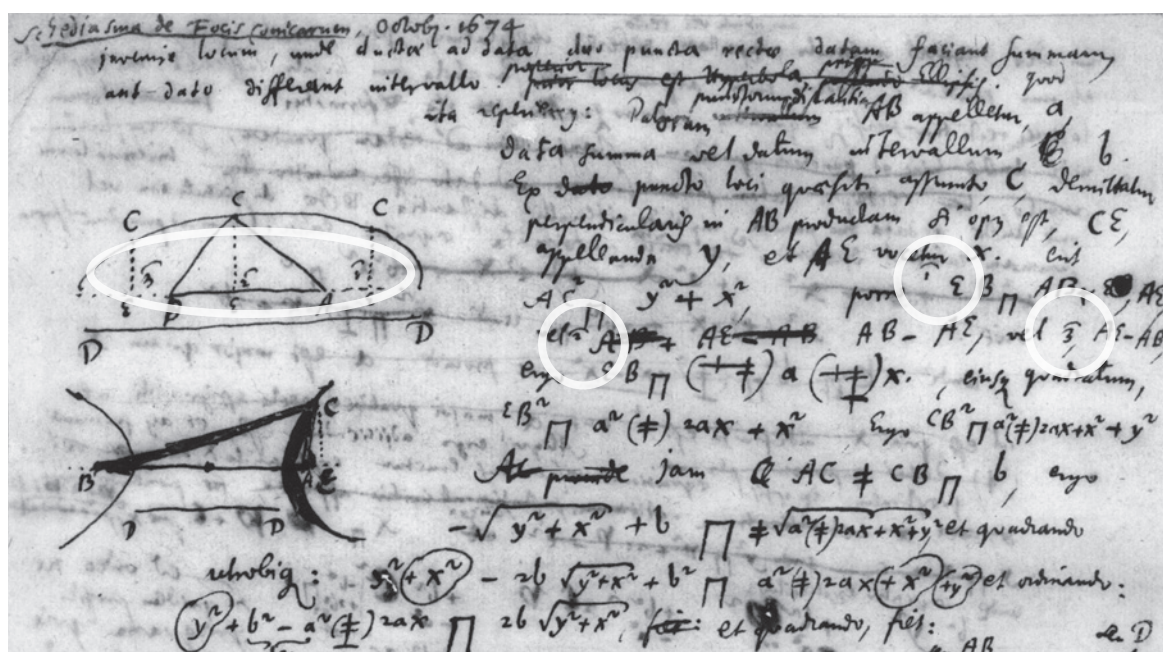


[Fig. 2]

Datorum punctorum distantia AB appelletur, a , data summa vel datum intervallum, b . Ex puncto loci quaesiti assumpto, C , demittatur perpendicularis in AB productam si opus est. CE , appellanda y , et AE vocetur x . Erit $AC^2 \sqcap y^2 + x^2$, porro $\widehat{1} EB \sqcap AB + AE$, vel $\widehat{2} AE - AE$, vel $\widehat{3} AE - AB$, ergo $EB \sqcap (\dagger)a(\dagger)x$, ejusque quadratum, $EB^2 \sqcap$

COMBINING HORIZONTAL PARANTHESIS

LAA VII-7 p. 357 – The glyphs applied in those two samples are not ideal.



COMBINING HORIZONTAL PARANTHESIS

LH 35 XII 1, fol. 280r

z terminus primus. $z - a$ terminus 2^{us}. $z - a - b$ terminus tertius. $z = \frac{c}{d}$. $z - a = \frac{c}{d+e}$. $z - a - b = \frac{c}{d+e+f}$. Ergo $\frac{c}{d} - \frac{c}{d+e} = a$. $\frac{c}{d} \times \frac{c}{d+e} [=] \frac{cd+ce-ed}{dd+de}$. Ergo
 $a = \frac{ce}{dd+de}$. $b = \frac{c}{d+e} \times \frac{c}{d+e+f} = \frac{cd+ce+cf-ed-ee}{(d+e)(dd+ee+2de+df+ef)} = b$.
 $\frac{c}{dd+de} \times \frac{c}{d+e+Q+df+ef} = \frac{c}{d} \times \frac{c}{d+e+f}$. $\frac{d+e+f}{d} = \frac{d+e+Q+df+ef}{ddf}$.

✂ COMBINING DOUBLE-WIDE SLASH

This character is similar to COMBINING LONG SOLIDUS OVERLAY (0338). Its function is to create a strike-through mark for *two* neighbouring base characters, so it is supposed to work in the same way as e.g. the characters 035C to 0362.

LAA VII-3 p.122

[Teil 1]

Fig. 3.

$$AN = AE = AK$$

$$AI = ID = IG = A\beta = \gamma M = \frac{AG}{2} \text{ modo } \beta \text{ sit in linea } DE.$$

$$IB = AZ = B\gamma = \gamma\delta = \frac{CG}{2} = ZG$$

$$BI = AZ \quad B\alpha = BE \quad \beta\alpha = \beta E \quad A\beta = D\beta$$

NB. recta $A\alpha$ non incidit in rectam AZ .

✂ COMBINING DOUBLE-WIDE SLASH

LAA VII-4 p. 409

5. Unicode Character Properties

xf01;CASTING-OUT-NINES;Sm;0;ON;;;;N;;;;;
xf02;LUNATE ENCIRCLED DIGIT ONE;Sm;0;ON;;;;N;;;;;
xf03;PROPORTION WITH ONE STROKE;Sm;0;ON;;;;N;;;;;
xf04;PROPORTION WITH TWO STROKES;Sm;0;ON;;;;N;;;;;
xf05;INFINITY WITH TWO DOTS;Sm;0;ON;;;;N;;;;;
xf06;INVOLVED;Sm;0;ON;;;;N;;;;;
xf07;LEIBNIZIAN ENCIRCLED V;Sm;0;ON;;;;N;;;;;
xf08;LEIBNIZIAN ENCIRCLED V IN BOX;Sm;0;ON;;;;N;;;;;
xf09;BROKEN EMDASH;So;0;ON;;;;N;;;;;
xf10;CROSSED EMDASH;So;0;ON;;;;N;;;;;
xf11;SUPERSCRIT WAVE SYMBOL;Sm;0;ON;;;;N;;;;;
xf12;SUPERSCRIT WAVE WITH OVERLINE SYMBOL;Sm;0;ON;;;;N;;;;;
xf13;COMBINING BOMBELLI POWER MARK;Mn;220;NSM;;;;N;;;;;
xf14;COMBINING DOUBLE-WIDE SLASH;Mn;1;NSM;;;;N;;;;;
xf15;COMBINING HALF CIRCLE BELOW;Mn;220;NSM;;;;N;;;;;
xf16;COMBINING ENCLOSING SPIRAL MARK;Mn;1;NSM;;;;N;;;;;
xf17;COMBINING DOUBLE-WIDE ENCLOSING SPIRAL MARK;Mn;1;NSM;;;;N;;;;;
xf18;COMBINING FACTOR MARK;Mn;1;NSM;;;;N;;;;;
xf19;COMBINING OVERLINE WITH TERMINALS;Mn;230;NSM;;;;N;;;;;
xf20;COMBINING DOUBLE-WIDE OVERLINE WITH TERMINALS;Mn;234;NSM;;;;N;;;;;
xf21;COMBINING HORIZONTAL PARANTHESIS;Mn;230;NSM;;;;N;;;;;

6. Bibliography

LAA – refers to: Leibniz, Gottfried Wilhelm: Sämtliche Schriften und Briefe. (‘Leibniz-Akademie-Ausgabe’, many volumes)

LH – refers to: Leibniz’s original manuscripts, GWLB Hanover

Bombelli, Rafael: L’Algebra. Bologna 1579

— : L’Algebra. Milan 1966

Cajori, Florian: A history of mathematical notations. Chicago 1928

Probst, Siegmund: Édition des symboles de Leibniz. PDF. Hanover 2023 (presentation Paris 2023)

Rahn, Johann Heinrich: Teutsche Algebra. Zurich 1659

Rinner, Elisabeth: List of glyphs in Leib.mf. PDF. Hanover 2022

**ISO/IEC JTC 1/SC 2/WG 2
PROPOSAL SUMMARY FORM TO ACCOMPANY SUBMISSIONS
FOR ADDITIONS TO THE REPERTOIRE OF ISO/IEC 10646¹**

Please fill all the sections A, B and C below.

Please read Principles and Procedures Document (P & P) from <http://std.dkuug.dk/JTC1/SC2/WG2/docs/principles.html> for guidelines and details before filling this form.

Please ensure you are using the latest Form from <http://std.dkuug.dk/JTC1/SC2/WG2/docs/summaryform.html>.

See also <http://std.dkuug.dk/JTC1/SC2/WG2/docs/roadmaps.html> for latest *Roadmaps*.

A. Administrative

1. Title:	Proposal to encode 21 miscellaneous scientific symbols		
2. Requester's name:	Uwe Mayer, Siegmund Probst, David Rabouin, Elisabeth Rinner, Andreas Stötzner, Achim Trunk, Charlotte Wahl		
3. Requester type (Member body/Liaison/Individual contribution):	Individual (work group)		
4. Submission date:	2025-05-30		
5. Requester's reference (if applicable):	LUCPL-2521		
6. Choose one of the following:			
This is a complete proposal:			Yes
(or) More information will be provided later:			

B. Technical – General

1. Choose one of the following:			
a. This proposal is for a new script (set of characters):			No
Proposed name of script:			
b. The proposal is for addition of character(s) to an existing block:			No
Name of the existing block:			
2. Number of characters in proposal:			21
3. Proposed category (select one from below - see section 2.2 of P&P document):			
A-Contemporary	B.1-Specialized (small collection)	Yes	B.2-Specialized (large collection)
C-Major extinct	D-Attested extinct		E-Minor extinct
F-Archaic Hieroglyphic or Ideographic			G-Obscure or questionable usage symbols
4. Is a repertoire including character names provided?			Yes
a. If YES, are the names in accordance with the "character naming guidelines" in Annex L of P&P document?			Yes
b. Are the character shapes attached in a legible form suitable for review?			Yes
5. Fonts related:			
a. Who will provide the appropriate computerized font to the Project Editor of 10646 for publishing the standard?	Andreas Stötzner		
b. Identify the party granting a license for use of the font by the editors (include address, e-mail, ftp-site, etc.):	Andreas Stötzner Gestaltung, Klaufügelweg 21, 88400 Biberach/R., Germany, as@signographie.de		
6. References:			
a. Are references (to other character sets, dictionaries, descriptive texts etc.) provided?			Yes
b. Are published examples of use (such as samples from newspapers, magazines, or other sources) of proposed characters attached?			Yes
7. Special encoding issues:			
Does the proposal address other aspects of character data processing (if applicable) such as input, presentation, sorting, searching, indexing, transliteration etc. (if yes please enclose information)?			No

8. Additional Information:

Submitters are invited to provide any additional information about Properties of the proposed Character(s) or Script that will assist in correct understanding of and correct linguistic processing of the proposed character(s) or script. Examples of such properties are: Casing information, Numeric information, Currency information, Display behaviour information such as line breaks, widths etc., Combining behaviour, Spacing behaviour, Directional behaviour, Default Collation behaviour, relevance in Mark Up contexts, Compatibility equivalence and other Unicode normalization related information. See the Unicode standard at <http://www.unicode.org> for such information on other scripts. Also see Unicode Character Database (<http://www.unicode.org/reports/tr44/>) and associated Unicode Technical Reports for information needed for consideration by the Unicode Technical Committee for inclusion in the Unicode Standard.

¹ Form number: N4502-F (Original 1994-10-14; Revised 1995-01, 1995-04, 1996-04, 1996-08, 1999-03, 2001-05, 2001-09, 2003-11, 2005-01, 2005-09, 2005-10, 2007-03, 2008-05, 2009-11, 2011-03, 2012-01)

C. Technical - Justification

1. Has this proposal for addition of character(s) been submitted before?	Yes
If YES explain <i>see N5277 (L-2402n)</i>	
2. Has contact been made to members of the user community (for example: National Body, user groups of the script or characters, other experts, etc.)?	Yes
If YES, with whom?	
Leibniz-Archiv, Forschungsstelle der Leibniz-Edition, Niedersächsische Landesbibliothek (GWLb), Hanover, Göttingen Academy of Science and Humanities in Lower Saxony (DE), Philiumm research group of CNRS (UMR 7219, laboratoire SPHERE) / Université de Paris VII; general: scholars, researchers, authors and editors working in the field of science history and upon editions of historic text corpora (e.g. of G. W. Leibniz, but also many others)	
If YES, available relevant documents: L-2409, L-2410	
3. Information on the user community for the proposed characters (for example: size, demographics, information technology use, or publishing use) is included?	Yes
Reference:	
4. The context of use for the proposed characters (type of use; common or rare)	Common
Reference: mainly specialist usage, scholarly, worldwide	
5. Are the proposed characters in current use by the user community?	Yes
If YES, where? Reference: mainly Europe, Americas; other countries	
6. After giving due considerations to the principles in the P&P document must the proposed characters be entirely in the BMP?	No
If YES, is a rationale provided?	
If YES, reference:	
7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)?	No
8. Can any of the proposed characters be considered a presentation form of an existing character or character sequence?	No
If YES, is a rationale for its inclusion provided?	
If YES, reference:	
9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?	No
If YES, is a rationale for its inclusion provided?	
If YES, reference:	
10. Can any of the proposed character(s) be considered to be similar (in appearance or function) to, or could be confused with, an existing character?	No
If YES, is a rationale for its inclusion provided?	
If YES, reference:	
11. Does the proposal include use of combining characters and/or use of composite sequences?	Yes
If YES, is a rationale for such use provided?	
If YES, reference: <i>see explanations</i>	
Is a list of composite sequences and their corresponding glyph images (graphic symbols) provided?	
If YES, reference:	
12. Does the proposal contain characters with any special properties such as control function or similar semantics?	No
If YES, describe in detail (include attachment if necessary)	
13. Does the proposal contain any Ideographic compatibility characters?	No
If YES, are the equivalent corresponding unified ideographic characters identified?	
If YES, reference:	