

Universal Multiple-Octet Coded Character Set
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Title: Proposal to encode 12 cossic characters

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Version: 5th revised version

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Related: Commentary doc.s L2/25-232; L-2506, L-2512

Status: final

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Requester's reference: LUCP L-2533

1.a The 5th revision of the Cossic proposal

We defined updated Unicode Character Properties for the two */s* characters, according to the recommendation we received after the discussion on October 2. According to **L2/25-232** we added provisional codepoints and made some changes to character names. The cossic characters are to be allocated in the Latin Ext. G block, the Miscellaneous Symbols Supplement block and one in the Mathematical Alphanumeric Symbols block.

1.b The 4th revision of the Cossic proposal

There is one minor change and one significant change in this proposal, regarding the previous version. The minor thing is: with regard to LOWERCASE KURRENT Z as a variation sequence of 1D4CF, we now reference an analogue case presented in our proposal L-2520 (N5335), the two instances of the same sort of character may strengthen the case pro encoding.

A significant change has been made to the character names of three root characters, according to a recommendation we received from the UTC the names now reflect their historic nomenclature more directly.

2. About Coss or cossic characters

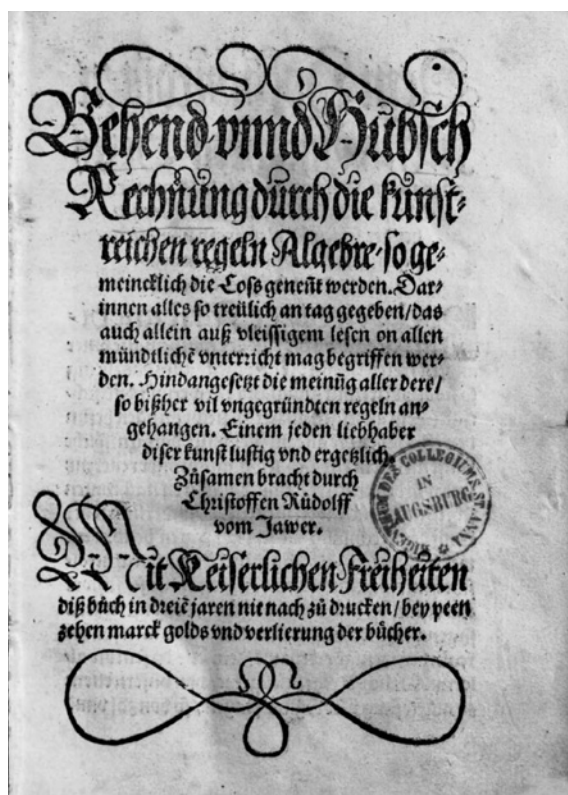
“Coss” (or “Cofs”, historic) is a German term for written or printed treatises about Algebra.

It derives from Italian *cosa* (“thing”) which was used to denote variables in calculations.

The first printed “Coss” was a book by German mathematician Christoff Rudolff (ca. 1500 – before 1543): *Behend und hübsch Rechnung durch die kunstreichen regeln Algebre, so gemeincklich die Cofs geneñt werden*. (“Handy and neat calculation by the artful Algebre rules, commonly so called the Coss.”) The work was based on older algebra manuscripts which the author studied

in Vienna. The book was released in Straßburg in 1525 and was out of stock soon. Because it was such a sought-after title, Michael Stifel edited a new and extended version of Rudolff's Coss in 1553.

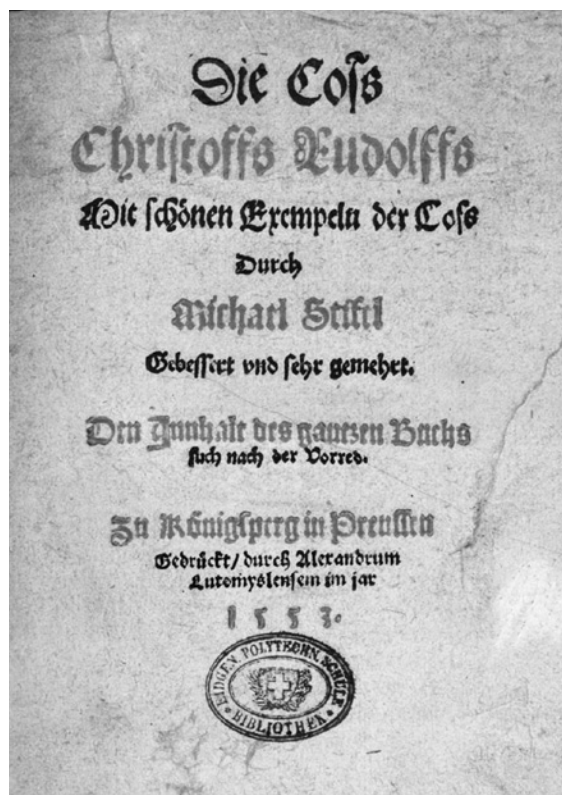
In the 1525 edition the character " $\sqrt{\quad}$ " was used the first time for *radix* in print. For the expression of powers (up to ninth) Rudolff used a set of special abbreviation characters. Some of them were common in writing at the time (and used for different purposes), some were rather special additions. Since this set of cossic characters appears explicitly for a longer time in mathematical literature, we see a need to have them encoded, in order to enable precise content encoding in facsimile transcriptions of the historic sources.



Title page of Rudolff's *Coss*, edited in Straßburg 1525.

Source:

Münchner Digitalisierungszentrum



Title page of Stifel's new edition of Rudolff's *Coss*, printed in Königsberg 1553.

Source:

ETH Zurich

3. Characters


The cossic characters set consists of two sub-groups. Group 1 is a range of 8 Latin abbreviation characters, derivatives from Latin letters c, d, r, f and z. They represent the initials of the names of roots or powers. These characters are comparable to other already encoded abbreviation characters, like lb (*libra*, 2114), p (*per*, 214C), ſ (*denarius/penny*, 20B0), p (*prae-*, A755) or z (*-rum*, A75D) which show a combination of a modified basic shape with some sort of graphic attachment, like scriptive loops directly connected to or crossing the base glyph.


We propose to encode the characters as *mathematical symbols*. In one case it has been worked out that a double encoding is required: one mathematical symbol character and one as a Latin letter character.


The aspect of case pairing is not relevant in all of the cases since no capital variants of these characters have ever been used anywhere. “Lowercase” in the proposed character names is chosen merely to indicate the proper respective ‘parent’ characters. The cossic characters do not occur as abbreviations in general Latin writing but exclusively in calculation contexts. Hence their specific shapes in combination with very specific meaning should justify their encoding, even if an apparent close optical ‘neighbourhood’ to existing characters can be observed. The proposed annotations will help to understand differences to and similarities with existing characters.

If this proposal gets accepted, the following new characters will exist:

- 1DF90 c LATIN LETTER SMALL C WITH SMALL SLASH
= cubus
• denotes cube of the unknown
- 1DF91 c LATIN LETTER SMALL C WITH DESCENDER
= census
• denotes square of the unknown
- 1DF92 c LATIN LETTER SMALL C WITH RIGHT LOOP
= cubus
• denotes cube of the unknown
- 1DF93 d LATIN LETTER SMALL D ROTUNDA WITH CROSSING LOOP
= dragma
• denotes numerus / constant
→ 1E9F d latin small letter delta
→ A77A d latin small letter insular d
→ 20B0 ſ german penny sign
- 1DF94 r LATIN LETTER SMALL R ROTUNDA WITH LOOP
= res, radix
• denotes the unknown
→ A75D r latin small letter r rotunda
→ A75D z latin small letter rum rotunda
→ A776 R latin letter small capital rum
→ 221A $\sqrt{}$ square root

1DF95  LATIN SMALL LIGATURE LONG S WITH DESCENDER S
 = sursolidum
 • denotes fifth power of the unknown in historical mathematics
 • glyph always resembles long s and s
 → 017F *ſ* latin small letter long s
 → 0073 *s* latin small letter s
 → 00DF *ß* latin small letter sharp s
 → A7D7 *ſ* latin small letter middle scots s

1DF96  LATIN LETTER SMALL LONG S WITH TOP LOOP
 = sursolidum
 • denotes fifth power of the unknown in historical mathematics
 → 017F *ſ* latin small letter long s
 → 1E9C *ſ* latin small letter long s with diagonal stroke
 → 1E9D *ſ* latin small letter long s with high stroke
 → 1DF95 latin small ligature long s with descender s

1D6A6  MATHEMATICAL ITALIC LIGATURE LONG S WITH DESCENDER S
 = sursolidum
 • denotes fifth power of the unknown in historical mathematics
 • glyph always resembles long s and s
 • in plain text the corresponding Latin letter 1DF95 is preferred


Group 2 is a set of three *root* or *radix* symbols, historically related to the $\sqrt{\quad}$ character (221A). The character names have now been defined according to the historic names in Stevin 1634 (see p. 18):

1CEDD  SQUARE ROOT OF SQUARE ROOT
 → 221A $\sqrt{\quad}$ square root

1CEDE  SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT
 → 221A $\sqrt{\quad}$ square root

1CEDF  SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT
 → 221A $\sqrt{\quad}$ square root

This character is proposed as a variation sequence:

 (LOWERCASE KURRENT Z) *variation sequence to U+1D4CF*

This variation sequence character would introduce a new category of variation sequences related to the Mathematical Alphanumerics (block 1D500) subgroup *Script symbols* (lowercase, 1D4B6 to 1D4CF). There has been a concern whether this single char. should justify such a new series of variation sequence characters. For to justify such a decision it may be considered that in our proposal N5335 another character of this kind is proposed:

 LOWERCASE KURRENT X

This may well be regarded as a case of the same kind and dealt with in the same way. Further examples of the use of other *kurrent style* small letters in mathematical notation may be testified in the future.

4. The *cubus* characters

In group 1 there are two different characters for “cubus”: Ꞑ and ꞑ. Although the meaning is the same, the representative glyphs differ considerably. These typographic differences are strongly tied to certain writing or publishing traditions. Therefore we propose to encode two characters, thus being in line with a principle which has been followed in e.g. the alchemical characters block, where also (in some cases) two or three different characters bear (basically) the same meaning. This character pair situation is also evident with some other characters of the cossic set.

5. *Radix* characters

The LOWERCASE R ROTUNDA WITH LOOP ꝛ occurs frequently with the meaning of “res” or “radix”. The left part of the glyph is derived from the shape of the capital R, in a similar way as the base parts of the R ROTUNDA and RUM ROTUNDA characters (A75A to A75D) are derived from R. The distinctive feature of ꝛ is its right half with a prominent crossing loop moving down as a descender. In this form, the character unambiguously denotes the mathematical meaning in contrast to the syllabic meaning “-rum” of A75C/A75D as well as of A776.

But, as the sources show, the small capital R with stroke ꝛ (A776, LATIN SMALL CAPITAL RUM) has also been used eventually in the set of cossic characters. Therefore we also propose an addition of new annotations to this character, as follows:

A776 ꝛ LATIN LETTER SMALL CAPITAL RUM

- cossic sign for res, radix
- A75D ꝛ latin small letter rum rotunda
- [xi05] ꝛ lowercase r rotunda with loop

6. *Sursolidum* characters

“Sursolidum” is also represented by two different characters: ꝥ and Ꝧ. This dual track situation has evolved historically by different local notation traditions. On the one hand, in an edition of historic sources it would not be tolerable to encode e.g. ꝥ (or even ꝥ, 00DF) instead of Ꝧ.

In recent discussions a variety of character names for ꝥ have been considered:

MATHEMATICAL ITALIC SHARP S

SHARP S WITH HOOK

MATHEMATICAL SHARP S

SHARP S WITH DESCENDER

The background for a decision about the name has changed for two reasons: a) *two* characters are proposed now instead of one; b) a further evaluation has revealed that a definition containing the part ‘SHARP S’ would give a wrong interpretation of the character’s nature, identity and use. A detailed discussion of this matter is to be found in the appendix at the end of this document.

Following a suggestion made by A. Freytag, we propose the names:

LATIN SMALL LIGATURE LONG S WITH DESCENDER S

MATHEMATICAL ITALIC LIGATURE LONG S WITH DESCENDER S

By this naming we achieve:

- compliance with established UCS naming conventions
- a structural and historical correct explanation

- a clearly understandable definition of the characters nature
- correct naming of the character's base characters
- to avoid confusion with the German ß (SHARP S)
- maintain the distinction between a plain-text character and a specific math character
- allow a different treatment of (xi07) and (xi06) in an Italic font,
if there should be any need for that
- leave the door open for a possible later request for a *mathematical sharp s* (without a descender)

7. *Census* characters

There are also two different characters for “census/zensus”: \mathfrak{c} and \mathfrak{z} , related either to *c* or to *z*.

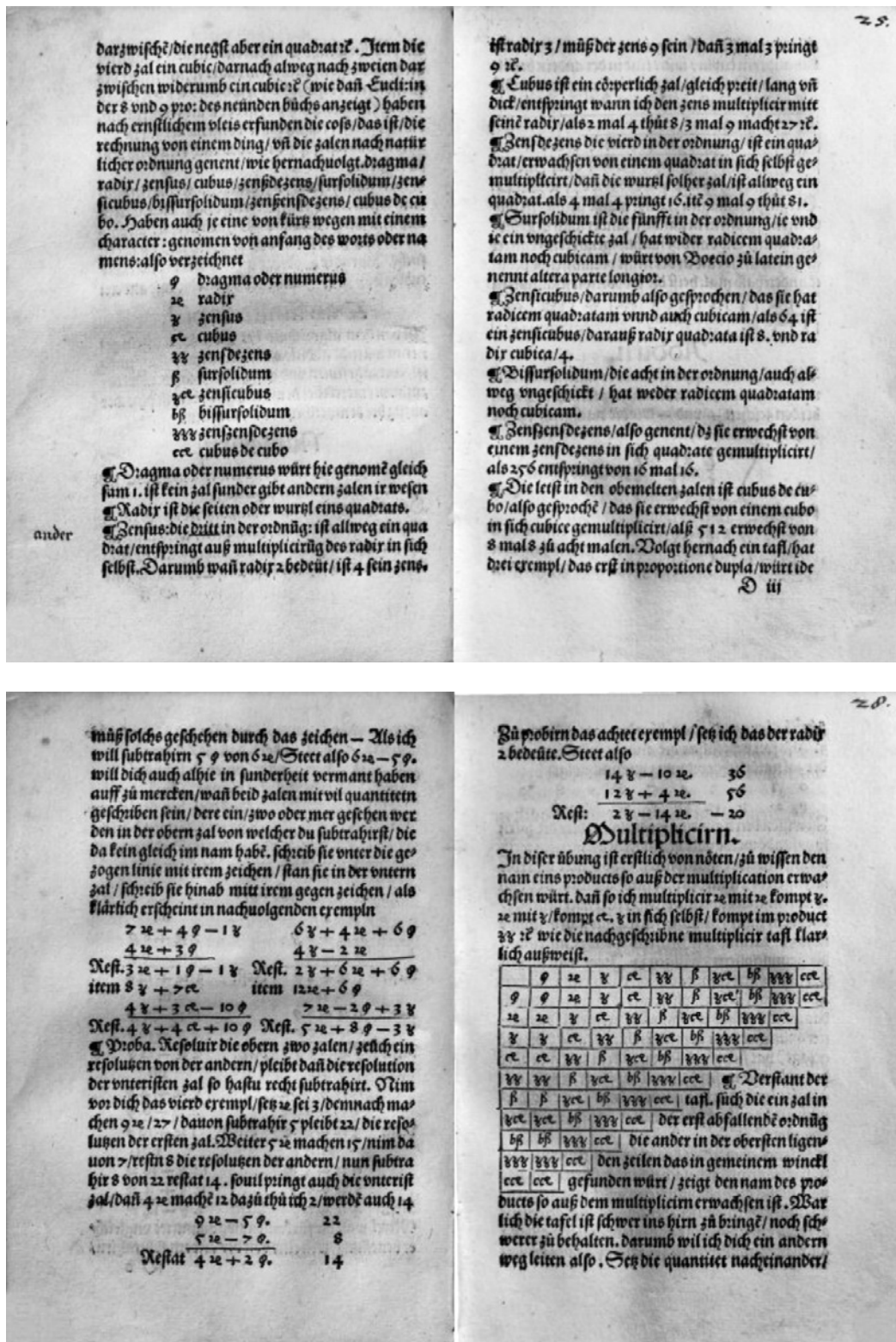
We propose LOWERCASE KURRENT Z as a new variation sequence on U+1D4CF.

Since \mathfrak{c} and \mathfrak{z} are derivatives of two different base letters, \mathfrak{c} is proposed separately.

8. Figures and further explanations

The *Coss* characters became a widely adopted set of characters for denoting powers and roots, in the 16th and 17th century. We show a couple of instances from printed sources and also a piece of manuscript evidence by Leibniz.

See page 19 for a synopsis of all characters belonging to the first group.



Christoff Rudolff: *Behend und hübsch Rechnung durch die kunstreichen regeln Algebre*, so gemeinlich die *Coss* genennt werden. Straßburg 1525. fol. 24v-25r, 27v-28r.

resolution der vnteristen zal / so hastu recht gemul-
tiplicirt. Als ich wil probirn dz drit exempl / setze den
werdt radialis 5. demnach würt die erst der obern:
nemlich 6 2e + 8 9: resoluirt in 38. die ander in 18 /
multiplicir 38 mit 18 komen 684. souil bedüt auch
das facit / daß 30 8 machen 750 / dauon subtrahir
10 / als den werdt 222 / mer subtrahir 56 / bleiben 684
hab ich wellen probiren.

Diuidirn.

Wan du hast diuidirt die grösser quantitet durch
die kleiner / wilt wissen den nam des quocients / Bee
in die nachuolgedt rasi / süch die grösser quantitet in
der obern / die kleiner in der vntern übereck hengen
den zeilen so würt dir in gemeinem winkel der nam
des quocients angezeigt.

9	2e	8	ce	38	β	3ce	68	388	ce
9	9	2e	8	ce	38	β	3ce	68	388
	2e	9	2e	8	ce	38	β	3ce	68
		8	9	2e	8	ce	38	β	3ce
			ce	9	2e	8	ce	38	β
				38	9	2e	8	ce	38
					β	9	2e	8	ce
						3ce	9	2e	8
							68	9	2e
								388	9
									ce

30.
Wan ein quantitet würt geteilt durch ein andere in
im namen gleich / kompt alweg 9 im quociens. würt
ein quantitet durch 9 geteilt / so kompt solch quanti-
tet im quociens. daß 9 verändert keine quantitet wi-
der im multiplicirn nach diuidirn.

Ein ander weiß / den nam des quocients zu süchē
wan die grösser geteilt würt durch ein kleinere oder
gleiche quantitet.

Schreib die quantitet nacheinander vñ verzeichē
sie mit der zal natürlicher ordnung / wie du im mul-
tiplicirn gelernt hast also.

0 1 2 3 4 5 6 7 8 9
9 2e 8 ce 38 β 3ce 68 388 ce

Subtrahir die zal der kleinern von der zal der gröf-
fern quantitet / durch dz übrig würt fundet der nam
des quocients. Als ich diuidir 8 durch ce / subtrahir
3 von 5 resten 2 / zeigt das der quociens sei 2. Item
ich diuidir 3et durch β / subtrahir 5 von 6 restat 1 /
zeigt im quociens 2e. Item ich diuidir ce durch ce /
subtrahir 3 von 3 restat 0 / zeigt 9. Des zu merern
verstandi nim dise exempl. Ich diuidir 6 8 durch 2
22 Stet also.

6 8 (fa: 32e. Item 5 ce (fa: 2 1/2. Item 12 8 (fa: 4 9
22e 22e 38

Proba. Resoluir beide zalen. Diuidir ein resolu-
ren durch die ander / das auß solcher teilung komen
würdt / müß gleich sein des quocients resoluten.
Zu einer prob nim das erst exempl / set den werde

diuidirt werde durch 3. Darumb laß dich alhie nie-
tiren / was oben im fünfften capitel des ersten teils
bey der diuision gesagt ist.

Die erst equation oder regl der cofs.

Wan 2wo quantitetn natürlicher ordnung einan-
der gleich werden / diuidir die kleiner in die grösser
quantitet / der quociens zeigt an den werdt 12e. Als
in disen exempln.

Die teiler

3 2e	6 9
4 8	8 2e
5 ce	10 8
6 38	12 ce
7 β	14 38 facit 12e. 29
8 3ce	16 β
9 68	18 3ce
10 388	20 68
11 ce	22 388

Die ander equation.

Wan 2wo quantitetn einander gleich werden / zwi-
schen welchen eine: natürlicher ordnung nach be-
griffen: geschwigen ist. Diuidir die kleiner in die
größer quantitet / radir quadrata des quociens zeigt
an den werdt 12e. Als

Die teiler

2 8	8 9
3 ce	12 2e
4 38	16 8
5 β	20 ce fa: 12e. 29
6 3ce	24 38
7 68	28 β
8 388	32 3ce
9 ce	36 68

Die dritt equation.

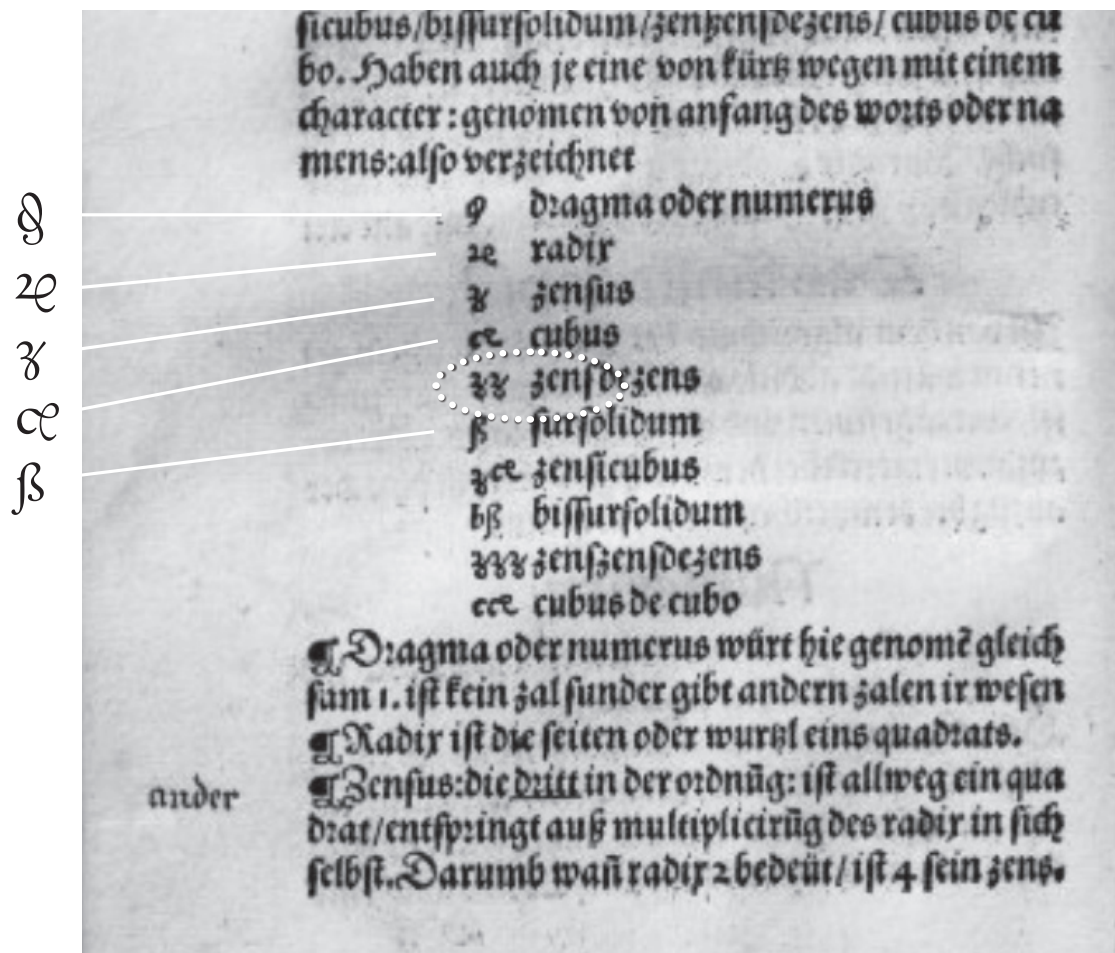
Wan 2wo quantitetn einander gleich werden / zwi-
schen welche 2wo andere: natürlicher ordnung nach
begriffen: geschwigen sein. Diuidir die kleiner in die
größer quantitet / radir cubica des quociens zeigt an
den werdt 12e. Als

Die teiler

2 ce	16 9
3 38	24 2e
4 β	32 8
5 3ce	40 ce fa: 12e. 22e. 29
6 68	48 38
7 388	56 β
8 ce	64 3ce

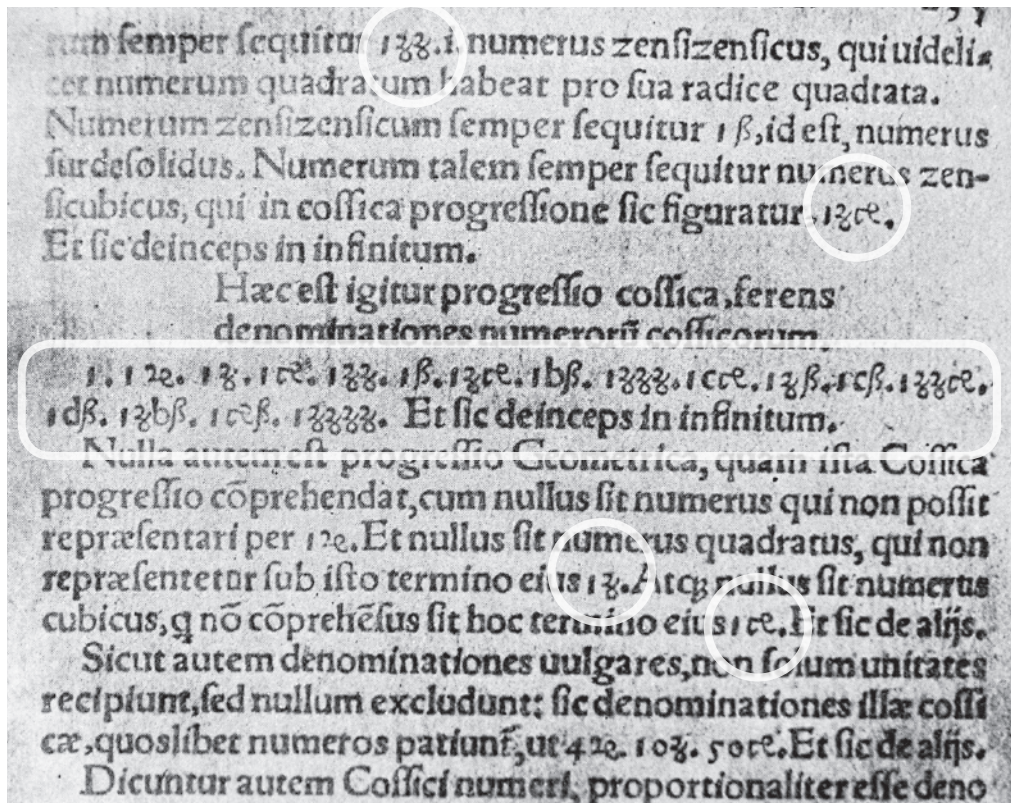
Die vierd equation

Wan 2wo quantitetn einander gleich werden / zwi-
schen welche / drey andere natürlicher ordnung nach
begriffen: geschwigen sein. Diuidir die kleiner in die
größer quantitet / Radir quadrata von radice qua-
drata des quociens / zeigt an den werdt 12e. Als

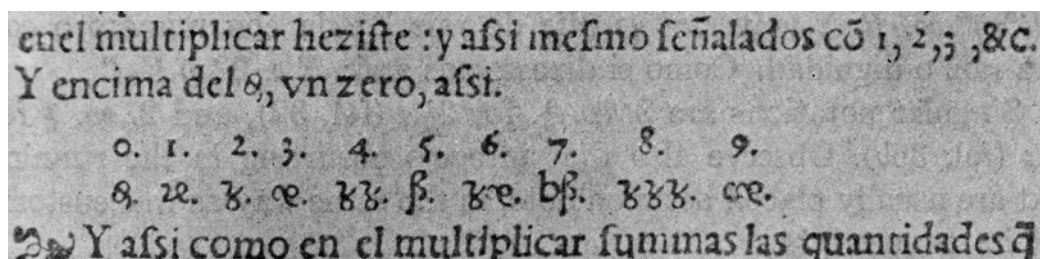


Christoff Rudolff: *Behend und hübsch Rechnung* ... Straßburg 1525, part of fol. 24v. In this chapter Rudolff introduces the set of root and power symbols by samples and explanations. We can see: ꝛ (LOWERCASE KURRENT Z), ȝ (LOWERCASE D ROTUNDA WITH CROSSING LOOP), ʒ (LOWERCASE R ROTUNDA WITH LOOP), ʒ (LOWERCASE C WITH RIGHT LOOP) and ʒ (LATIN SMALL LIGATURE LONG S WITH DESCENDER S).

This print demonstrates the deliberate distinction between the cossic character ꝛ and the normal fraktur ʒ (see at ꝛ). Whereas in other scenarios this two shapes could be seen as ‘just’ glyph variants without semantic distinction, in this case the form difference is clearly an indicator for a specific meaning. The character ꝛ (LOWERCASE KURRENT Z) is denoting *zensus*. It is graphically characterized by a) a round-shaped upper part (mostly), and b) a prominent loop descender which crosses upwards. The origin of its shape is neither *Fraktur* type nor Latin script style but the German *Kurrent* writing style.



Stifel 1544 (after Cajori). This sample shows *z* (LOWERCASE KURRENT Z), *r* (LOWERCASE R ROTUNDA WITH LOOP), *c* (LOWERCASE C WITH RIGHT LOOP) and *s* (LATIN SMALL LIGATURE LONG S WITH DESCENDER S).



Aurel 1552, fol. 73B (after Cajori). This sample shows *z* (LOWERCASE KURRENT Z) (2., 4., 6., 8.), *d* (LOWERCASE D ROTUNDA WITH CROSSING LOOP) (0.), *r* (LOWERCASE R ROTUNDA WITH LOOP) (1.), *c* (LOWERCASE C WITH RIGHT LOOP) (3., 6., 9.), and *s* (LATIN SMALL LIGATURE LONG S WITH DESCENDER S) (5., 7.).

These samples also show how those characters were used in combination to express the powers 4th and so on.

8

nous fournit de termes consecutiz, pour expo-
ser les nombres Radicaus e leurs Sing:s:comme
vous voyez par la Table ici mise.

O, I, 2, 3, 4 5, 6, 7, 8, 9, IO,
I, R, G, C, GG, B, CC, bB, CGC, CC, GB,
I, 2, 4, 8, 16, 32, 64, 128, 256, 512, 1024,

II, 12, 13, 14, 15, 16.
cB, CGC, dB, CB, CC, CC.
2048, 4096, 8192, 16384, 32768, 65536.

L'ordre des Exposans composez.

4, 6, 8, 9, 10, 12, 14, 15, 16, 18, 20, 21, 22, 24,
25, 26, &c.

L'ordre des Singes composez.

ㄨㄨ, ㄨㄩ, ㄨㄨㄨ, ㄩㄩ, ㄨㄨ, ㄨㄨㄩ, ㄨㄨㄨ. &c. La ou
 vous noterez, que le Chantique  t toujours
 participant, ou le Cube redouble.

L'ordre des Exposans incompofez.

Exemple de la Diuifion.

Je veù diuifer 308 m. 58^{Re}, p. 24, par 5^{Re} m. 3.
La posicion s'era comme vous voyez.

40
 $3 \text{ } \theta \text{ } \zeta \text{ m. } 5 \text{ } 8 \text{ } \text{R} \text{ p. } 24$
 $5 \text{ } \text{R} \text{ m. } 3.$ (6R.)

 $3 \text{ } \theta \text{ } \zeta \text{ m. } 1 \text{ } 8 \text{ } \text{R}.$

(GR.

Le di donq einfi : 5 an 30 font com-

Three extracts from Peletier 1554: ç LOWERCASE C WITH DESCENDER, ç LOWERCASE C WITH RIGHT LOOP and ß LATIN SMALL LIGATURE LONG S WITH DESCENDER S.

These samples also demonstrate the usage of \mathbb{R}_7 (A776) as part of the cossic set, as well as the use of slashed digits.

to uoide the tedious repetition of these woordes: is equalle to: I will sette as I doe often in woorkes bse, a paire of paralleles, or Gemowe lines of one lengthe, thus:=====, bicause noe. 2. thynges, can be moare equalle. And now marke these numbers.

1. 14.ze. + 15.g. = 71.g.
2. 20.ze. = 18.g. = 102.g.
3. 26.z. + 10ze. = 9.z. + 10ze. + 213.g.
4. 19.ze. + 192.g. = 10z. + 108g. + 19ze.
5. 18.ze. + 24.g. = 8.z. + 2.ze.
6. 34z. = 12ze. = 40ze. + 480g. + 9.z.
1. In the firste there appeareth. 2. numbers, that is
14.ze.

Another Example of Addition.

$$\begin{array}{rcl}
 5.z.c. + 20.c. & = & 3.s.z. \\
 \hline
 5.z.c. + 3.s.z. & \text{to} & 20.c. + 6.s.z. \\
 \hline
 6.c.c. & & 6.c.c. \\
 \hline
 6.c.c. & &
 \end{array}$$

That is in les-
ser termes.

$$\begin{array}{rcl}
 5.c. + 20.g. & = & 3.z. \\
 \hline
 6.z.c. & &
 \end{array}$$

Here is noe multiplication, no2 reduction to one common denominato2: sith thei bee one all ready: no2

Two extracts from Recorde 1557 (after Cajori): c LOWERCASE C WITH RIGHT LOOP, § LOWERCASE D ROTUNDA WITH CROSSING LOOP, ze LOWERCASE R ROTUNDA WITH LOOP and z (LOWERCASE KURRENT Z).

nis, a diuerſe *Arithmetike* from the other. Practiſe bryngeth in, here, diuerſe compounding of Numbers: as ſome tyme, two, three, foure (or more) *Radicall* nũbers, diuerſly knit, by ſignes, of More & Leſſe: as thus $\sqrt{8} 12 + \sqrt{c} 15$. Or thus $\sqrt{8} 8 19 + \sqrt{c} 12 - \sqrt{8} 2$. &c. And ſome tyme with whole numbers, or fractions of whole Number, amõg them: as $20 + \sqrt{8} 24. \sqrt{c} 16 + 33 - \sqrt{8} 10. \sqrt{8} 8 44 + 12 \div + \sqrt{c} 9$. And ſo infinitely, may hap the varietie. After this: Both the one and the other.

Example from Dee 1570 (after Cajori): Ꝣ LOWERCASE C WITH RIGHT LOOP and ꝥ (LOWERCASE KURRENT Z).

0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10,
 1, Ꝣ, ꝥ, ꝥꝥ, Ꝣ, ꝥꝥ, ꝢꝢ, ꝥꝥꝥ, ꝥꝥꝥ, ꝥꝢ,
 1, 2, 4, 8, 16, 32, 64, 128, 256, 512, 1024,
 11, 12, 13, 14, 15, 16,
 ꝥꝢ, ꝥꝥꝥ, ꝢꝢ, ꝥꝢꝢ, ꝥꝢꝢ, ꝥꝥꝥꝥ,
 2048, 4096, 8192, 16384, 32768, 65536.

From Peletier 1620.

C A P. XXVIII. 159

Sit rursus Binomium primum $72 + \sqrt{8} 2880$. Maius nomen 72 . fecabitur in duas partes producentes 720 . quartam partem quadrati 2880 . maioris nominis, hac ratione. Semissis maioris nominis 72 . est 36 . a cuius quadrato 1296 . detracta quarta pars prædicta 720 . relinquit 576 . cuius radix 24 . addita ad semissem nominatam 36 . & detracta ab eadem, facit partes quasiras 60 . & 12 . Ergo radix Binomij est $\sqrt{8} 60 + \sqrt{8} 12$. quod hic probatum est per multiplicationem radices in se quadratè.

Sit quoque elicienda radix ex hoc residuo sexto $\sqrt{8} 60 - \sqrt{8} 12$. Maius nomen $\sqrt{8} 60$. distribuetur in duas partes producetes 3 . quartam partem quadrati 12 . minoris nominis, hoc pacto. Semissis maioris nominis $\sqrt{8} 60$. est $\sqrt{8} 15$. a cuius quadrato 15 . detracta nominata pars quarta 3 . relinquit 12 . cuius radix $\sqrt{8} 12$. addita ad semissem $\sqrt{8} 15$. prædictam, & ab eadem sublata facit partes $\sqrt{8} 15 + \sqrt{8} 12$. & $\sqrt{8} 15 - \sqrt{8} 12$. Ergo radix dicti Residui sexti est $\sqrt{8} (\sqrt{8} 15 + \sqrt{8} 12) - \sqrt{8} (\sqrt{8} 15 - \sqrt{8} 12)$ quod hic probatum est.

$\sqrt{8} 60 + \sqrt{8} 12$
$\sqrt{8} 60 + \sqrt{8} 12$
$+ \sqrt{8} 720 + 12$
$60 + \sqrt{8} 720$
$72 + \sqrt{8} 2880$

$\sqrt{8} (\sqrt{8} 15 + \sqrt{8} 12) - \sqrt{8} (\sqrt{8} 15 - \sqrt{8} 12)$
$\sqrt{8} (\sqrt{8} 15 + \sqrt{8} 12) - \sqrt{8} (\sqrt{8} 15 - \sqrt{8} 12)$
Quadrata partium. $\sqrt{8} 15 + \sqrt{8} 12$ & $\sqrt{8} 15 - \sqrt{8} 12$
$- \sqrt{8} 3$
$- \sqrt{8} 3$
Summa. $\sqrt{8} 60 - \sqrt{8} 12$

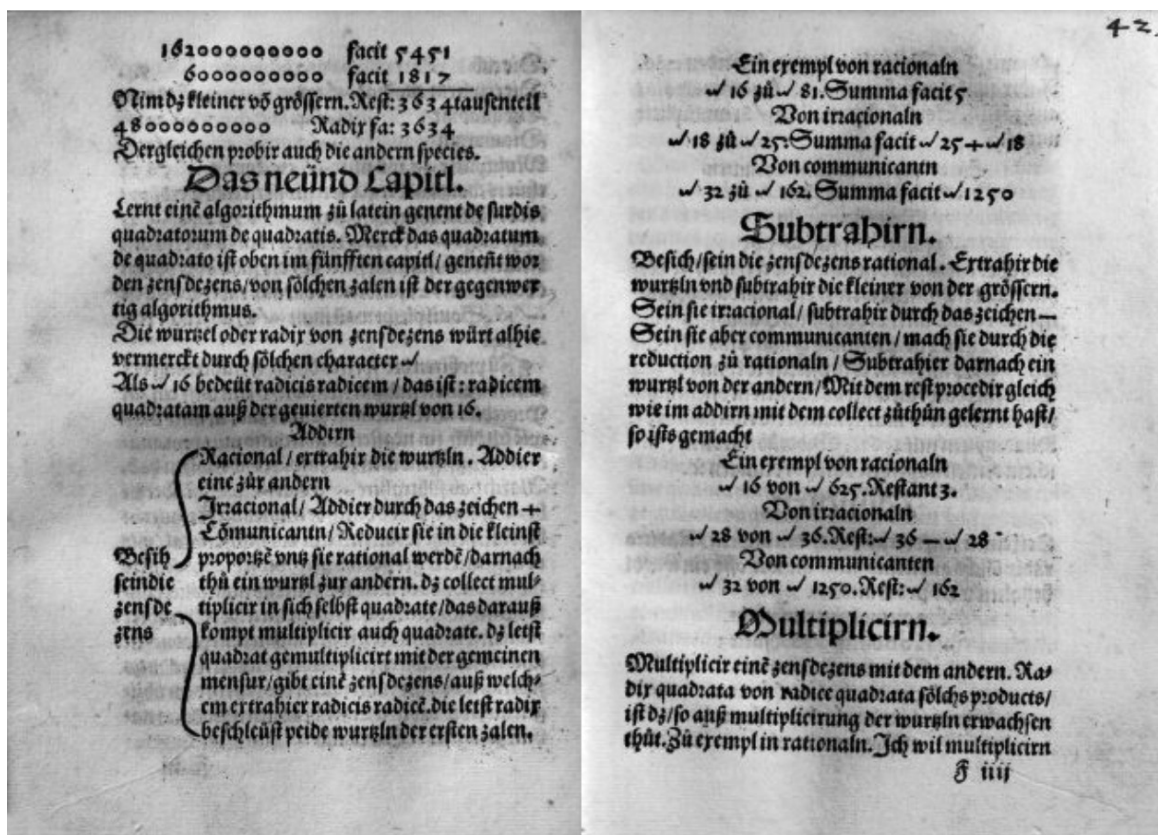
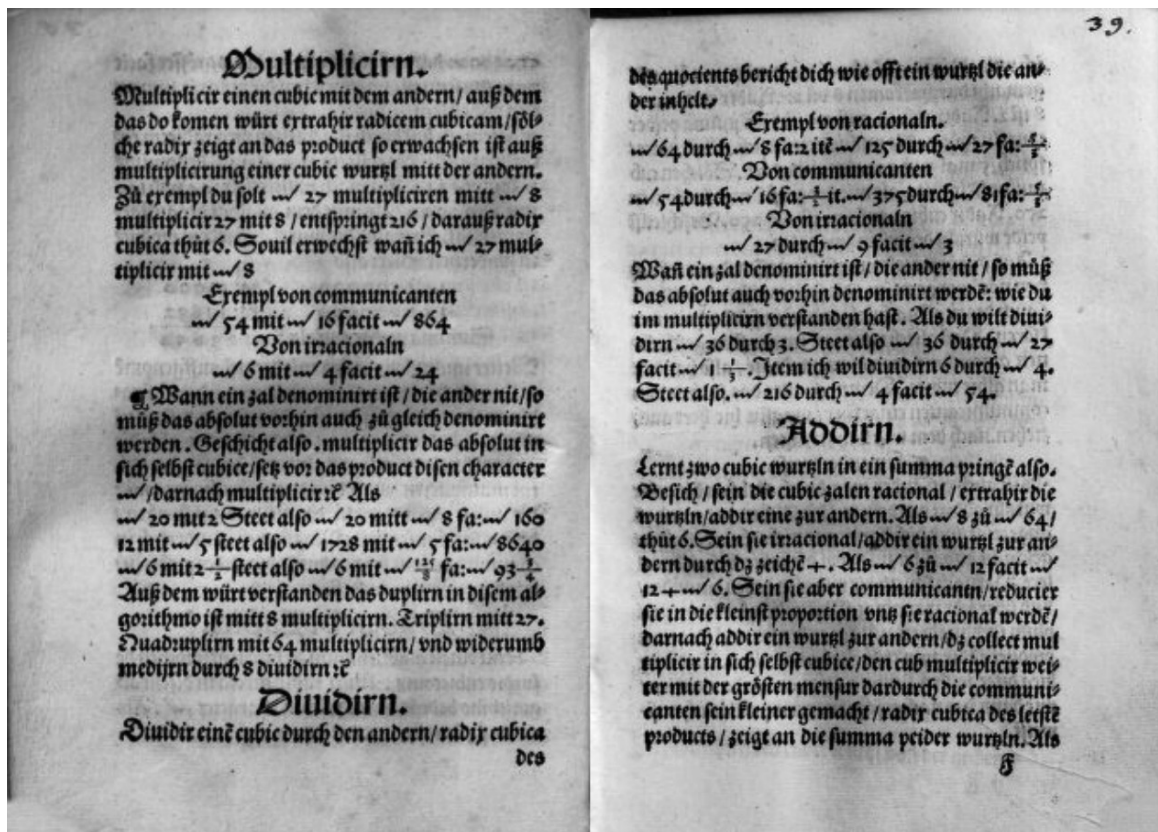
Clavius 1608 (after Cajori): ꝥ (LOWERCASE KURRENT Z). In this setting of Roman type style the common z character will have the usual Greek-Latin ‘Zeta’ shape, z, whereas the symbol for *zensus* retains not only the z initial (in this Latin treatise one may expect *census* instead), but also the specific *kurrent* script form of the letter.

\mathfrak{z}
 \mathfrak{z}
 \mathfrak{z}
 \mathfrak{z}

72		De Notatione Algebraica.		C A I	
Nomina.		Characteres.		Pot.	
Radix	\mathfrak{z}	R	A	a	a
Quadratum	$\mathfrak{z}\mathfrak{z}$	\mathfrak{Q}	Aq	aa	a ²
Cubus	$\mathfrak{z}\mathfrak{z}\mathfrak{z}$	C	Ac	aaa	a ³
Quad. quadratum	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	$\mathfrak{Q}\mathfrak{Q}$	Aqq	aaaa	a ⁴
Surdefolidum	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	S	Aqc	&c.	a ⁵
Quad. Cubi.	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	$\mathfrak{Q}\mathfrak{C}$	Acc		a ⁶
2 ^m Surdefolidum.	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	bS	Aqqc		a ⁷
Quad. quad. quad.	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	$\mathfrak{Q}\mathfrak{Q}\mathfrak{Q}$	Aqcc		a ⁸
Cubi cubus	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	CC	Accc		a ⁹
Quad. Surdefol.	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	$\mathfrak{Q}\mathfrak{S}$	Aqqcc		a ¹⁰
3 ^m Surdefolidum	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	cS	Aqccc		a ¹¹
Quad. quad. cubi	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	$\mathfrak{Q}\mathfrak{Q}\mathfrak{C}$	Acccc		a ¹²
4 ^m Surdefolidum	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	dS	Aqqccc		a ¹³
Quad. 2 ⁱ Surdefol.	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	$\mathfrak{Q}\mathfrak{b}\mathfrak{S}$	Aqcccc		a ¹⁴
Cubus Surdefol.	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	CS	Accccc		a ¹⁵
Quad. quad. quad. quad.	$\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}\mathfrak{z}$	$\mathfrak{Q}\mathfrak{Q}\mathfrak{Q}\mathfrak{Q}$	Aqqcccc		a ¹⁶
&c.					

From Wallis, Operum mathematicorum, 1657 (after Cajori); shows the use of \mathfrak{z} LOWERCASE LONG S WITH TOP LOOP for “sursolidum”.

The \mathfrak{z} (LOWERCASE KURRENT Z) has been given a sort of ‘Latinization treatment’ here, based rather on the Greek/Roman zeta shape. We regard this as a glyph variant with no distinctive meaning.



W SQUARE ROOT OF SQUARE ROOT

W SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT














































Christoff Rudolff: Behend und hübsch Rechnung durch die kunstreichen regeln Algebre, so gemeinlich die Cofs genennt werden. Straßburg 1525. fol. 38v-39r., 41v-42r

see also
next page

1 ① sec ① Produict d'une prime quantité par une prime
quantité secondement posée.
5 ④ ter ② Produict de cinq quartes quantitez par une
seconde quantité tiercement posée.
Les caracteres signifians racines de quels l'expli-
cation se trouve à la 29 & 30 definition sont tels :
✓ Racine de quarré.
✓✓ Racine de racine de quarré.
✓✓✓ Racine de racine de racine de quarré.
✓✓✓✓ Racine de racine de racine de racine de quarré.
✓ ③ Racine de cube.
✓✓ ③ Racine de racine de cube.
✓ ④ Racine de quarte quantité.
✓✓ ④ Racine de racine de quarte quantité, &c.
Le caractere signifiant la separation entre le si-
gne de racine & la quantité, duquel l'explication se
trouve à la 34. definition, est tel.
X, Comme ✓ 3 X ② n'est pas le mesme que ✓ 3 ②,
comme dict est à ladicte 34. definition.
Les caracteres signifians plus & moins, comme à
la 36 definition, sont tels :
+ Plus.
— Moins.
Et pour expliquer la racine d'un multinomie
(qu'aucuns appellent racine universelle) nous use-
rons le vocable du multinomie, comme:
✓ bino 2 + ✓ 3, c'est à dire racine quarrée de bino-
mie, ou de la somme de 2 & ✓ 3.
✓ trino ✓ 3 + ✓ 2 — ✓ 5, c'est à dire racine quarrée
de trinomie, ou de la somme de ✓ 3 & ✓ 2 & —
✓ 5.
✓ ③ bino ✓ 2 + ✓ 3, c'est à dire racine cubique de

✓ SQUARE ROOT OF SQUARE ROOT,
✓✓ SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT,
✓✓✓ SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT.
These characters can be seen related to the established radix symbol $\sqrt{\quad}$ (221A).
Simon Stevin, L'arithmétique in Œuvres mathématiques, 1634 (after Cajori)

9. Synopsis of historic Cossic characters (Group 1)

	Glyph	ð	ꝛ	ꝥ	Ꝩ	Ꝥ	Ꝭ	ß	ſ̊
	Character	LOWERCASE D ROTUNDA WITH CROSS- ING LOOP	LOWERCASE R ROTUNDA WITH LOOP	LOWERCASE KURRENT Z SIGN	LOWERCASE C WITH DESCENDER	LOWERCASE C WITH SMALL SLASH	LOWERCASE C WITH RIGHT LOOP	LATIN SMALL LIGA- TURE LONG S WITH DE- SCENDER S	LOWERCASE LONG S WITH TOP LOOP
	Meaning	dragma	radix	zensus	census	cubus	cubus	solidus sursolidum semis	sursolidum
1	Rudolf 1525								
2	Stifel 1544								
3	Aurel 1552								
4	Peletier 1554								
5	Reorde 1557								
6	Dee 1570								
7	Peletier 1620								
8	Clavius 1608/12								
9	Beeckmann 1628								
10	Wallis 1657								
11	Leibniz MS 1676								
12	MS Leiden 17. c.								
13	MS Ham- burg 17. c.								

Comparative survey of Coss characters in various sources, 1525 to 1676.

10. Unicode Character Properties

```
1D4CF FE02; kurrent style; # MATHEMATICAL SCRIPT SMALL Z

1DF90;LATIN LETTER SMALL C WITH SMALL SLASH;Sm;0;ON;;;;N;;;;;
1DF91;LATIN LETTER SMALL C WITH DESCENDER;Sm;0;ON;;;;N;;;;;
1DF92;LATIN LETTER SMALL C WITH RIGHT LOOP;Sm;0;ON;;;;N;;;;;
1DF93;LATIN LETTER SMALL D ROTUNDA WITH CROSSING LOOP;Sm;0;ON;;;;N;;;;;
1DF94;LATIN LETTER SMALL R ROTUNDA WITH LOOP;Sm;0;ON;;;;N;;;;;
1DF95;LATIN SMALL LIGATURE LONG S WITH DESCENDER S;Ll;0;L;<compat>00DF;;;;N;;;;;
1DF96;LATIN LETTER SMALL LONG S WITH TOP LOOP;Sm;0;ON;;;;N;;;;;

1CEDD;SQUARE ROOT OF SQUARE ROOT;Sm;0;ON;;;;N;;;;;
1CEDE;SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT;Sm;0;ON;;;;N;;;;;
1CEDF;SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT OF SQUARE ROOT;Sm;0;ON;;;;N;;;;;

1D6A6;MATHEMATICAL ITALIC LIGATURE LONG S WITH DESCENDER S;Sm;0;ON;<font>1DF95;;;;N;;;;;
```

11. Bibliography

LAA – refers to: Leibniz, Gottfried Wilhelm: Sämtliche Schriften und Briefe. (‘Leibniz-Akademie-Ausgabe’, many volumes)

LBr – refers to: Leibniz’s original correspondence papers, GWLB Hanover

LH – refers to: Leibniz’s original manuscripts, GWLB Hanover

Aurel, Marco: Arithmetica algebratica, Valencia 1552

Bombelli, Rafael: L’Algebra. Bologna 1579

— : L’Algebra. Milan 1966

Cajori, Florian: A history of mathematical notations. Chicago 1928

Cardano, Gerolamo: Opera omnia. Lyon 1663

Clavius, Christophorus: Algebra. Rome 1608

Dee, John: [preface] in: Euclid: The elements. Henry Billingsley (ed.), London 1570

Descartes, René: La Géométrie. Leiden 1637

Dulaurens, François: Specimina Mathematica. Paris 1667

Ghaligai, Francesco: Pratica d’Arithmetica, Florence 1552

Peletier, Jaques: L’Algèbre. Lyon 1554

Probst, Siegmund: Édition des symboles de Leibniz. PDF, Hanover 2023 (presentation Paris 2023)

Rudolff, Christoff: Behend und hübsch Rechnung durch die kunstreichen regeln Algebre, so gemeincklich die Coß genennt werden. Straßburg 1525

Stevin, Simon: Œuvres mathématiques. Leiden 1634

Stifel, Michael: Arithmetica integra. Nürnberg 1544

Wallis, John: De sectionibus conicis nova methodo expositis tractatus. Oxford 1655

— : Operum mathematicorum, Oxford 1657

— : Treatise of Algebra. London 1685

**ISO/IEC JTC 1/SC 2/WG 2
PROPOSAL SUMMARY FORM TO ACCOMPANY SUBMISSIONS
FOR ADDITIONS TO THE REPERTOIRE OF ISO/IEC 10646¹**

Please fill all the sections A, B and C below.

Please read Principles and Procedures Document (P & P) from <http://std.dkuug.dk/JTC1/SC2/WG2/docs/principles.html> for guidelines and details before filling this form.

Please ensure you are using the latest Form from <http://std.dkuug.dk/JTC1/SC2/WG2/docs/summaryform.html>.

See also <http://std.dkuug.dk/JTC1/SC2/WG2/docs/roadmaps.html> for latest **Roadmaps**.

A. Administrative

1. Title:	Proposal to encode 12 cossic characters		
2. Requester's name:	Uwe Mayer, Siegmund Probst, David Rabouin, Elisabeth Rinner, Andreas Stötzner, Achim Trunk, Charlotte Wahl		
3. Requester type (Member body/Liaison/Individual contribution):	Individual (work group)		
4. Submission date:	2025-11-25		
5. Requester's reference (if applicable):	LUCPL-2533		
6. Choose one of the following:			
This is a complete proposal:			Yes
(or) More information will be provided later:			

B. Technical – General

1. Choose one of the following:			
a. This proposal is for a new script (set of characters):			No
Proposed name of script:			
b. The proposal is for addition of character(s) to an existing block:			
Name of the existing block:	Latin Extended G, Miscellaneous Symbols Supplement, Mathematical Alphanumeric Symbols		
2. Number of characters in proposal:			12
3. Proposed category (select one from below - see section 2.2 of P&P document):			
A-Contemporary	B.1-Specialized (small collection)	Yes	B.2-Specialized (large collection)
C-Major extinct	D-Attested extinct		E-Minor extinct
F-Archaic Hieroglyphic or Ideographic			G-Obsecure or questionable usage symbols
4. Is a repertoire including character names provided?			Yes
a. If YES, are the names in accordance with the "character naming guidelines" in Annex L of P&P document?			Yes
b. Are the character shapes attached in a legible form suitable for review?			Yes
5. Fonts related:			
a. Who will provide the appropriate computerized font to the Project Editor of 10646 for publishing the standard?	Andreas Stötzner		
b. Identify the party granting a license for use of the font by the editors (include address, e-mail, ftp-site, etc.):	Andreas Stötzner Gestaltung, Klaufügelweg 21, 88400 Biberach/R., Germany, as@signographie.de		
6. References:			
a. Are references (to other character sets, dictionaries, descriptive texts etc.) provided?			Yes
b. Are published examples of use (such as samples from newspapers, magazines, or other sources) of proposed characters attached?			Yes
7. Special encoding issues:			
Does the proposal address other aspects of character data processing (if applicable) such as input, presentation, sorting, searching, indexing, transliteration etc. (if yes please enclose information)?			No

8. Additional Information:

Submitters are invited to provide any additional information about Properties of the proposed Character(s) or Script that will assist in correct understanding of and correct linguistic processing of the proposed character(s) or script. Examples of such properties are: Casing information, Numeric information, Currency information, Display behaviour information such as line breaks, widths etc., Combining behaviour, Spacing behaviour, Directional behaviour, Default Collation behaviour, relevance in Mark Up contexts, Compatibility equivalence and other Unicode normalization related information. See the Unicode standard at <http://www.unicode.org> for such information on other scripts. Also see Unicode Character Database (<http://www.unicode.org/reports/tr44/>) and associated Unicode Technical Reports for information needed for consideration by the Unicode Technical Committee for inclusion in the Unicode Standard.

¹ Form number: N4502-F (Original 1994-10-14; Revised 1995-01, 1995-04, 1996-04, 1996-08, 1999-03, 2001-05, 2001-09, 2003-11, 2005-01, 2005-09, 2005-10, 2007-03, 2008-05, 2009-11, 2011-03, 2012-01)

C. Technical - Justification

1. Has this proposal for addition of character(s) been submitted before?	Yes
If YES explain <i>see N5333R; L-2518 (N5333); L2/25-123 (L-2509)</i>	
2. Has contact been made to members of the user community (for example: National Body, user groups of the script or characters, other experts, etc.)?	Yes
If YES, with whom?	
Leibniz-Archiv, Forschungsstelle der Leibniz-Edition, Niedersächsische Landesbibliothek (GWLb), Hanover, Göttingen Academy of Science and Humanities in Lower Saxony (DE), Philium research group of CNRS (UMR 7219, laboratoire SPHERE) / Université de Paris VII; general: scholars, researchers, authors and editors working in the field of science history and upon editions of historic text corpora (e.g. of G. W. Leibniz, but also many others)	
If YES, available relevant documents: L-2409, L-2410	
3. Information on the user community for the proposed characters (for example: size, demographics, information technology use, or publishing use) is included?	Yes
Reference:	
4. The context of use for the proposed characters (type of use; common or rare)	Common
Reference: mainly specialist usage, scholarly, worldwide	
5. Are the proposed characters in current use by the user community?	Yes
If YES, where? Reference: mainly Europe, Americas; other countries	
6. After giving due considerations to the principles in the P&P document must the proposed characters be entirely in the BMP?	No
If YES, is a rationale provided?	
If YES, reference:	
7. Should the proposed characters be kept together in a contiguous range (rather than being scattered)?	No
8. Can any of the proposed characters be considered a presentation form of an existing character or character sequence?	No
If YES, is a rationale for its inclusion provided?	
If YES, reference:	
9. Can any of the proposed characters be encoded using a composed character sequence of either existing characters or other proposed characters?	Yes
If YES, is a rationale for its inclusion provided?	
If YES, reference: 1 variation sequence, see p. 4	
10. Can any of the proposed character(s) be considered to be similar (in appearance or function) to, or could be confused with, an existing character?	No
If YES, is a rationale for its inclusion provided?	
If YES, reference:	
11. Does the proposal include use of combining characters and/or use of composite sequences?	No
If YES, is a rationale for such use provided?	
If YES, reference:	
Is a list of composite sequences and their corresponding glyph images (graphic symbols) provided?	
If YES, reference:	
12. Does the proposal contain characters with any special properties such as control function or similar semantics?	No
If YES, describe in detail (include attachment if necessary)	
13. Does the proposal contain any Ideographic compatibility characters?	No
If YES, are the equivalent corresponding unified ideographic characters identified?	
If YES, reference:	